

Magnetic Resonance Imaging in Turbulent Flows

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UNIVERSITY OF NEW BRUNSWICK DEPARTMENT OF

PHYSICS



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MAKE A SIGNIFICANT DIFFERENCE IN

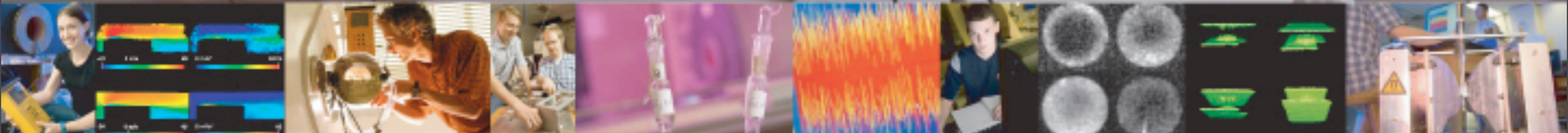
PHYSICS

Magnetic Resonance Imaging
Atomic & Molecular Physics
Space & Atmospheric Physics

UNIVERSITY OF NEW BRUNSWICK DEPARTMENT OF PHYSICS

MAGNETIC RESONANCE IMAGING (MRI)

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MAKE A SIGNIFICANT DIFFERENCE IN

PHYSICS

The UNB MRI Centre



materials MRI (short signal lifetimes)

The UNB MRI Centre



materials MRI (short signal lifetimes)

The UNB MRI Centre



materials MRI (short signal lifetimes)

The UNB MRI Centre

materials MRI (short signal lifetimes < 1 ms)

single point ramped imaging with T_1 enhancement

(SPRITE)

motion-sensitised SPRITE

Why? Turbulent Flow.

Turbulence is still incompletely described.



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Many natural and engineering flows are turbulent.



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Many natural and engineering flows are turbulent.

We have collaborators who are interested in

- fish migration in rivers
- validation of CFD codes
- steam turbines
- cardiovascular flows



Why? MRI.

There are lots of ways to measure flow.

Magnetic resonance imaging is non-invasive
(*cf.* particle imaging velocimetry, hot wire/film anemometry, laser doppler anemometry).

It is not point-by-point.

(*cf.* HWA, some LDA, some ultrasound)

It doesn't care about optical opacity

(*cf.* PIV, LDA)

Why not? MRI.

There are lots of ways to measure flow.

Magnetic resonance imaging is low resolution and/or slow.
(cf. LDA).

MRI does care about RF opacity
(cf. metal pipes can be a problem)

Why not? MRI.

There are lots of ways to measure flow.

Magnetic resonance imaging is low resolution and/or slow.

(*cf.* LDA).

MRI does care about RF opacity
(metal pipes can be a problem)

This is how it will end

MRI measures average propagators non-invasively, even in the dark.

SPRITE MRI can do it even when there are liquid/gas interfaces **or** just gas...
...and when the flow is “fast”.

The propagator contains information about average velocity **and** velocity fluctuation.

Order of Service

Magnetic Resonance Imaging (MRI)

SPRITE MRI with motion sensitisation

Advantages of SPRITE MRI in subsonic gas flow

Advantages of SPRITE MRI in two-phase flow

Run for the hills

Magnetic Resonance Imaging

Nuclei with spin angular momentum, \vec{J}

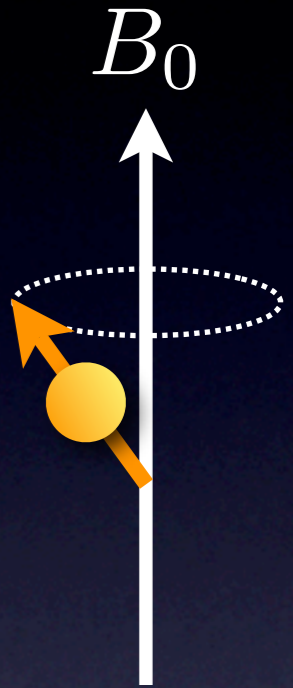
... have a magnetic dipole moment $\vec{\mu} = \gamma \vec{J}$

... and, by virtue of the two, precess around a static magnetic field at the **Larmor frequency**

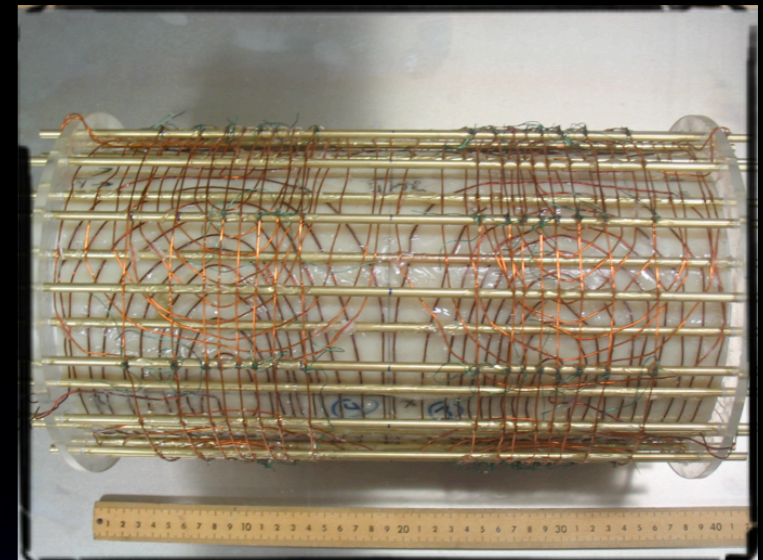
$$\omega_L = \gamma B_0$$

In the presence of a magnetic field gradient the precession frequency depends on position

$$\omega(\vec{r}) = \gamma \left(B_0 + \vec{G} \cdot \vec{r} \right)$$



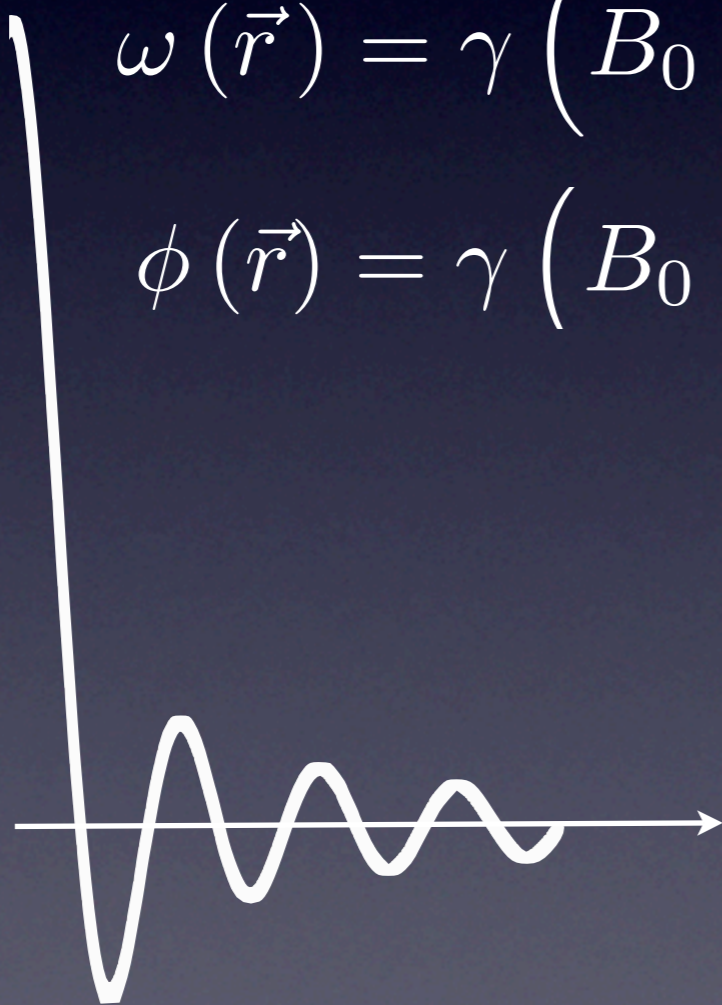
Spatial spectroscopy



In a magnetic field gradient
the precession frequency depends on position

$$\omega(\vec{r}) = \gamma \left(B_0 + \vec{G} \cdot \vec{r} \right)$$

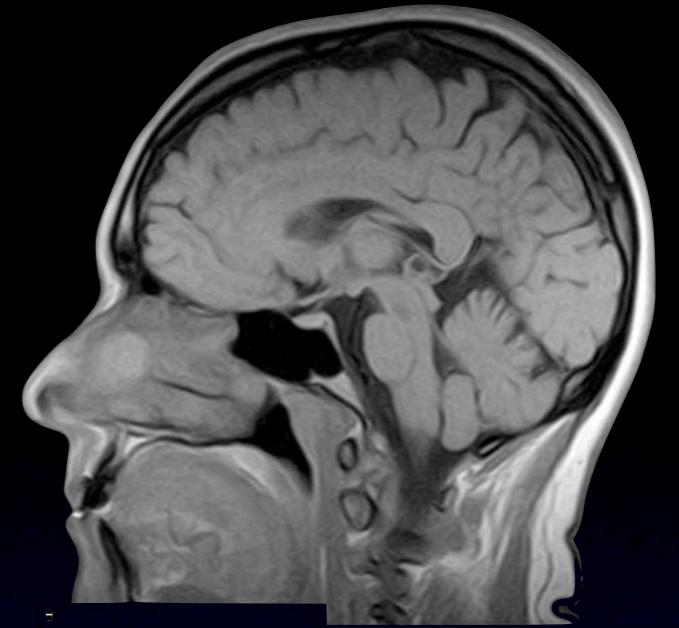
$$\phi(\vec{r}) = \gamma \left(B_0 + \vec{G} \cdot \vec{r} \right) t$$



FT
⇒

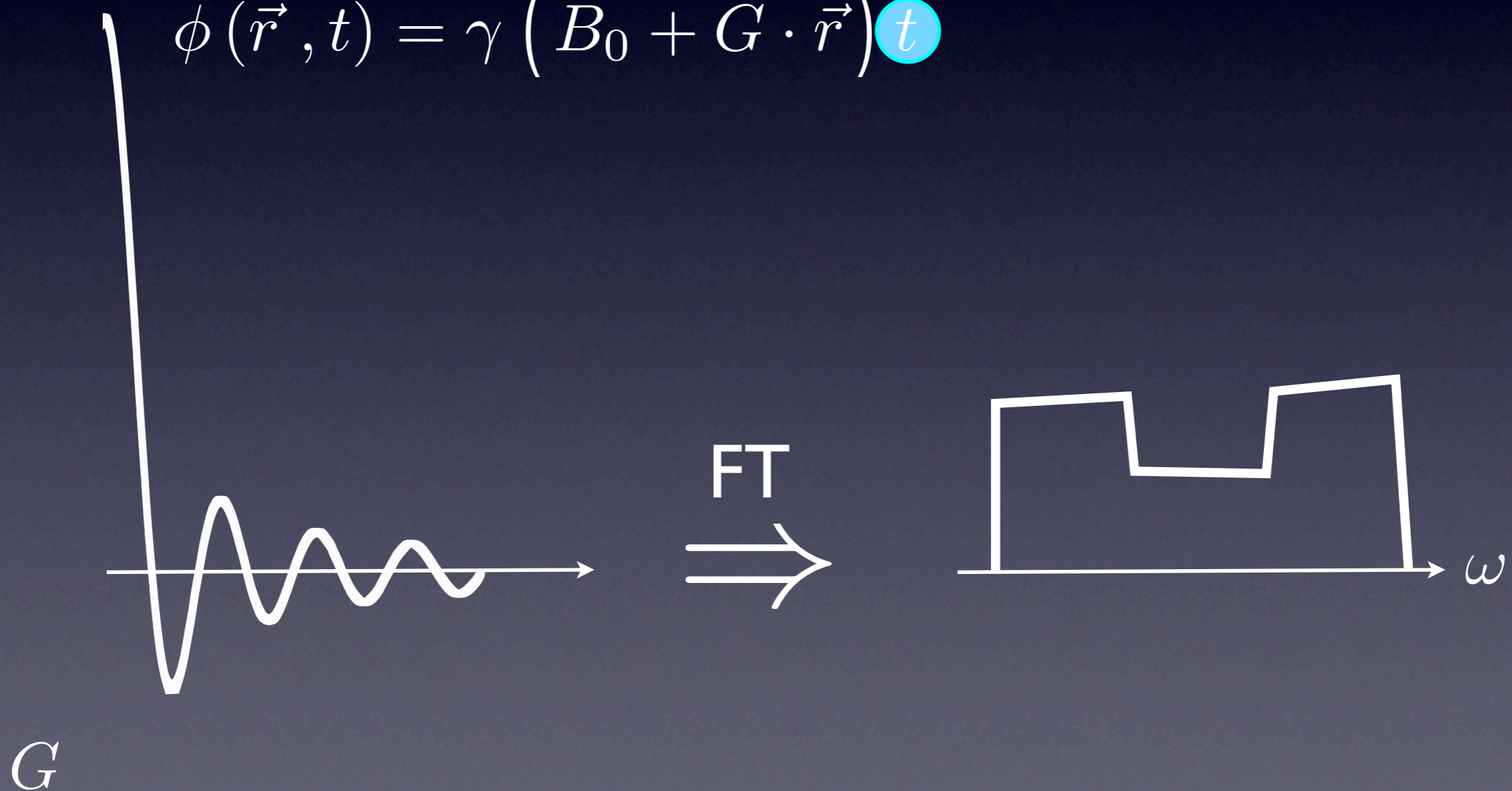


Spatial spectroscopy

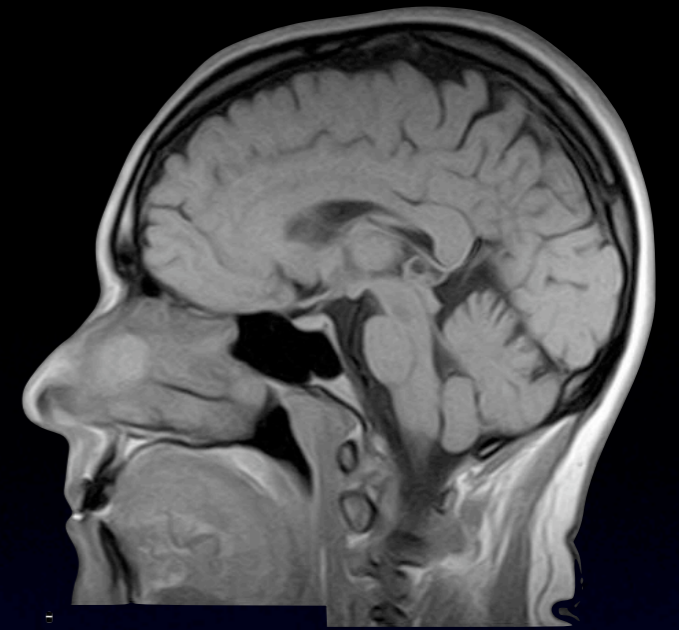


How should we sample the signal?
If we sample as a time axis, then...

$$\phi(\vec{r}, t) = \gamma (B_0 + \vec{G} \cdot \vec{r}) t$$

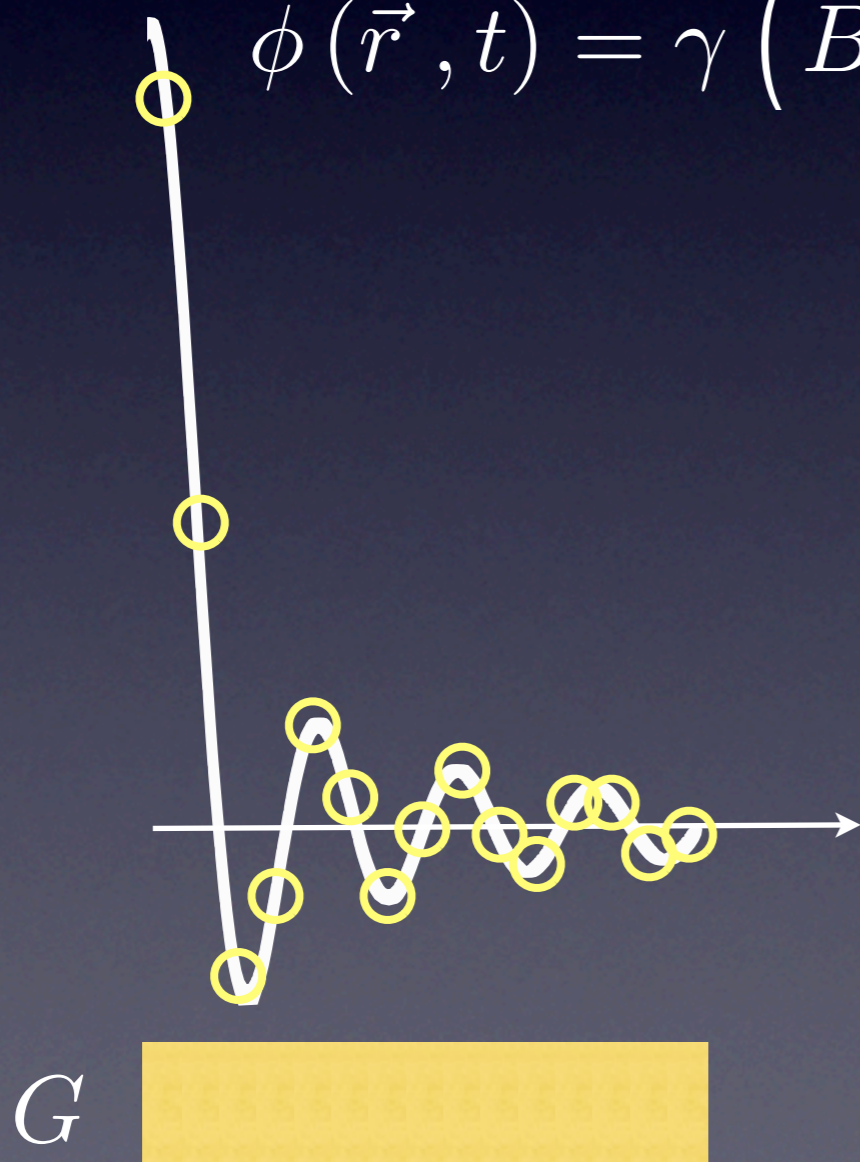


Spatial spectroscopy



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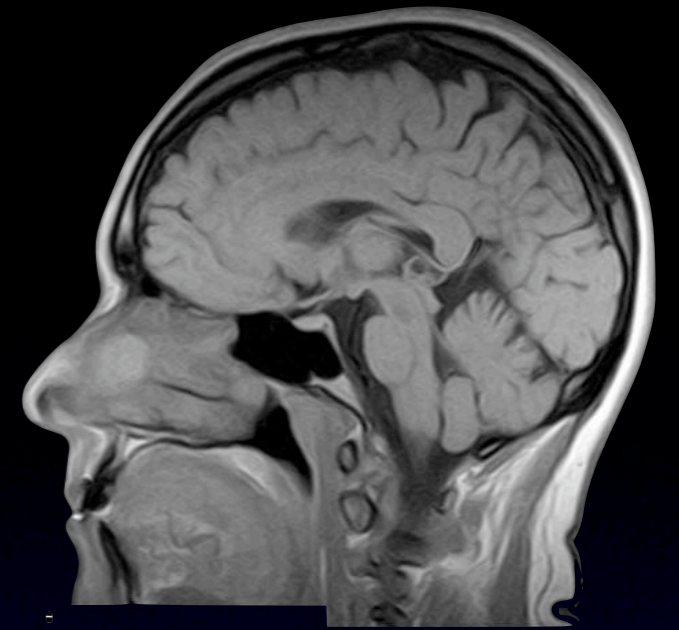
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FT
⇒



Spatial spectroscopy



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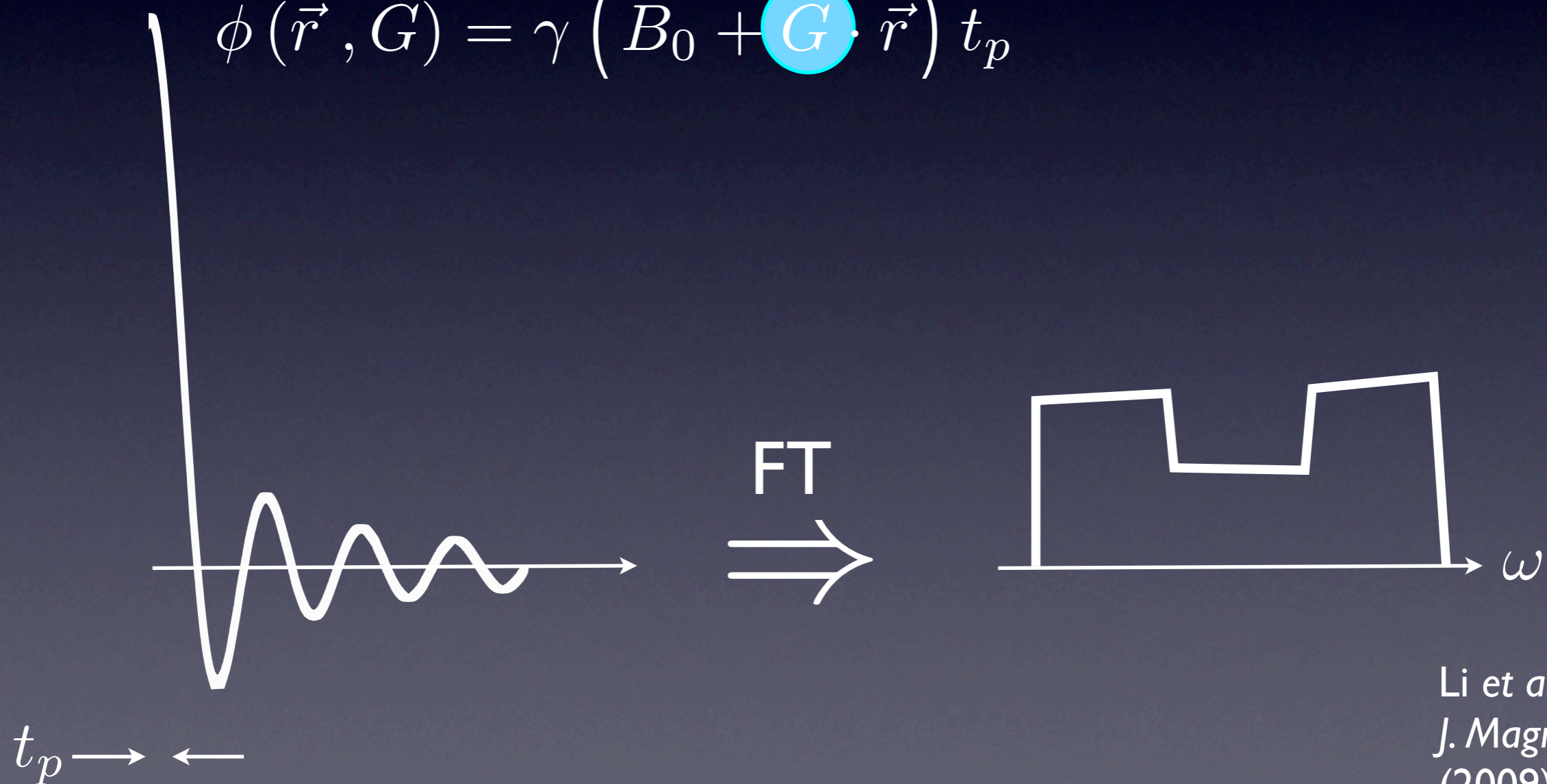
Unfortunately there are other things that cause time variation of MRI signal (relaxation)



Spatial spectroscopy

How should we sample the signal?
If we sample as a time axis, then

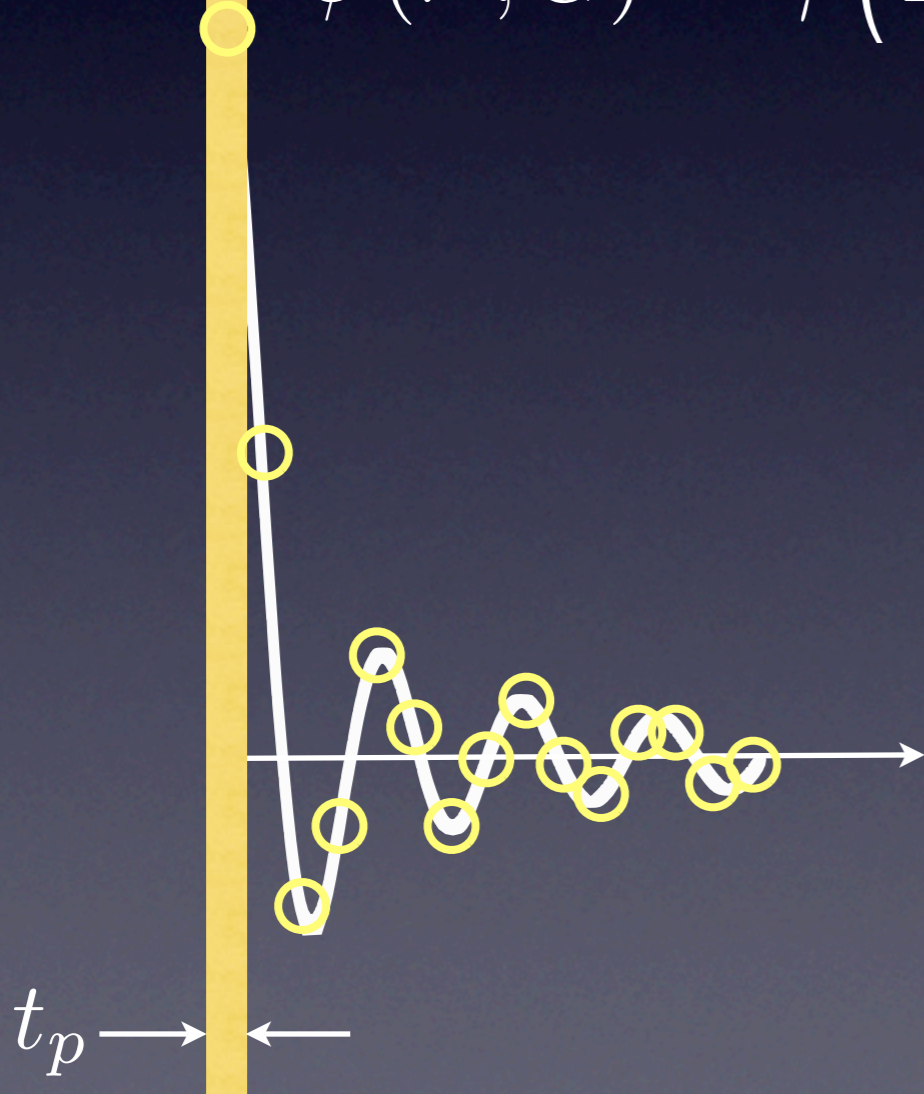
$$\phi(\vec{r}, \vec{G}) = \gamma \left(B_0 + \vec{G} \cdot \vec{r} \right) t_p$$



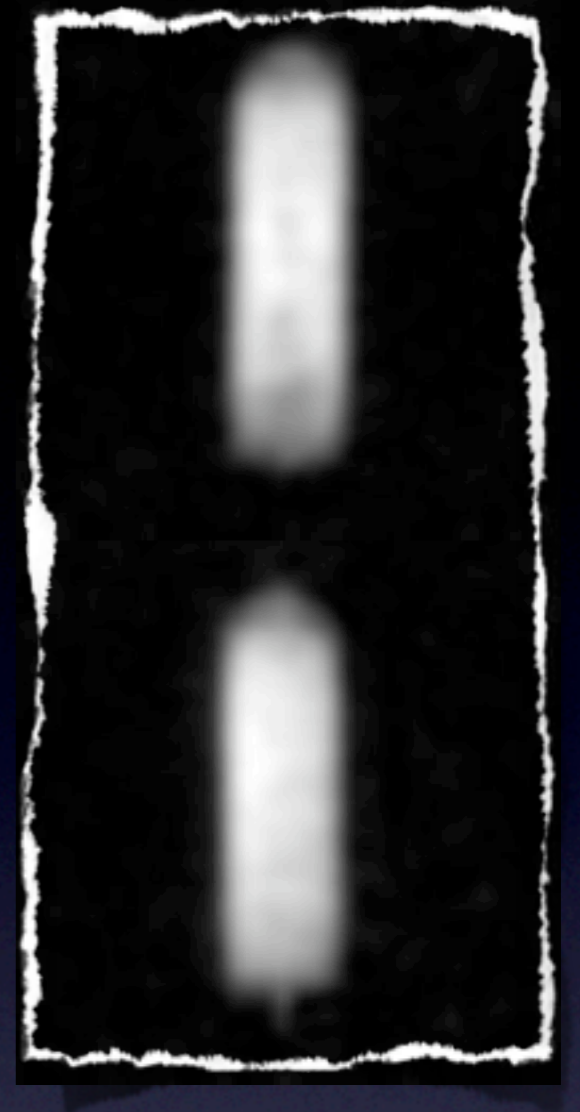
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FT
⇒

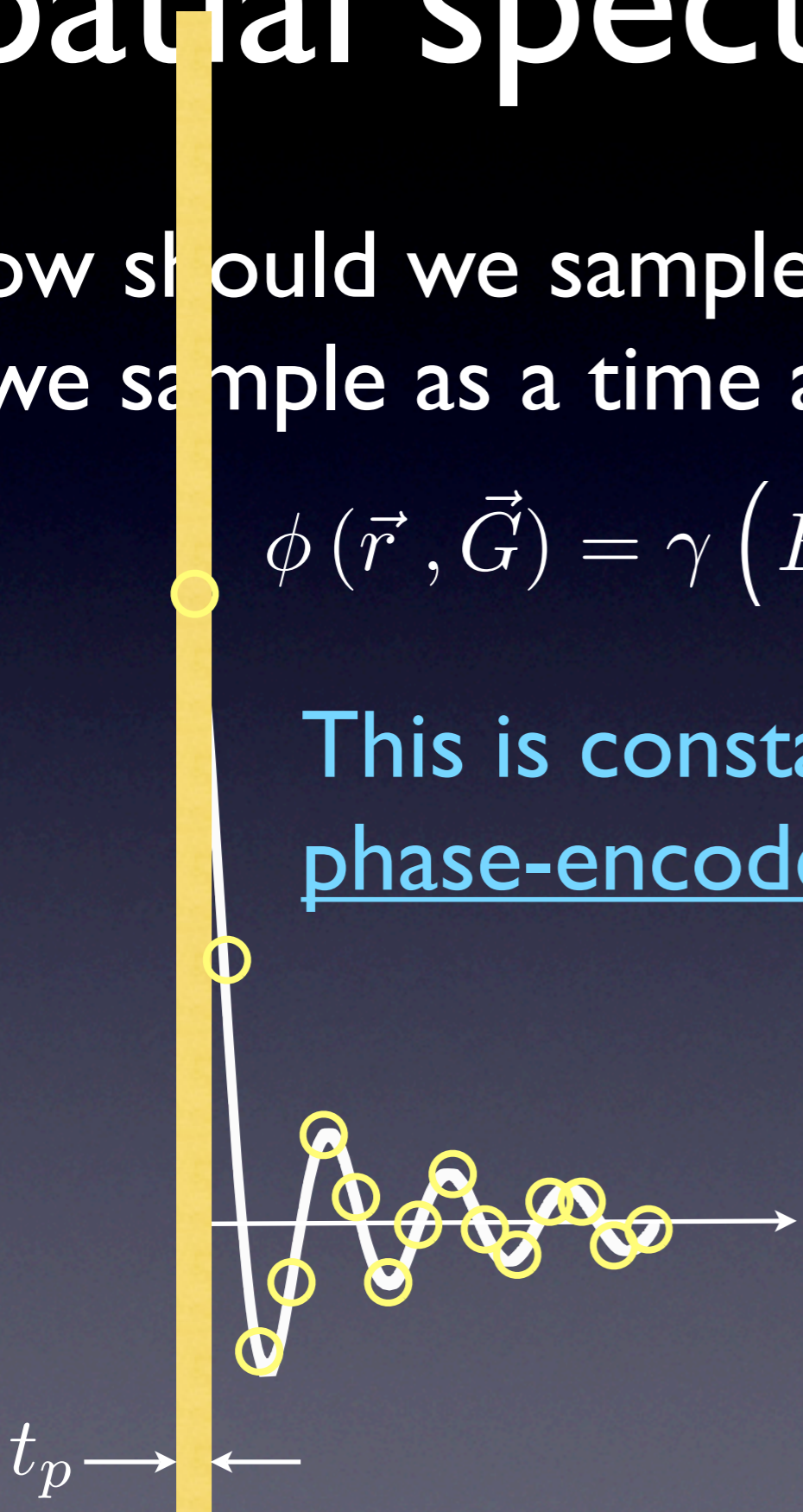
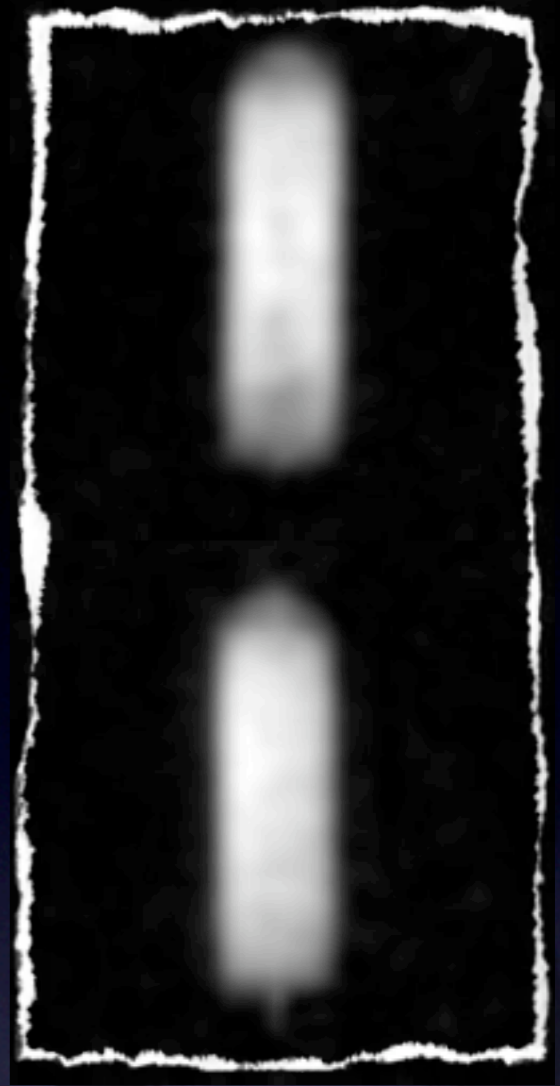


Spatial spectroscopy

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This is constant time (or purely phase-encoded) MRI: our version is SPRITE.



FT
⇒

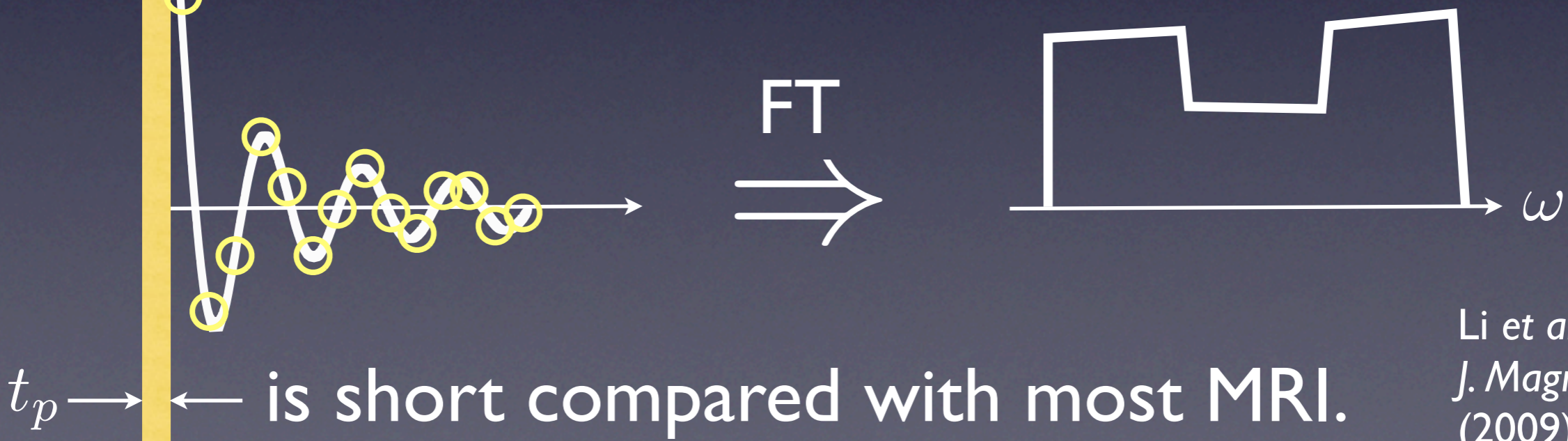
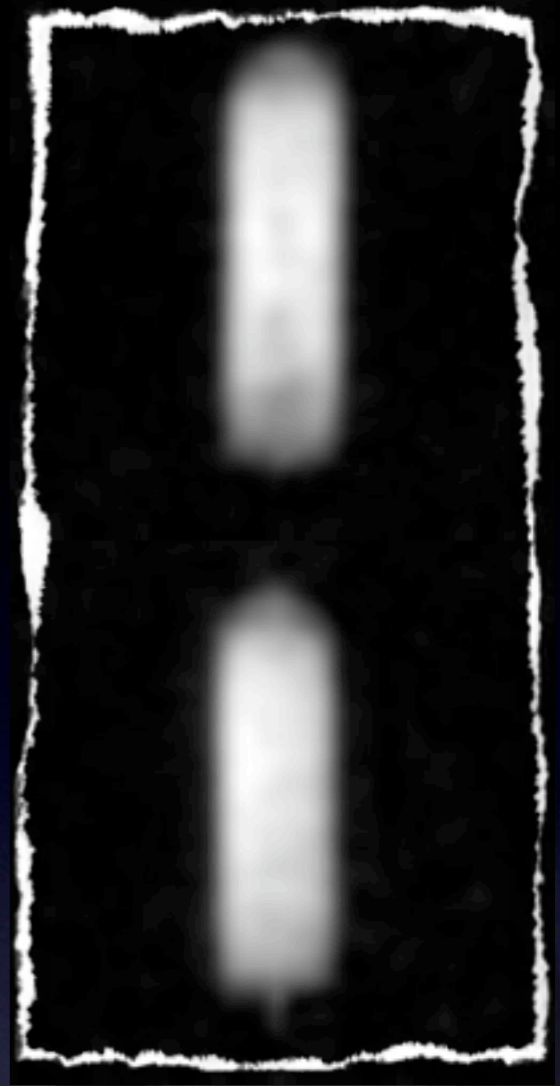


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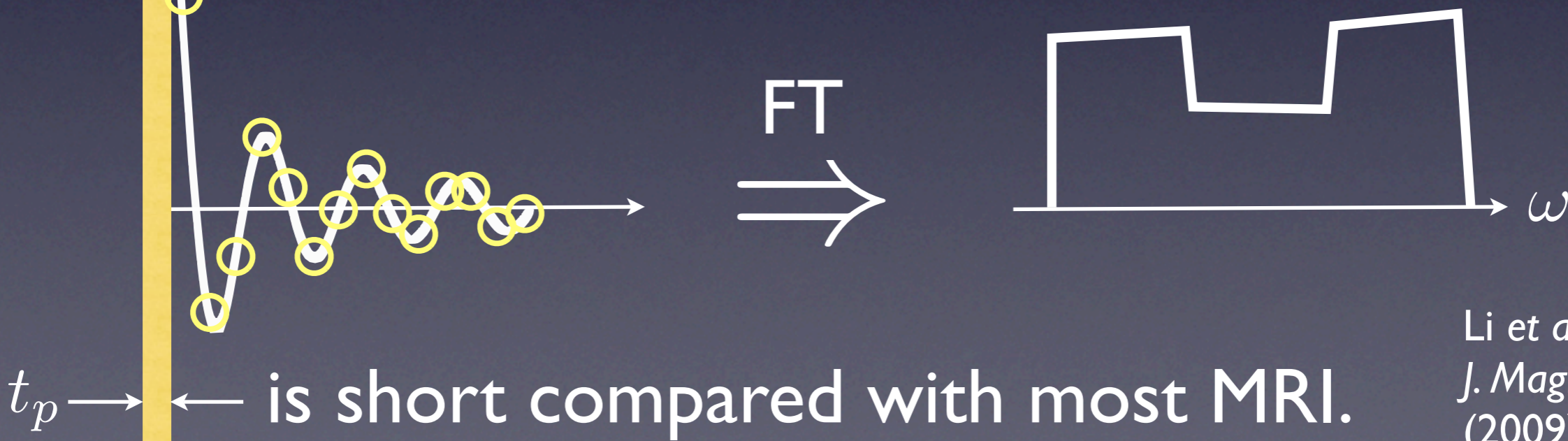
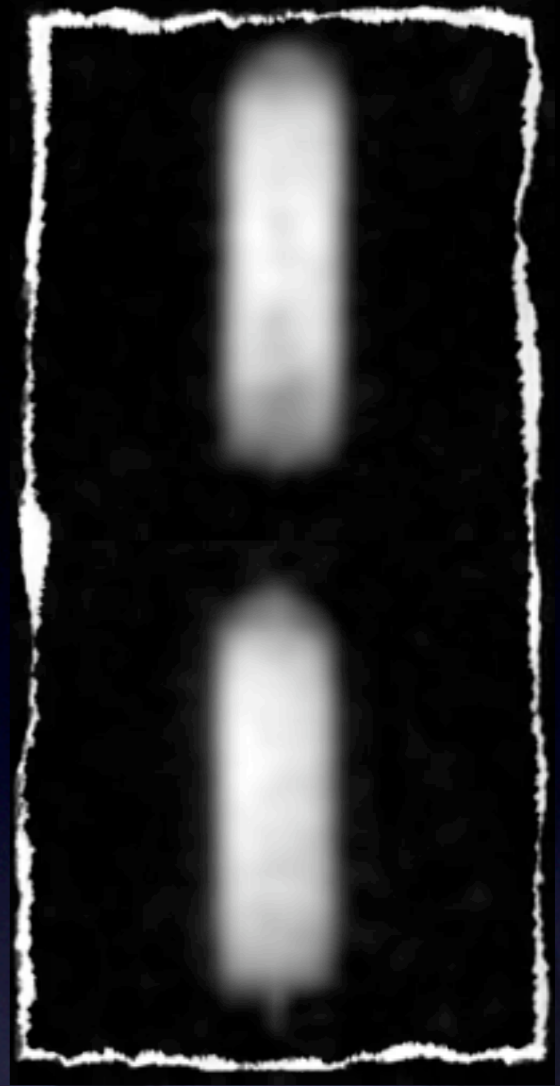


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Purely phase-encoded MRI

The encoding time t_p is **short**: this is good for short-lived signal....

... *and* for fast flow ($\gg 1$ m/s)

The encoding time t_p is **constant**: this is good for time-varying effects:

- signal relaxation

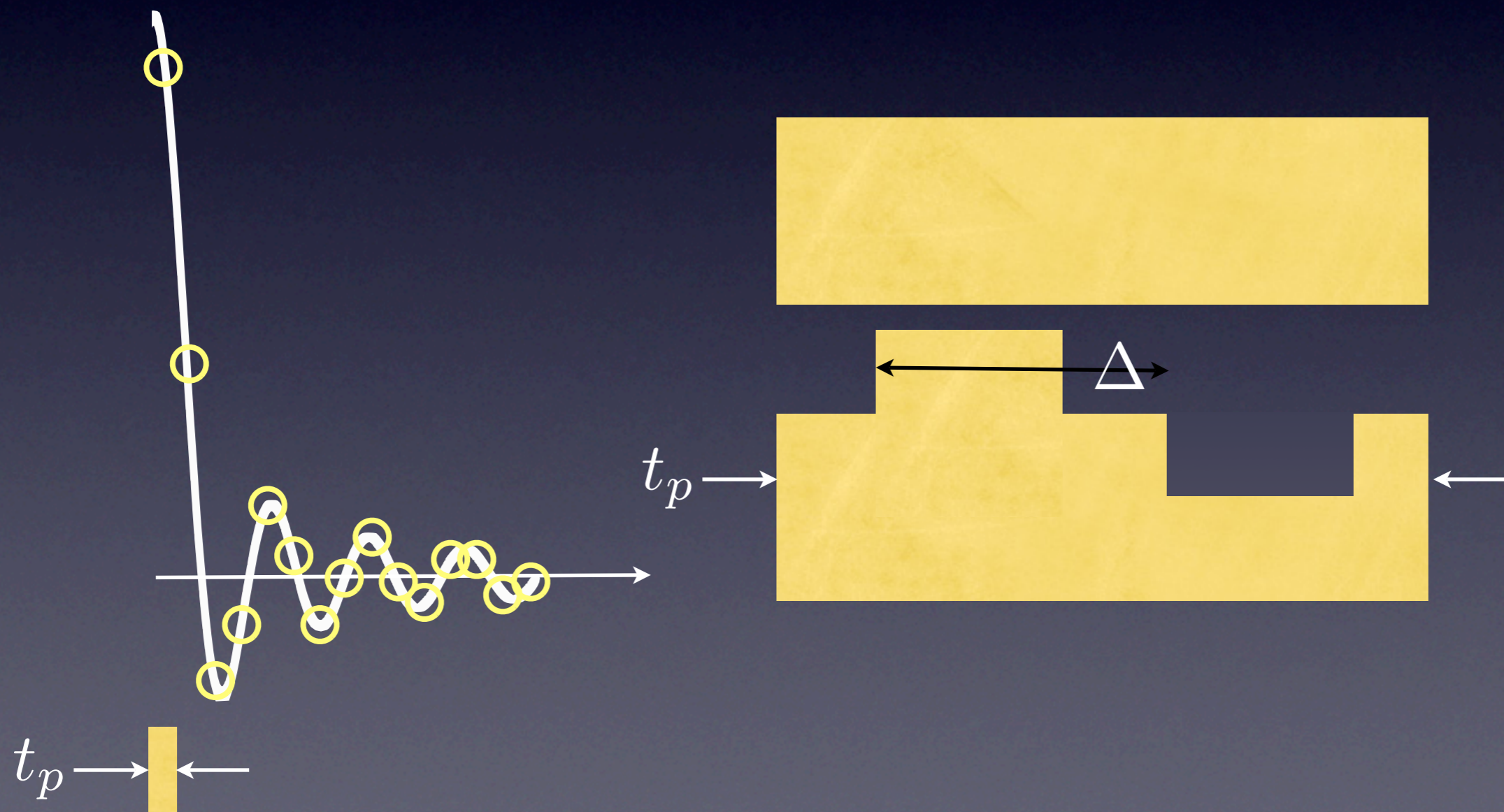
- magnetic susceptibility effect

- turbulent flow

leading to quantitative imaging.

Motion sensitisation

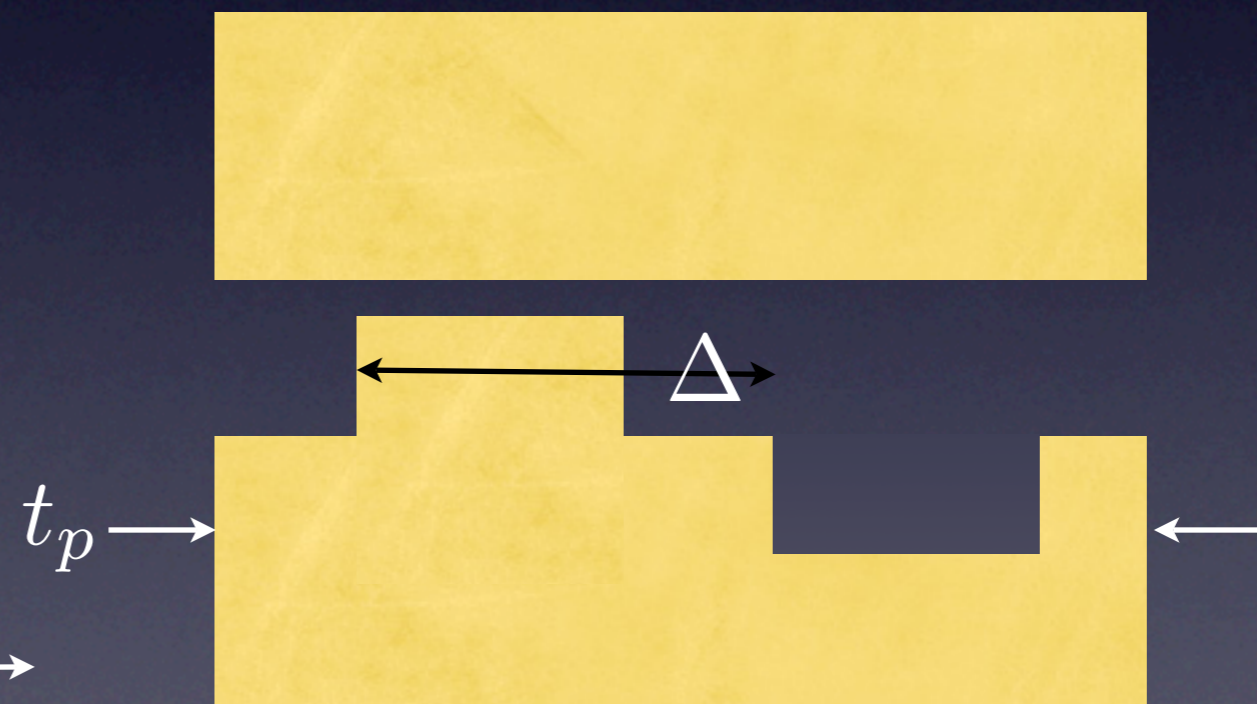
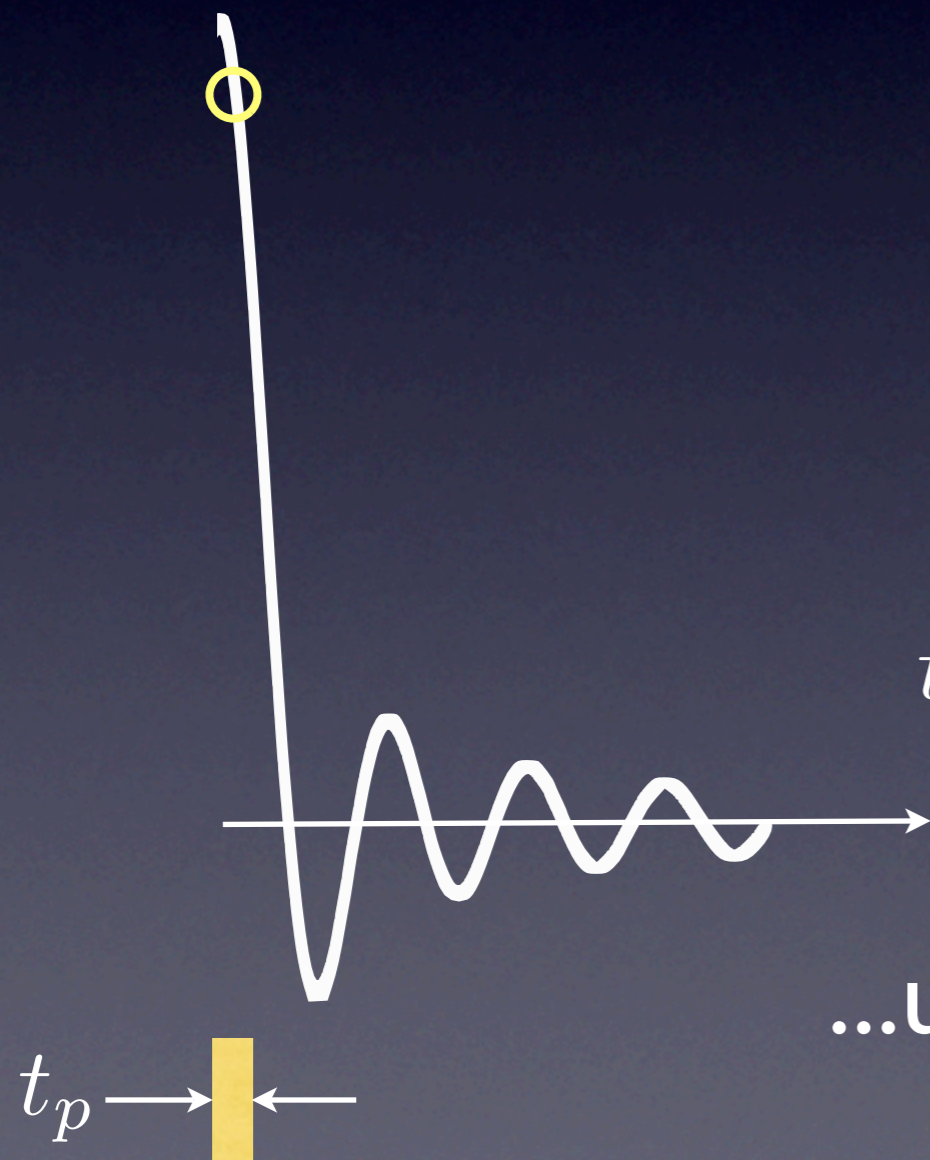
Notice that the gradient area is important in determining the phase.



Motion sensitisation

Notice that the gradient area is important in determining the phase.

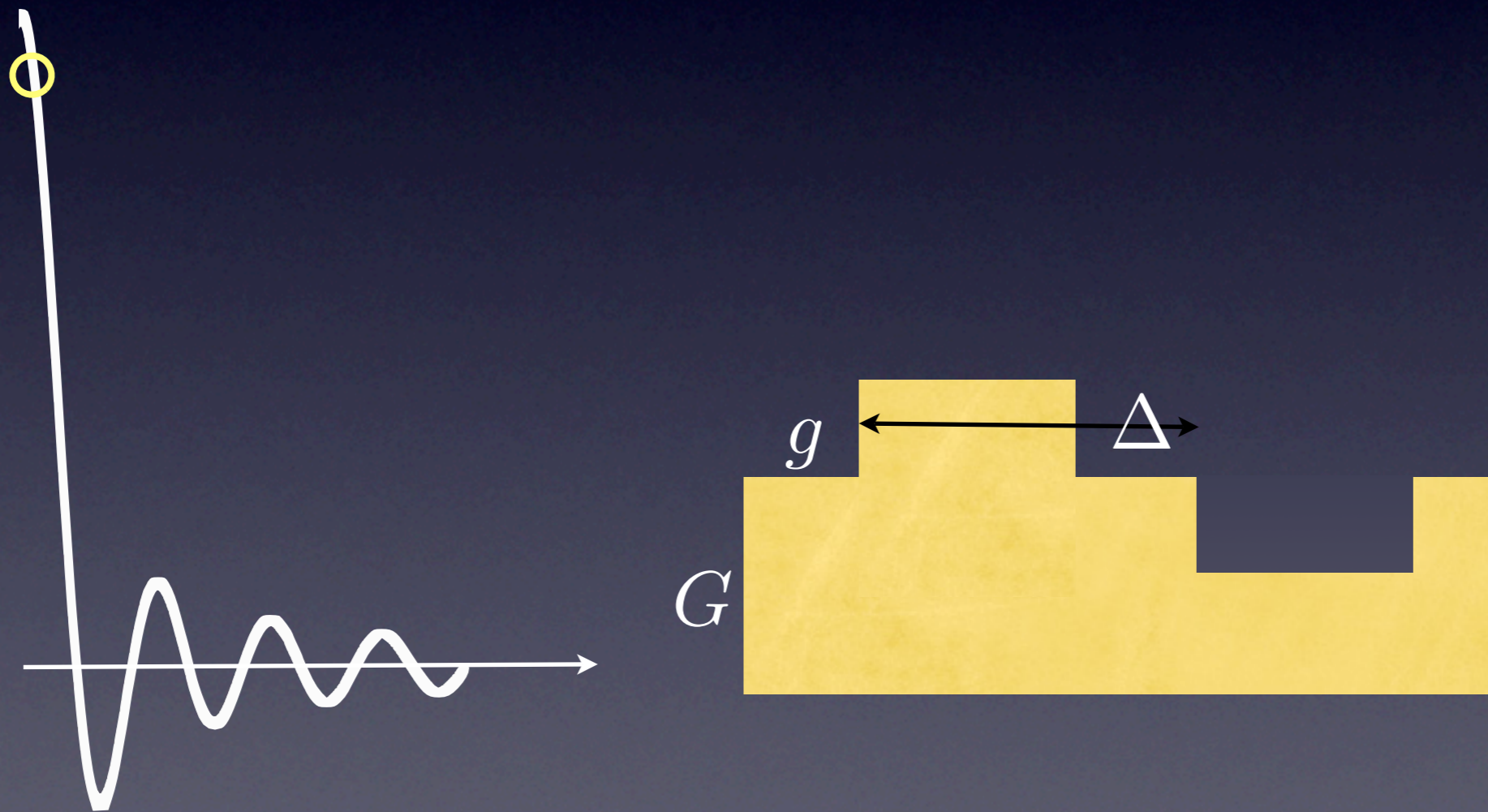
These two are the same...



...unless there is motion during Δ .

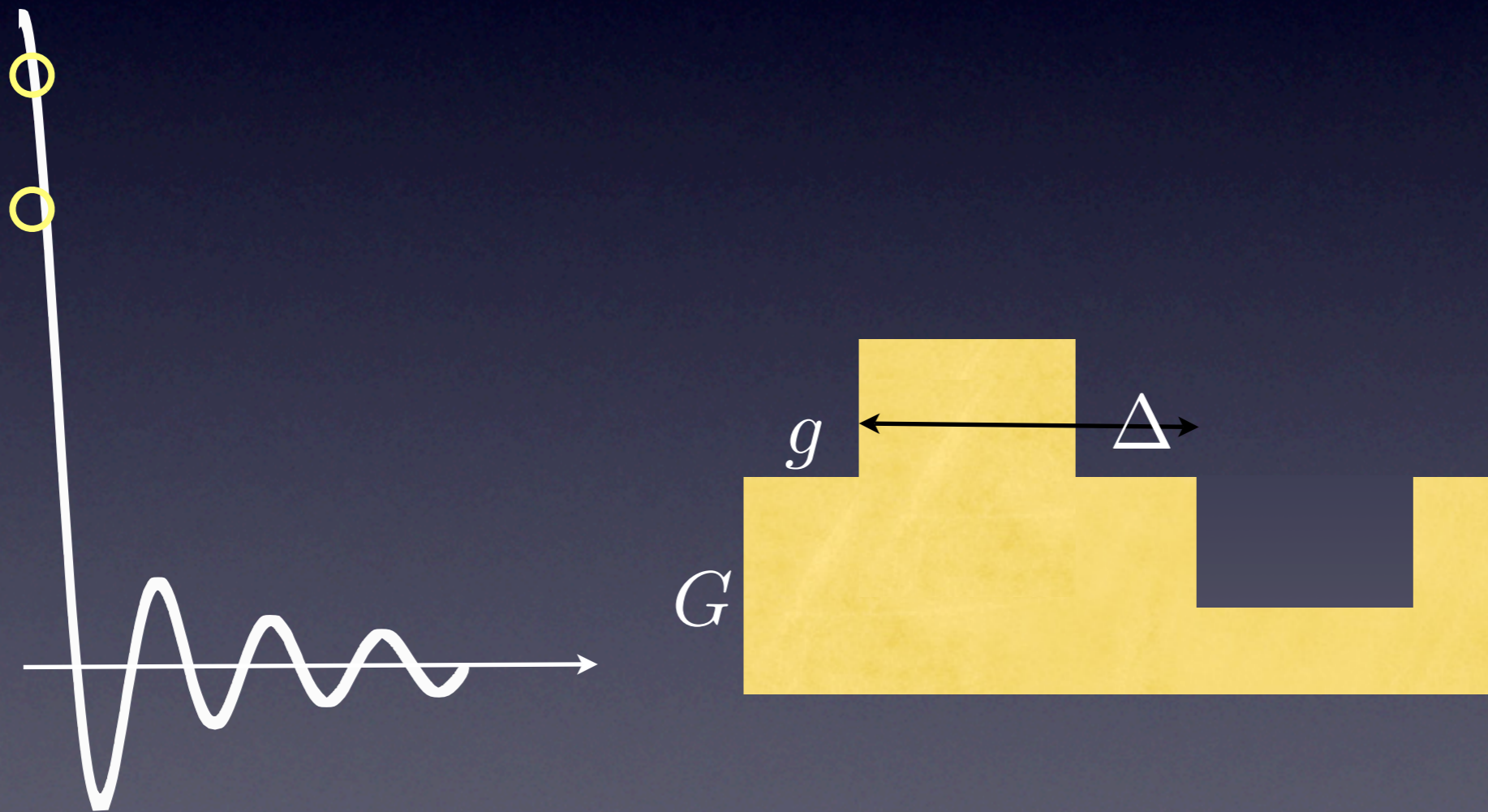
Motion sensitisation

Increasing the step increases sensitivity to displacement.
We can Fourier transform along this dimension too.



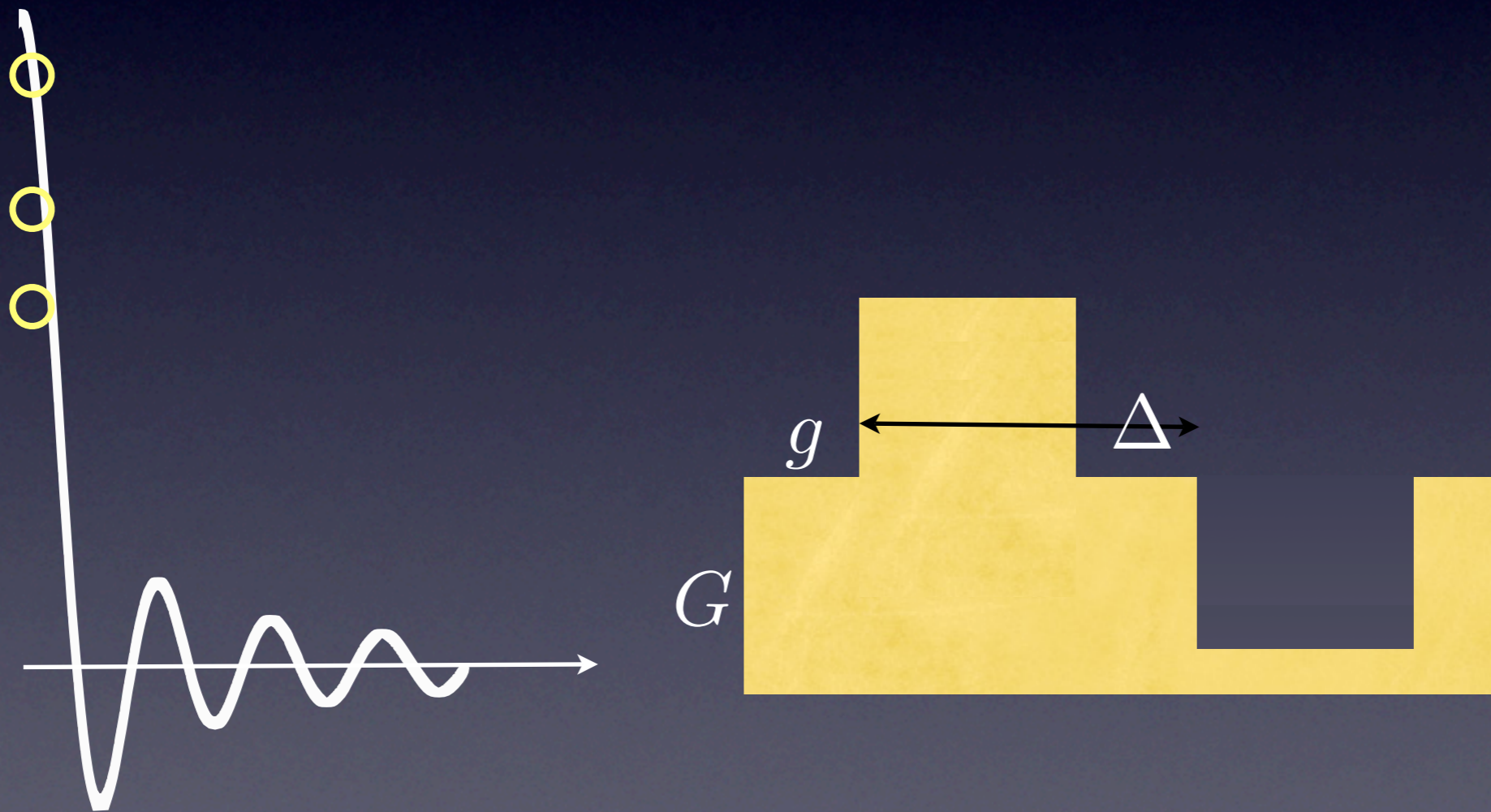
Motion sensitisation

Increasing the step increases sensitivity to displacement.
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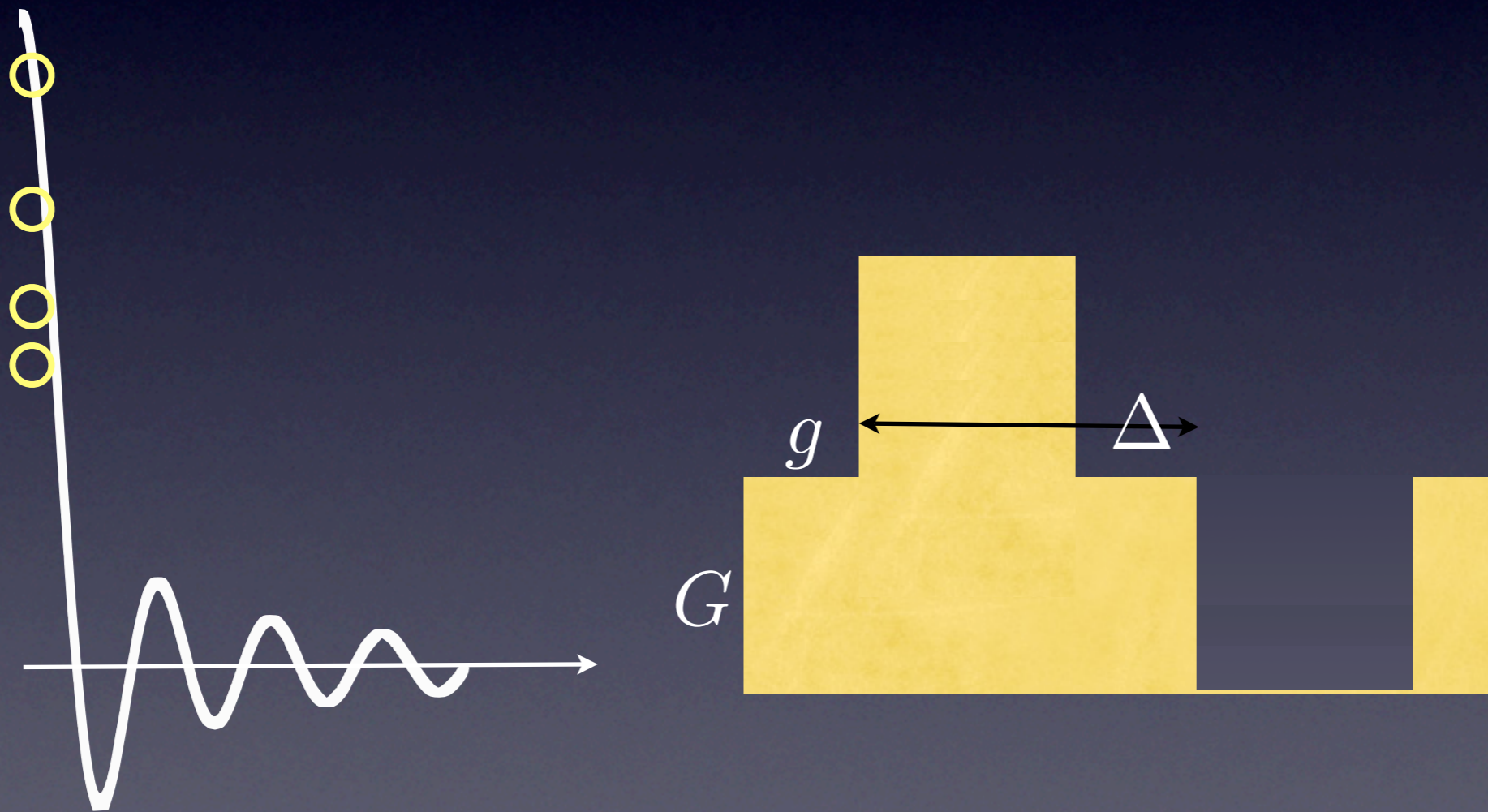
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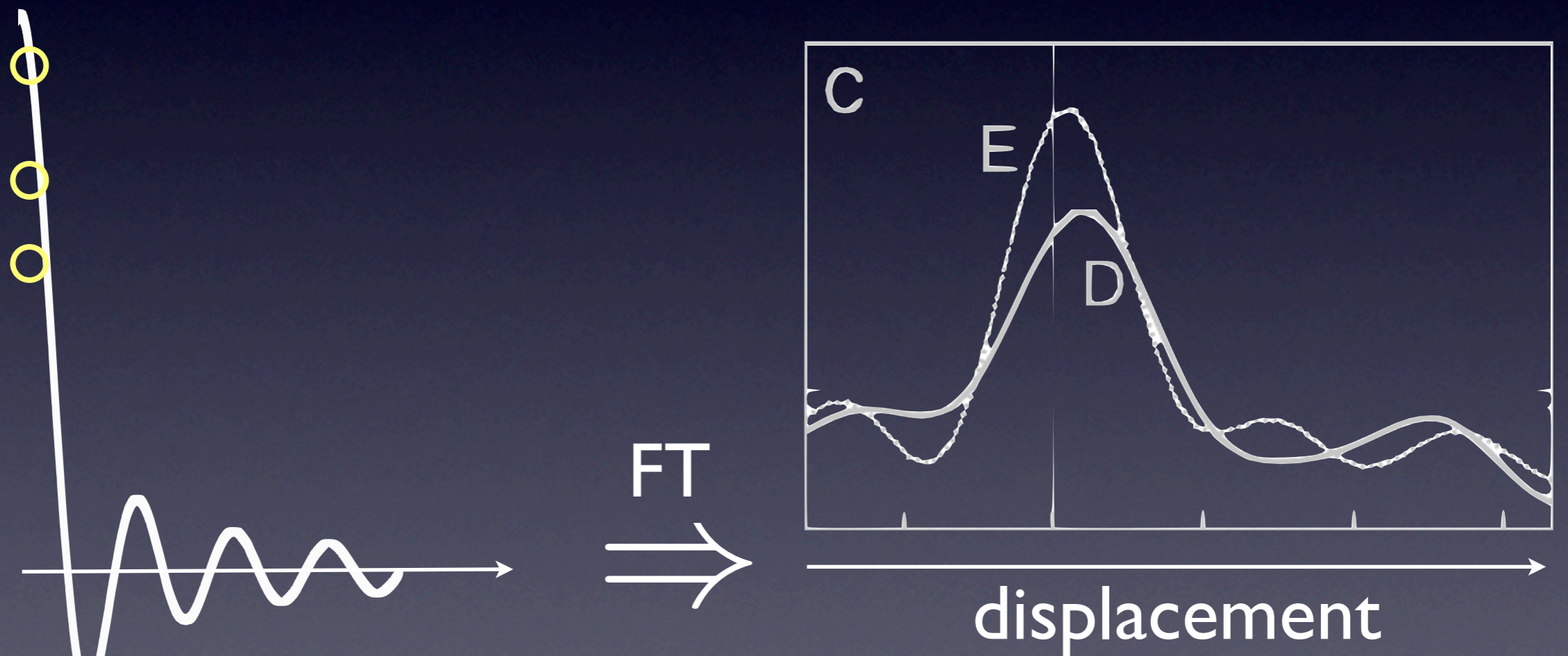
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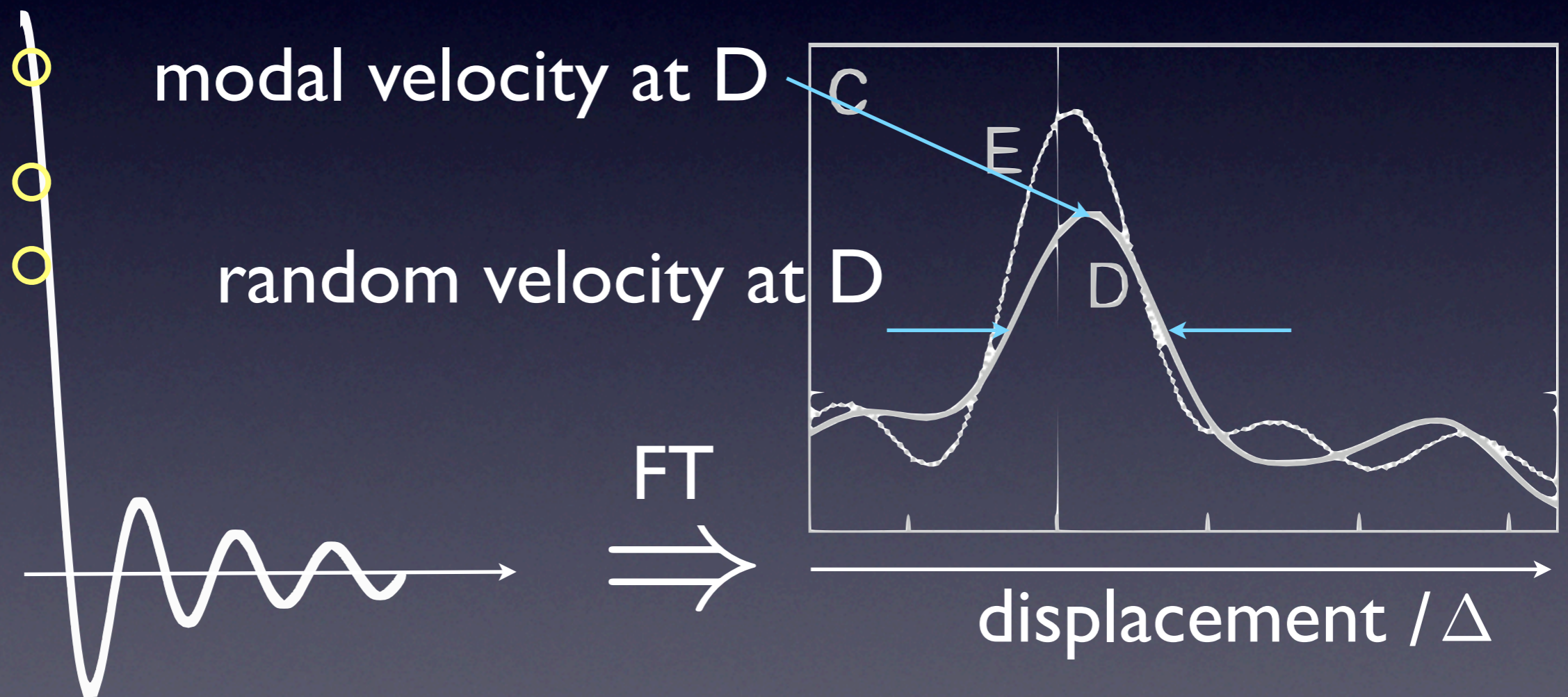
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... giving an average propagator at every position.

Motion sensitisation

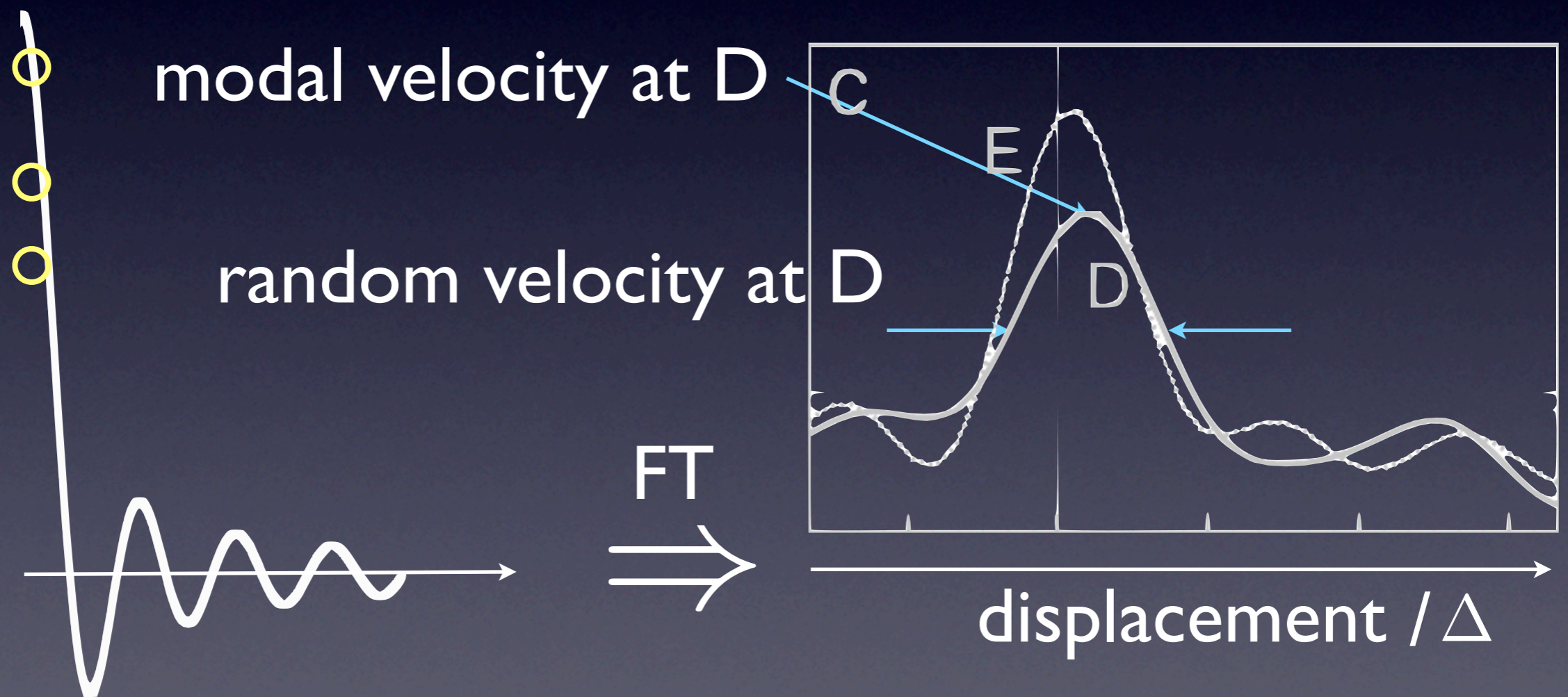
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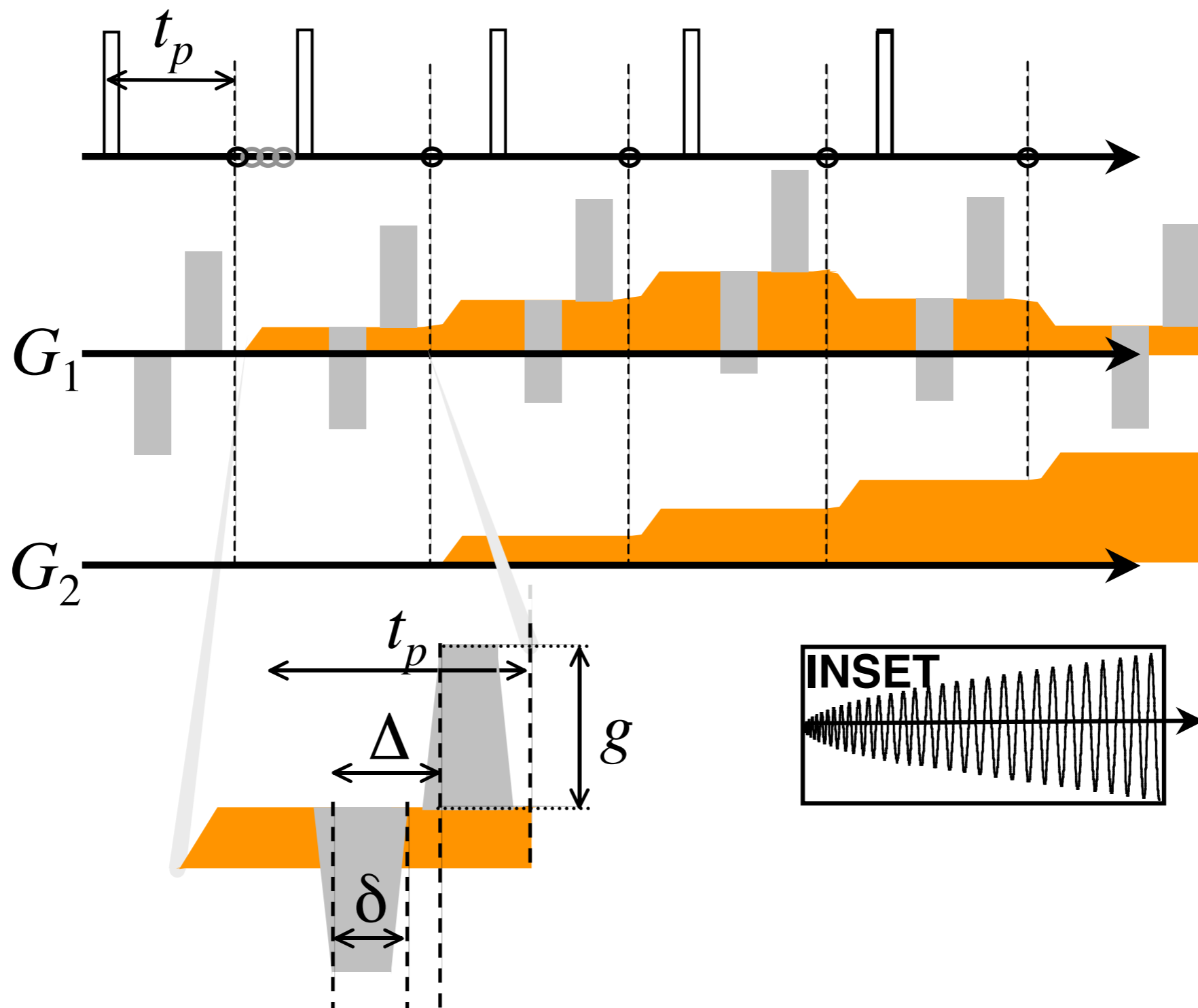
... giving an average propagator at every position.

Motion sensitisation

Random displacements could be due to turbulence or diffusion or mechanical dispersion or cavitation.



Motion sensitisation



Motion sensitisation

Recall that these data take several tens of minutes to acquire in total.

The measurements are highly time-averaged.

Motion sensitisation

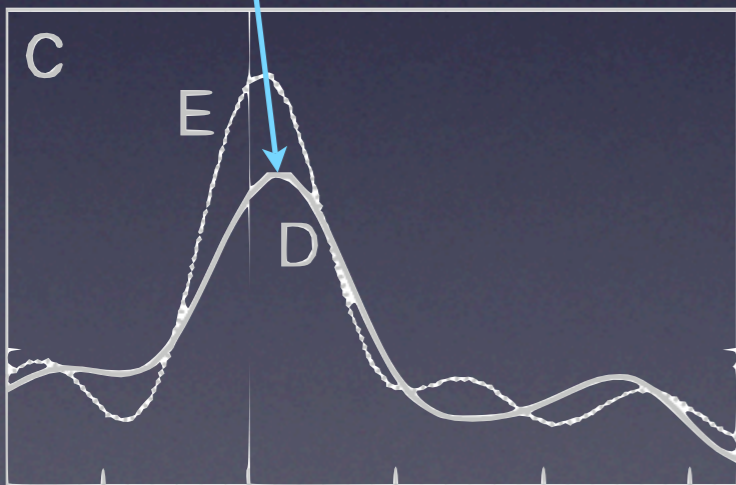
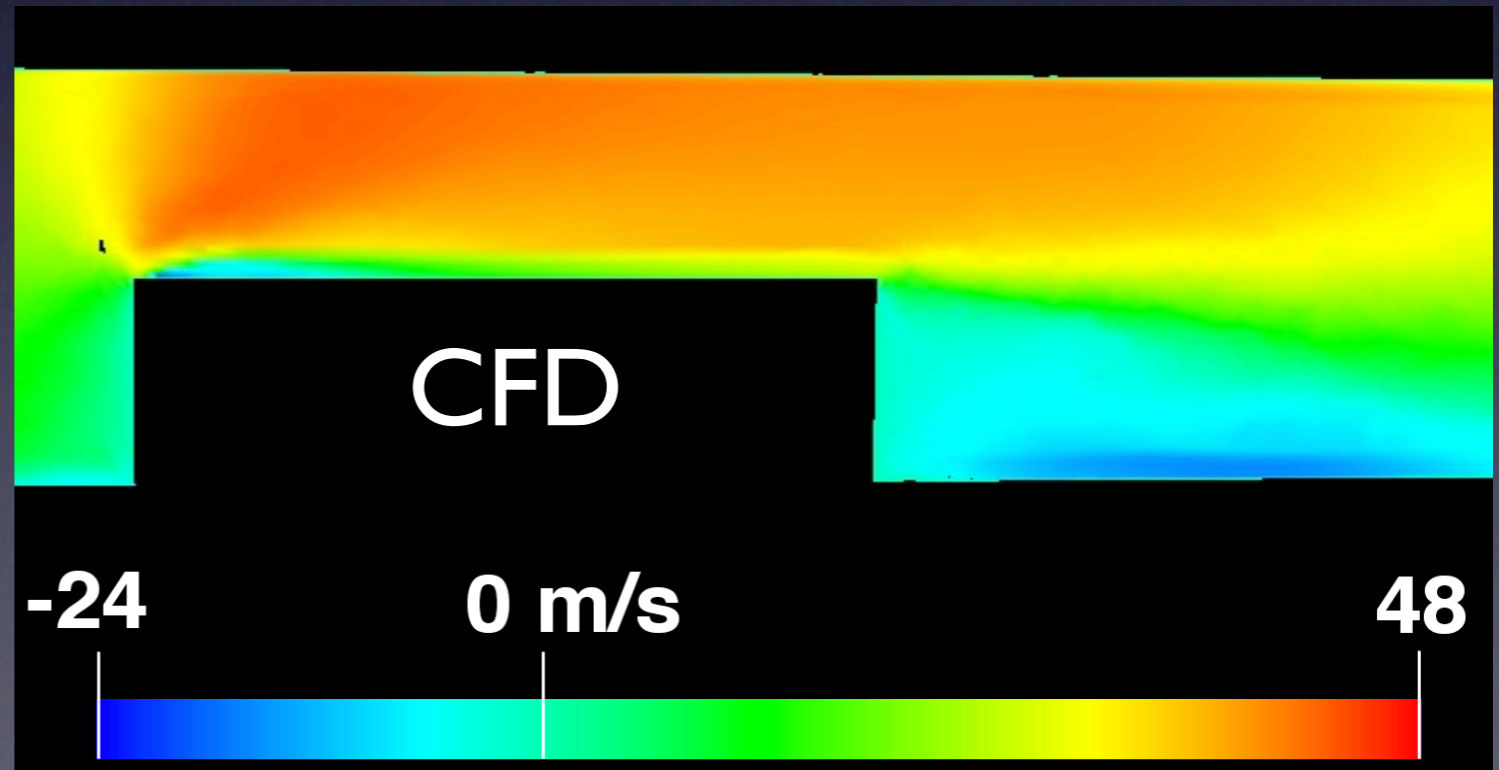
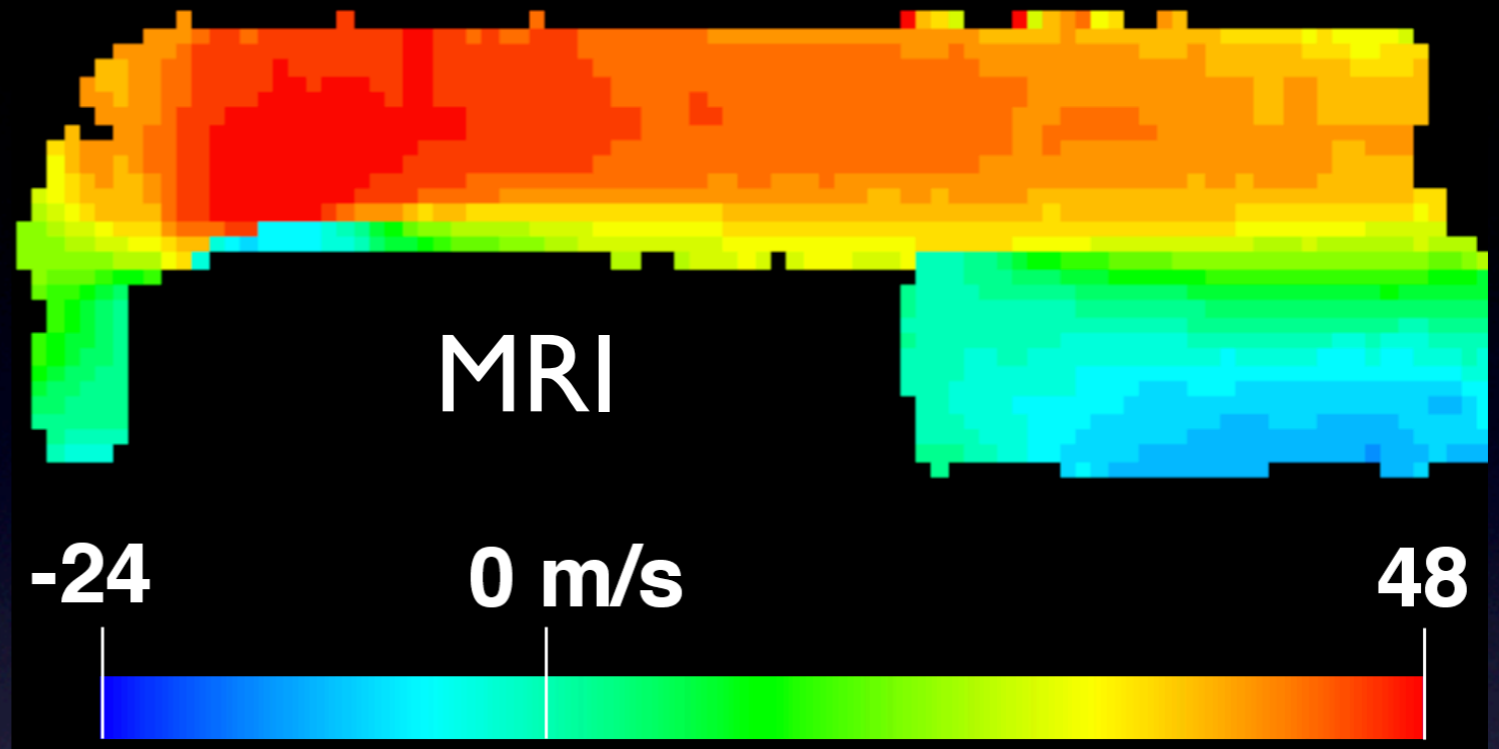
Recall that these data take several tens of minutes to acquire in total.

The measurements are highly time-averaged.

So all the statistics are done for you.

Subsonic gas

From the average propagator, we pick a modal velocity.



Subsonic gas

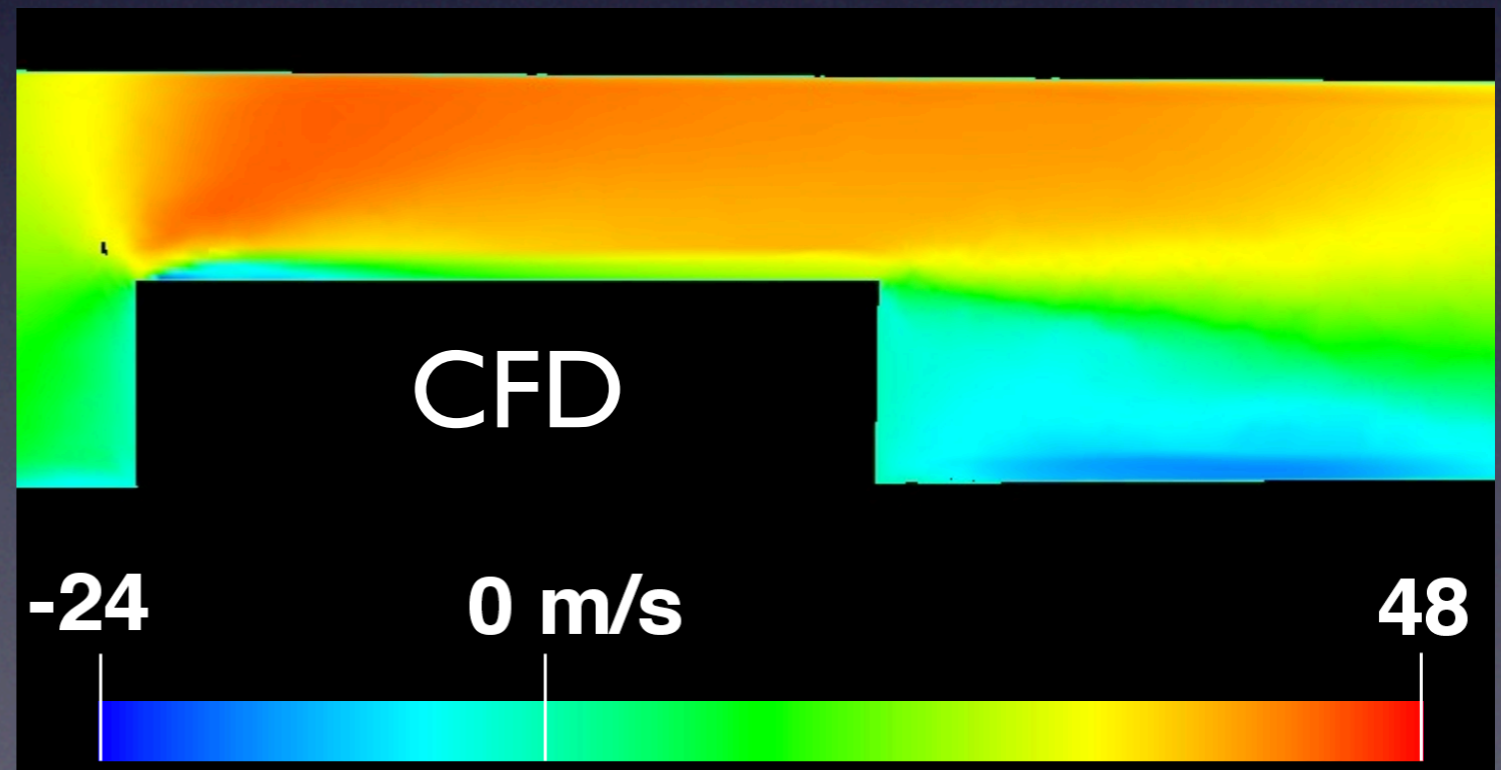
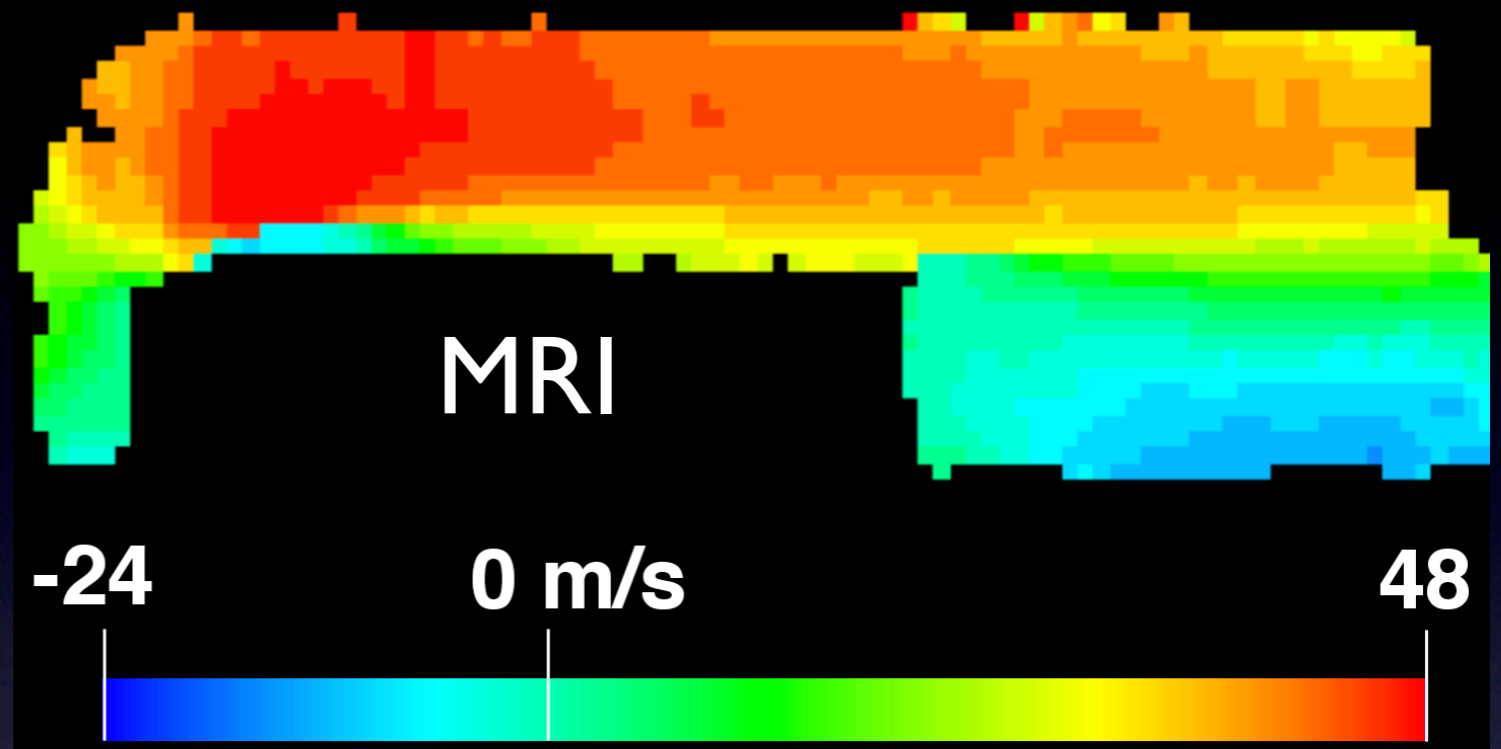
Flow of SF₆ gas

Mach 0.12

Re = 210,000

Modal velocities

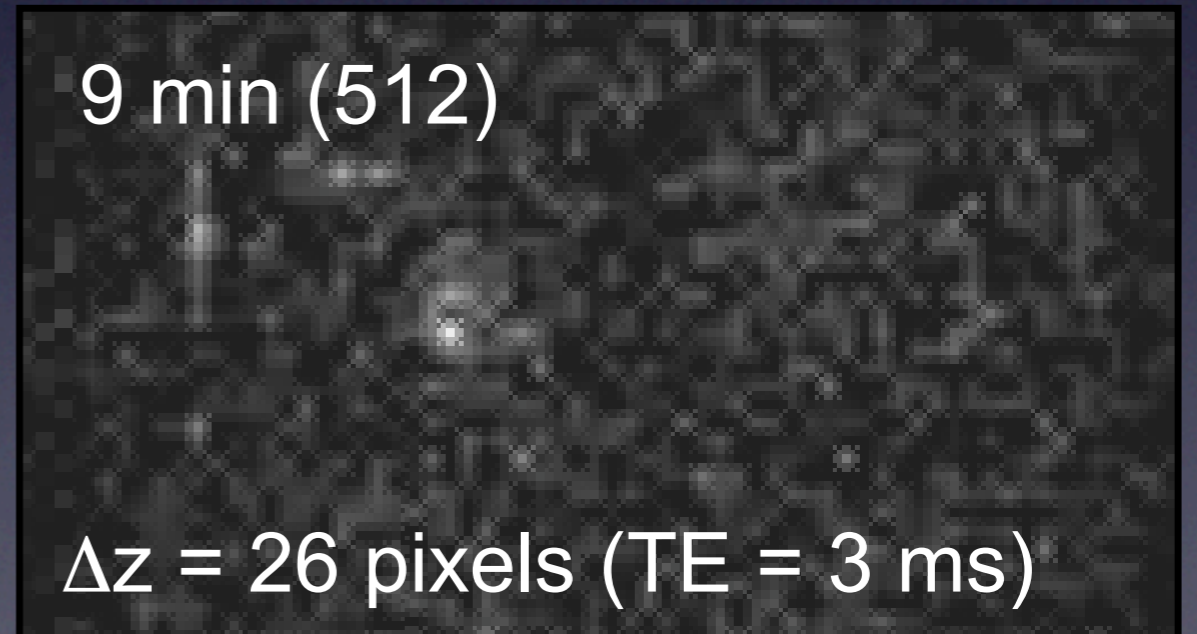
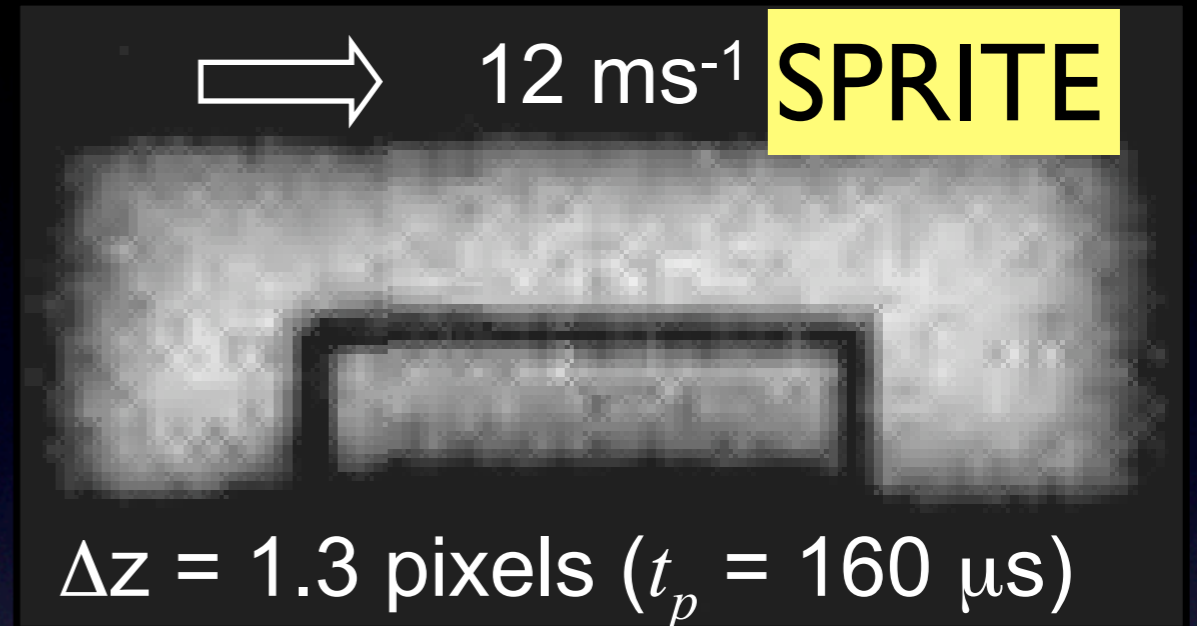
Only SPRITE could do this (among MRI).



Subsonic gas

Flow faster than c. 1 m/s

... can lead to complete signal loss in conventional MRI
... the gas leaves the probe during the measurement.

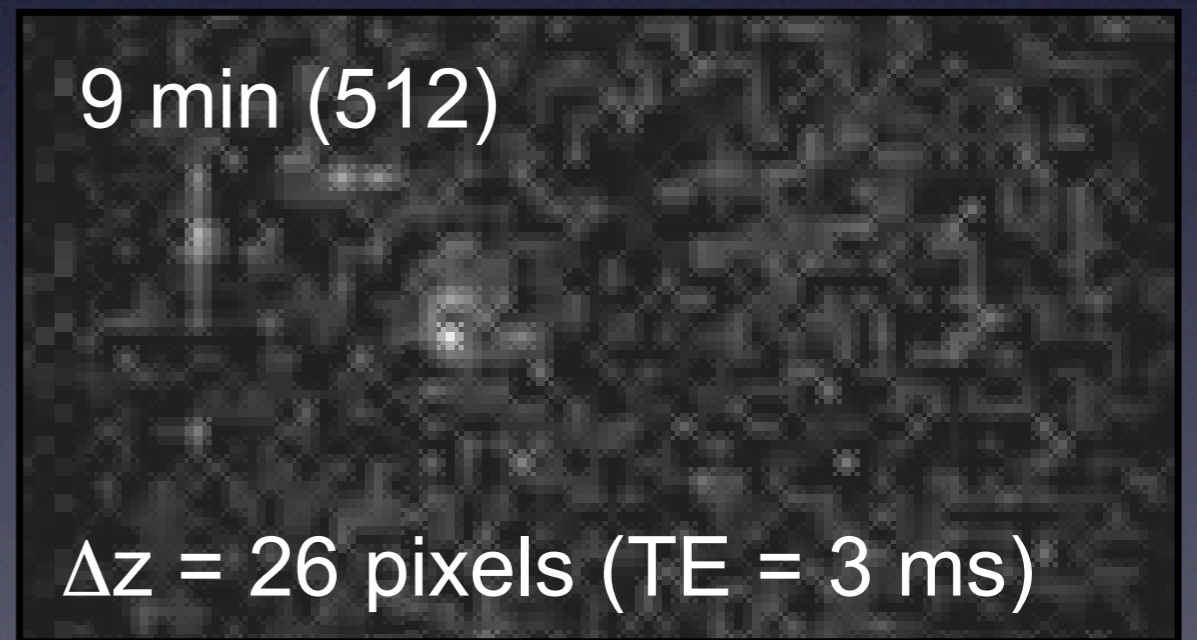
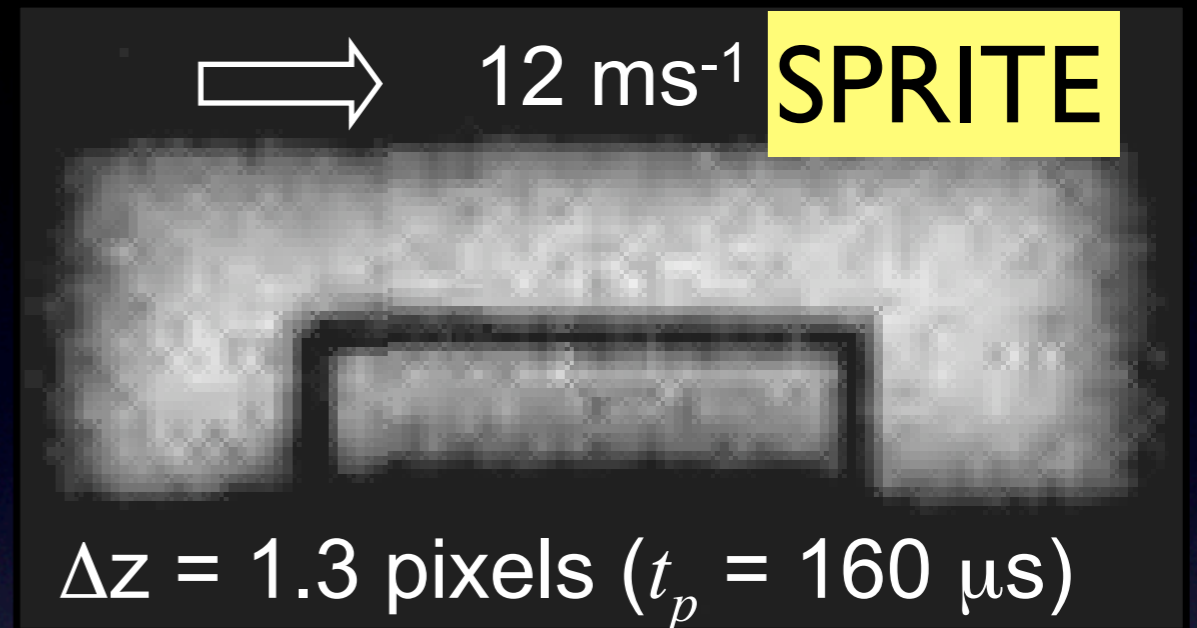


Subsonic gas

Random fluctuations in displacement also lead to extreme signal attenuation in conventional MRI.

In SPRITE MRI, short t_p controls the signal loss.

In fact, we measure the signal loss (width of propagator).



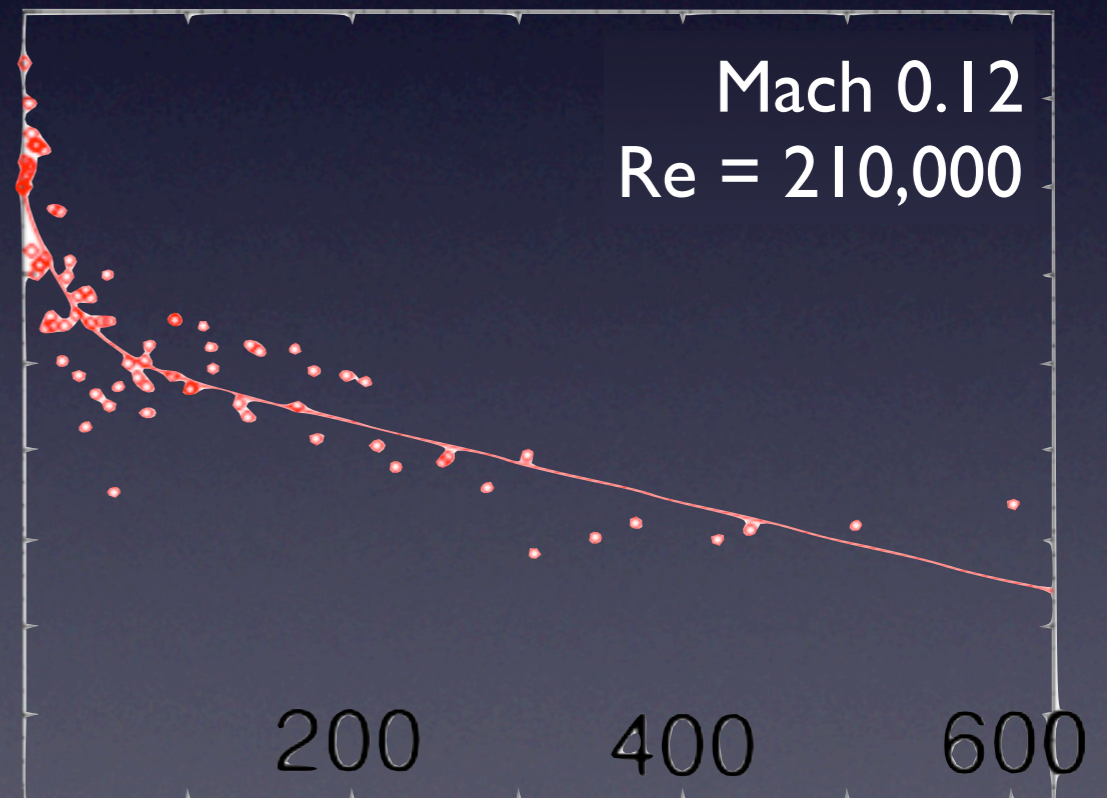
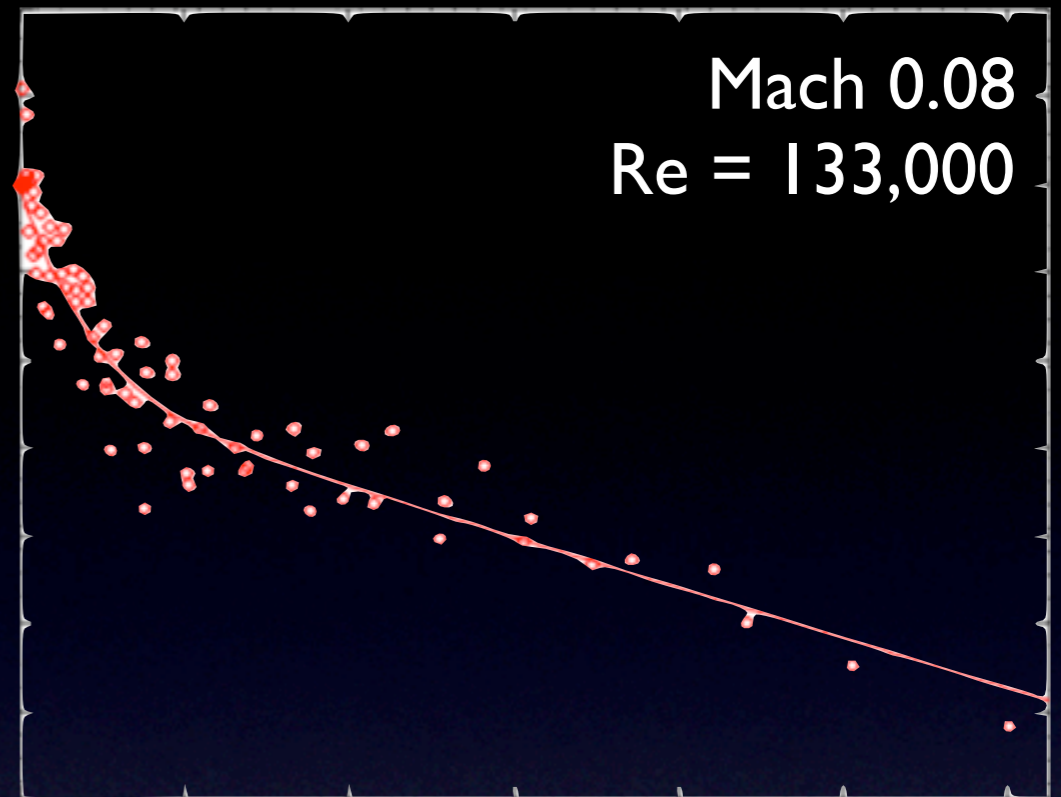
Subsonic gas

In fact, we measure the signal loss (width of average propagator).

Slope is proportional to width...

... which we associate with [two] turbulent eddy diffusivity coefficients.

$$\ln \frac{s(g)/ss(g)}{s(0)/ss(0)}$$



$$\gamma^2 g^2 \frac{1}{2} t_p^3$$

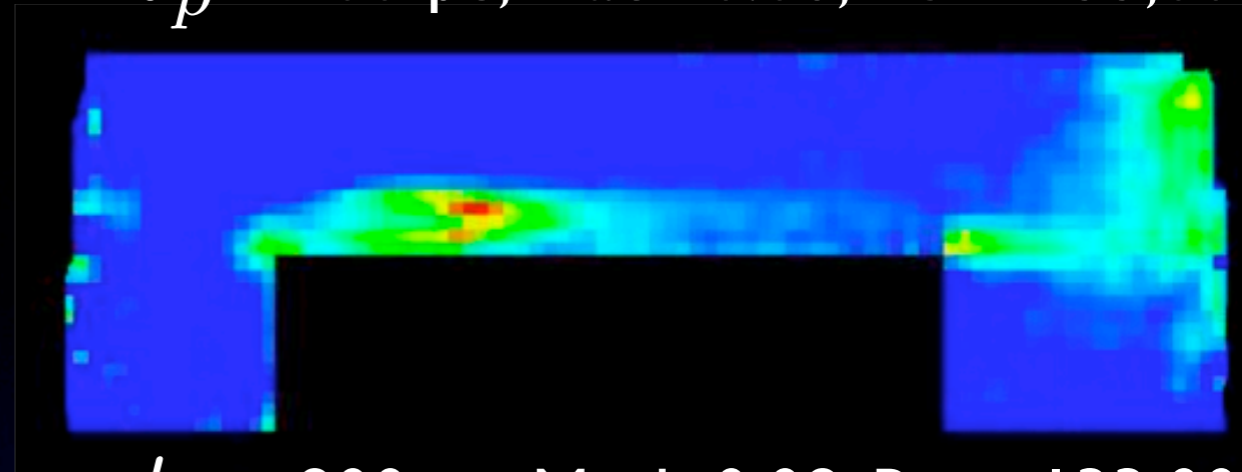
Subsonic gas

We can map D_t
because it is constant
with t_p

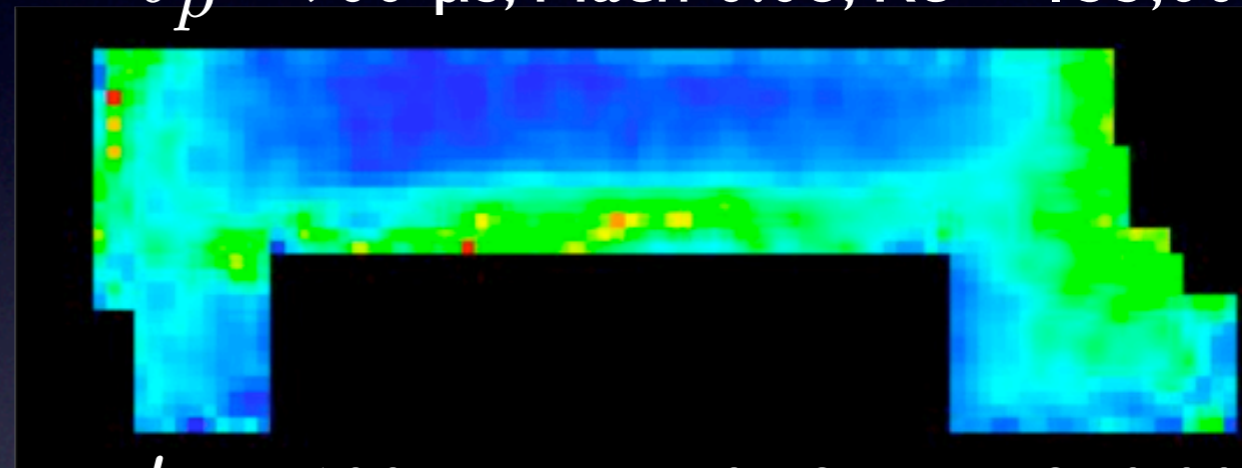


0 60 / m²/s²

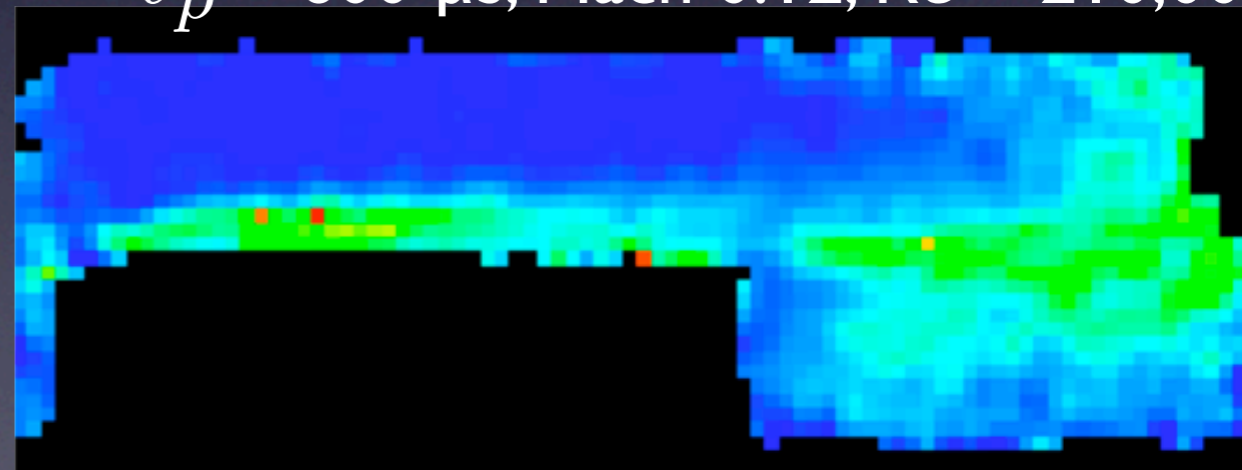
$t_p = 400 \mu\text{s}$, Mach 0.08, Re = 133,000



$t_p = 900 \mu\text{s}$, Mach 0.08, Re = 133,000



$t_p = 600 \mu\text{s}$, Mach 0.12, Re = 210,000

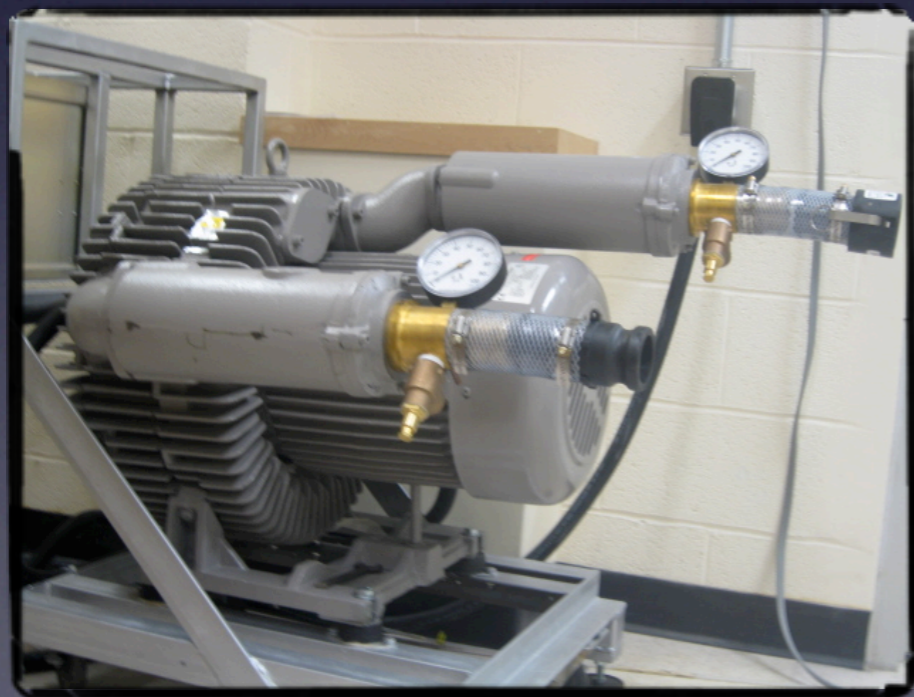


0 0.020 / m²/s

Slightly-less-subsonic gas

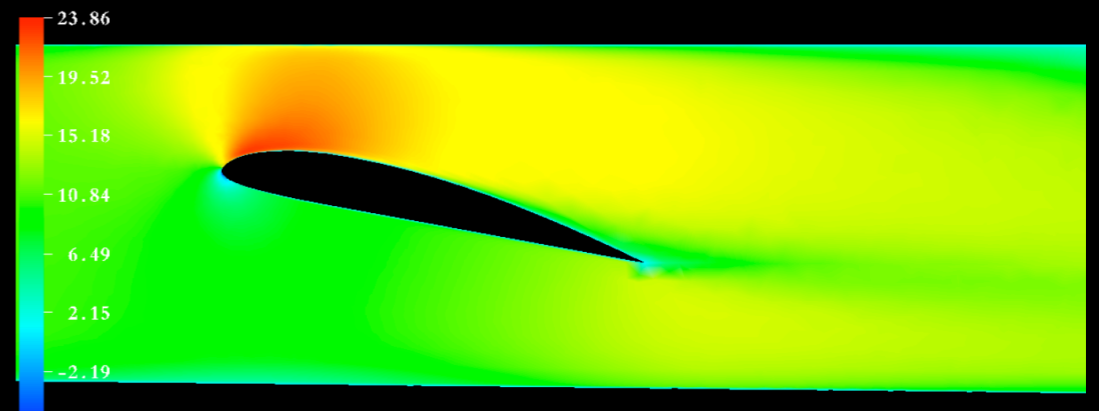
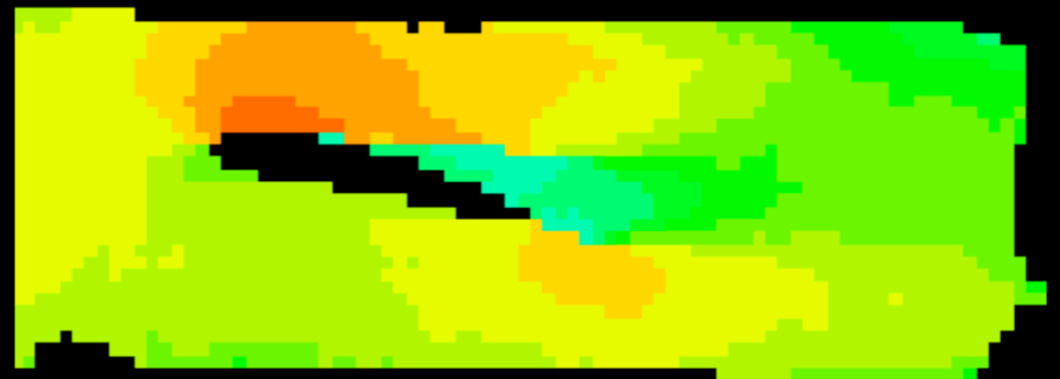
This arrangement can be used as an MRI wind tunnel.

Current developments are towards Mach 1



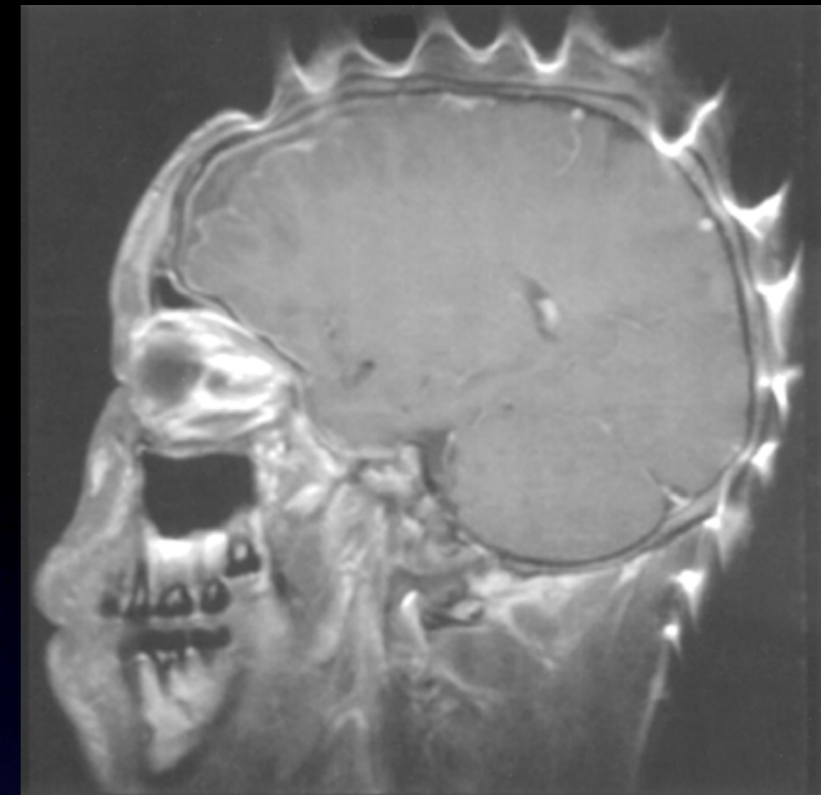
Newling et al. *Phys Rev. Lett.* (2004) **93** 154504

12 m/s **Re** 165 000 SF₆

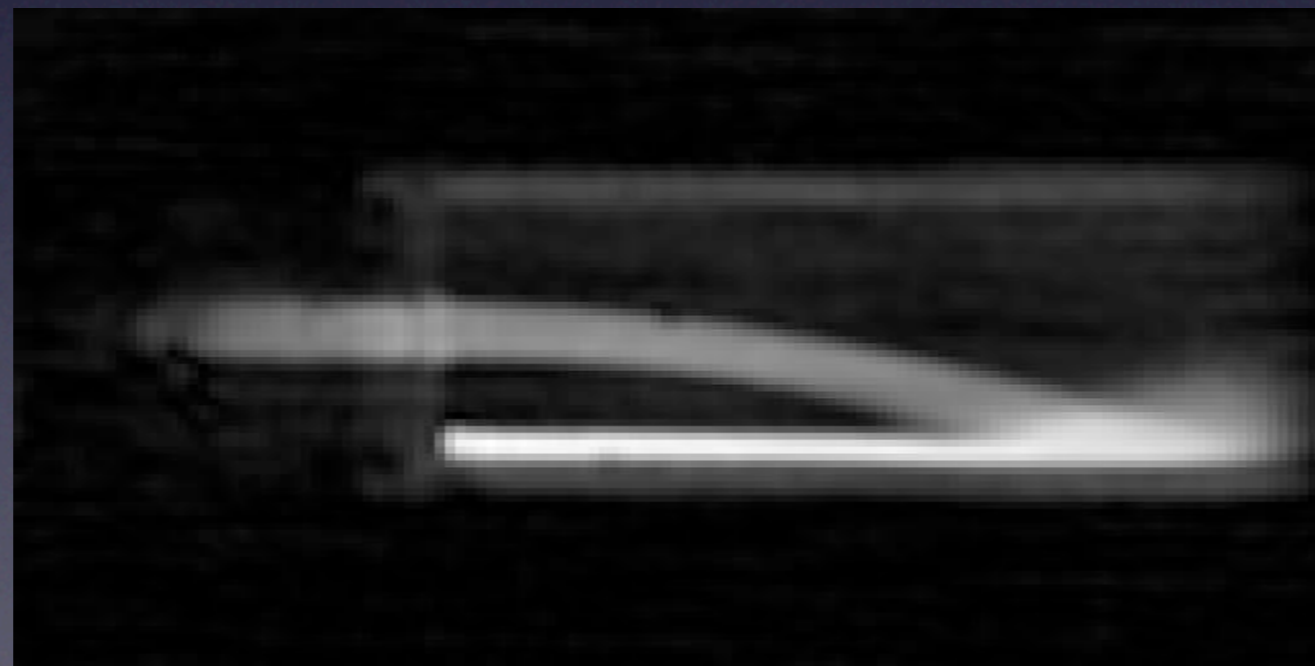


Two-phase flow

Another place where traditional MRI would not cope well...



... at the interface of air and water χ changes (artefacts)



Two phase flow

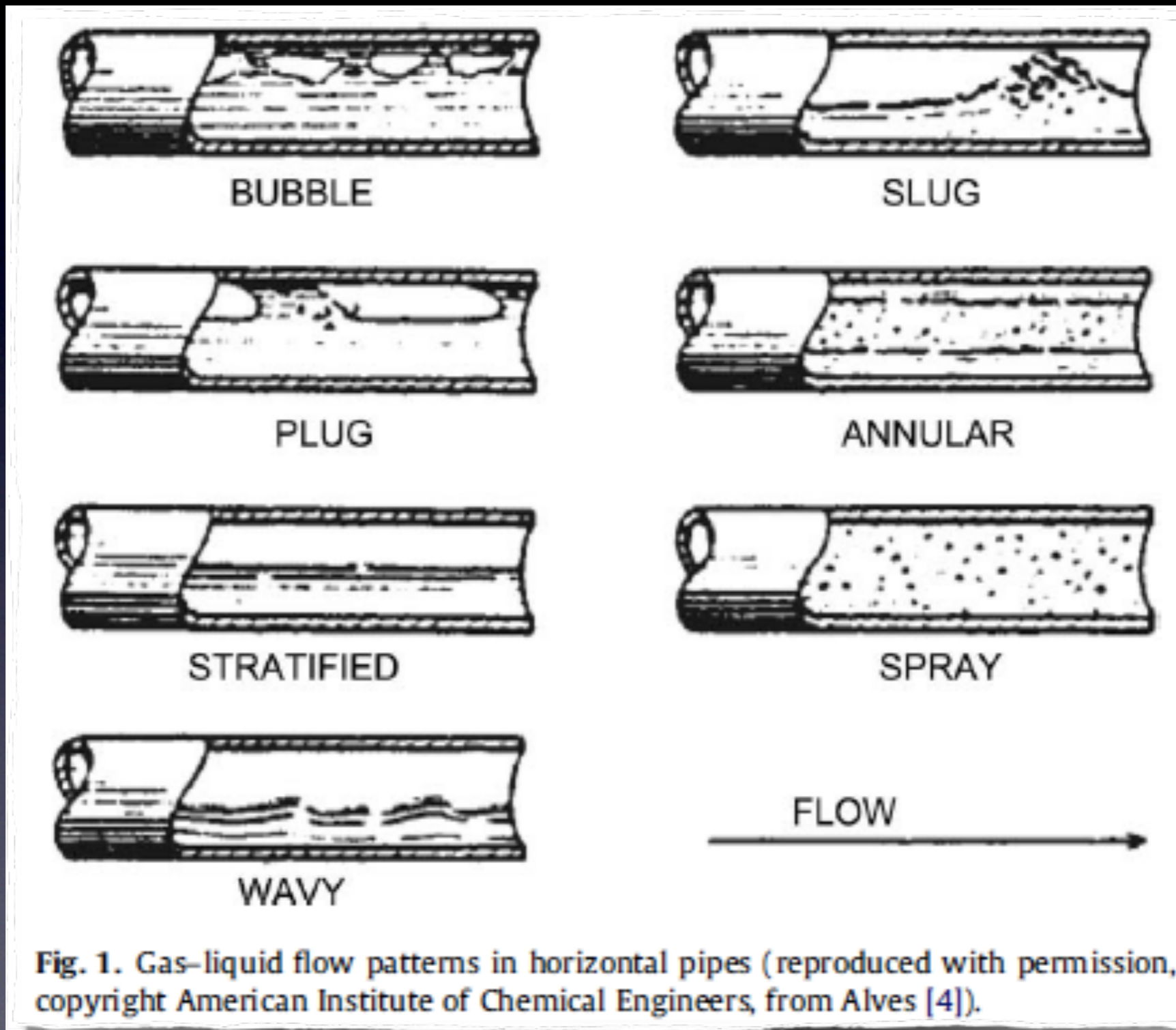
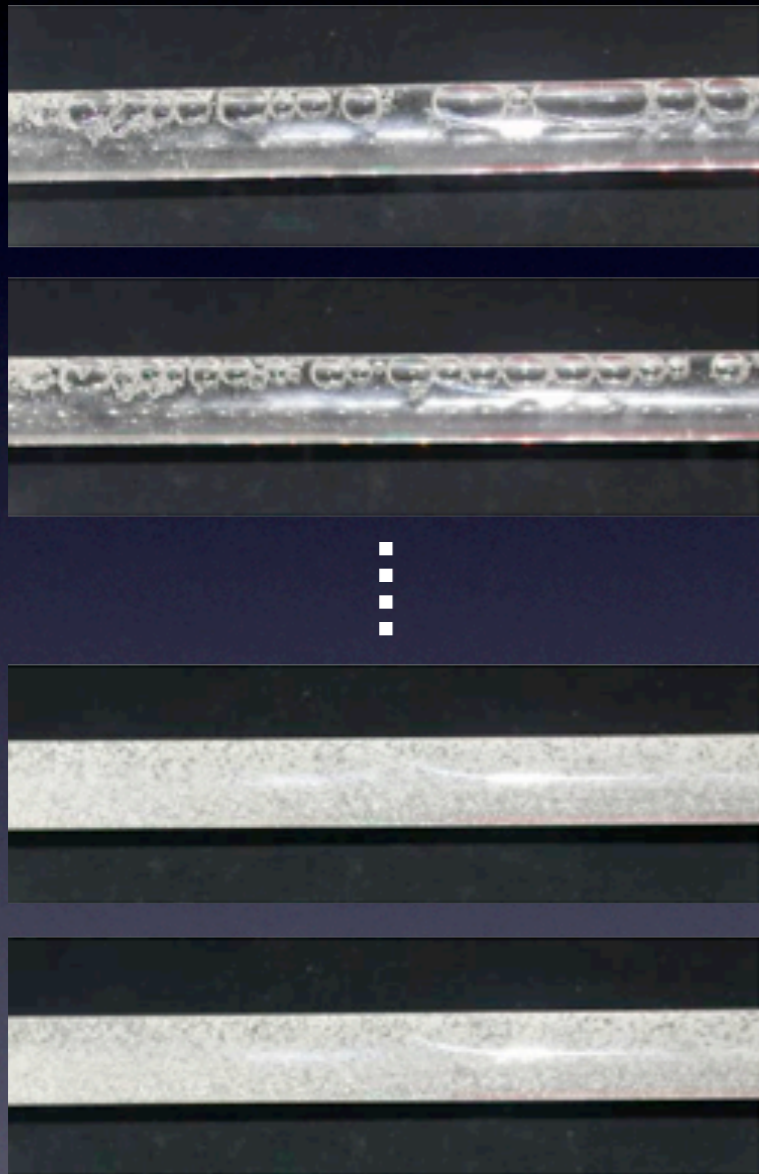
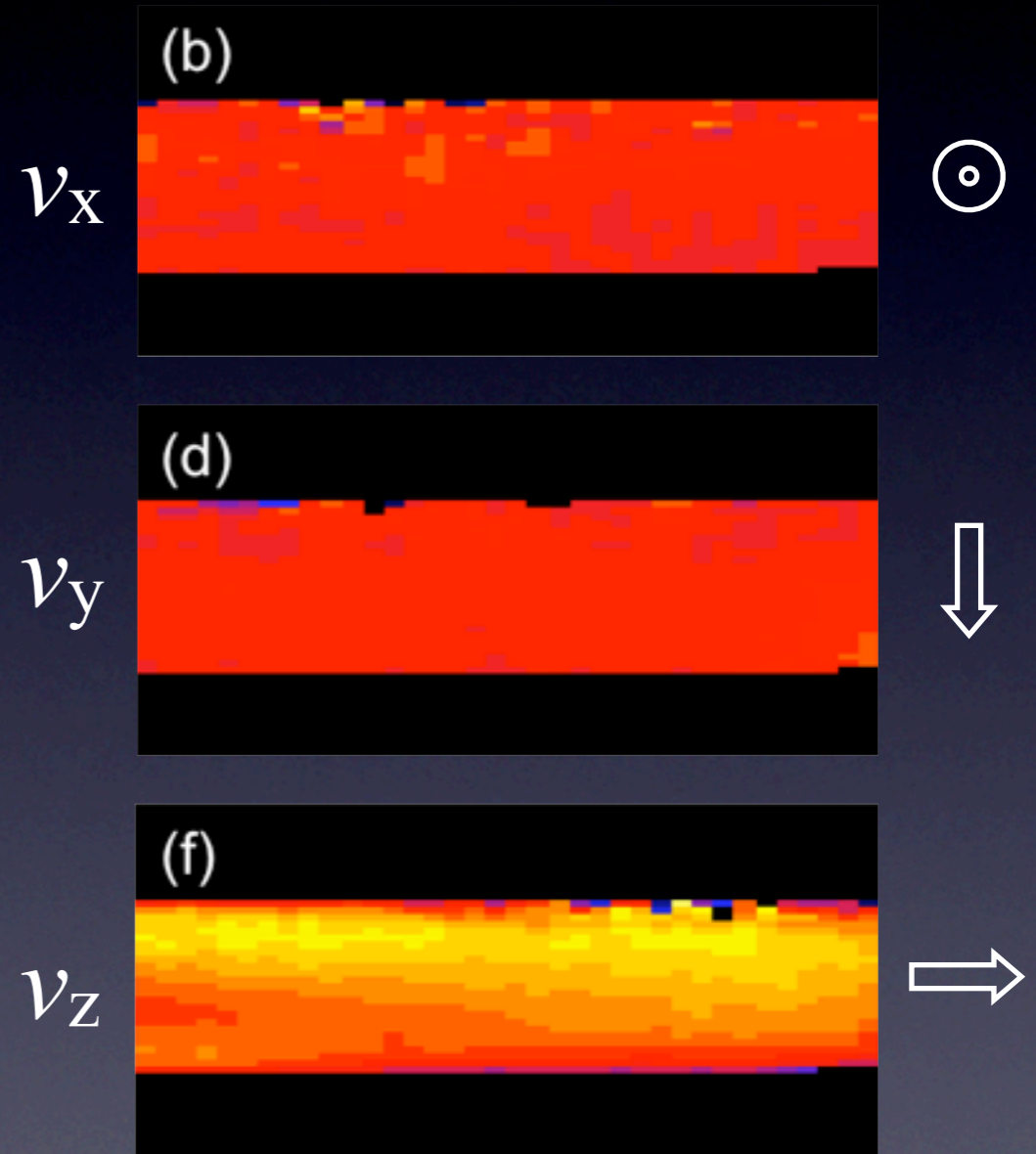
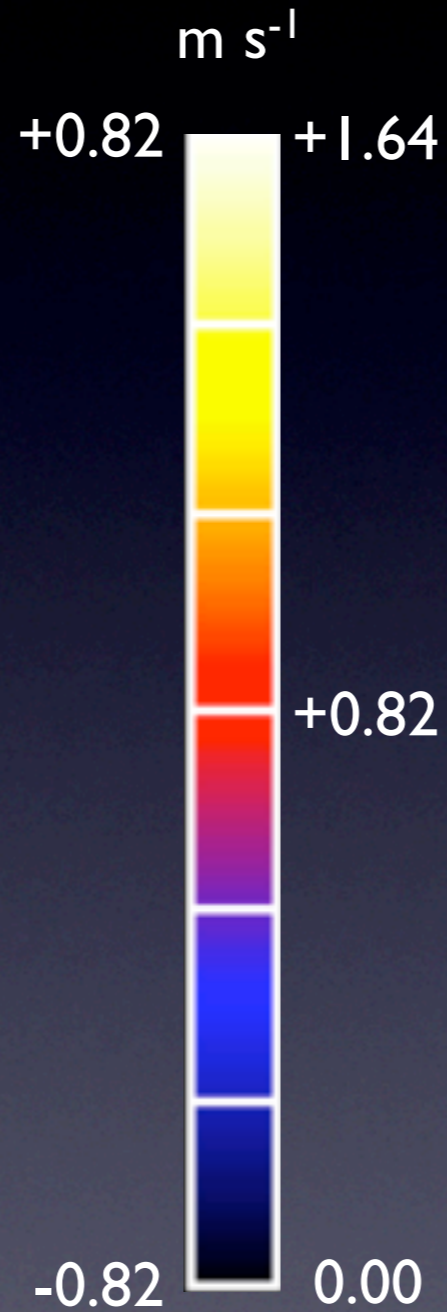


Fig. 1. Gas-liquid flow patterns in horizontal pipes (reproduced with permission, copyright American Institute of Chemical Engineers, from Alves [4]).

Two-phase flow



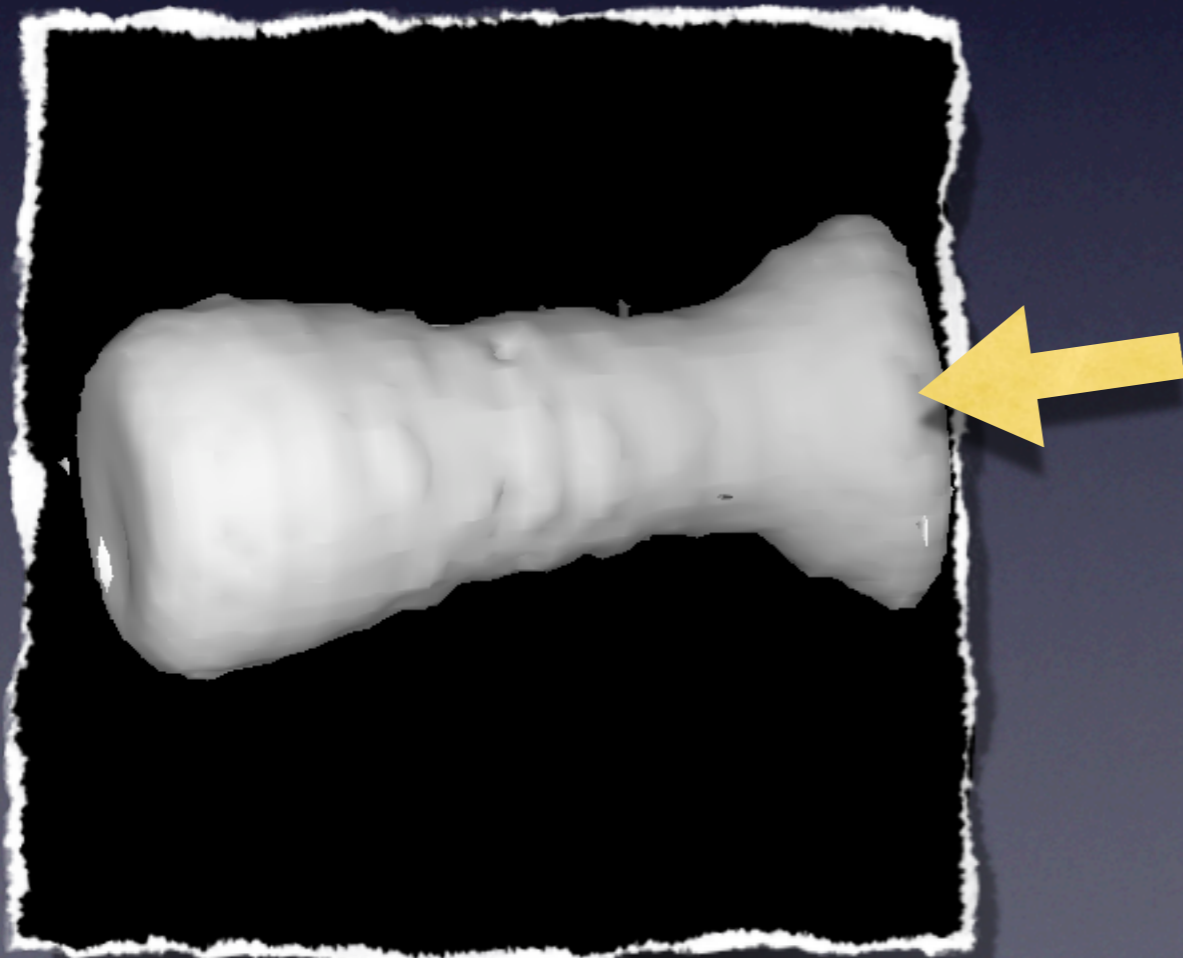
e.g. $t_p = 1.3$ ms



1 m/s **Re** 14 500 GdCl₃ (aq.)

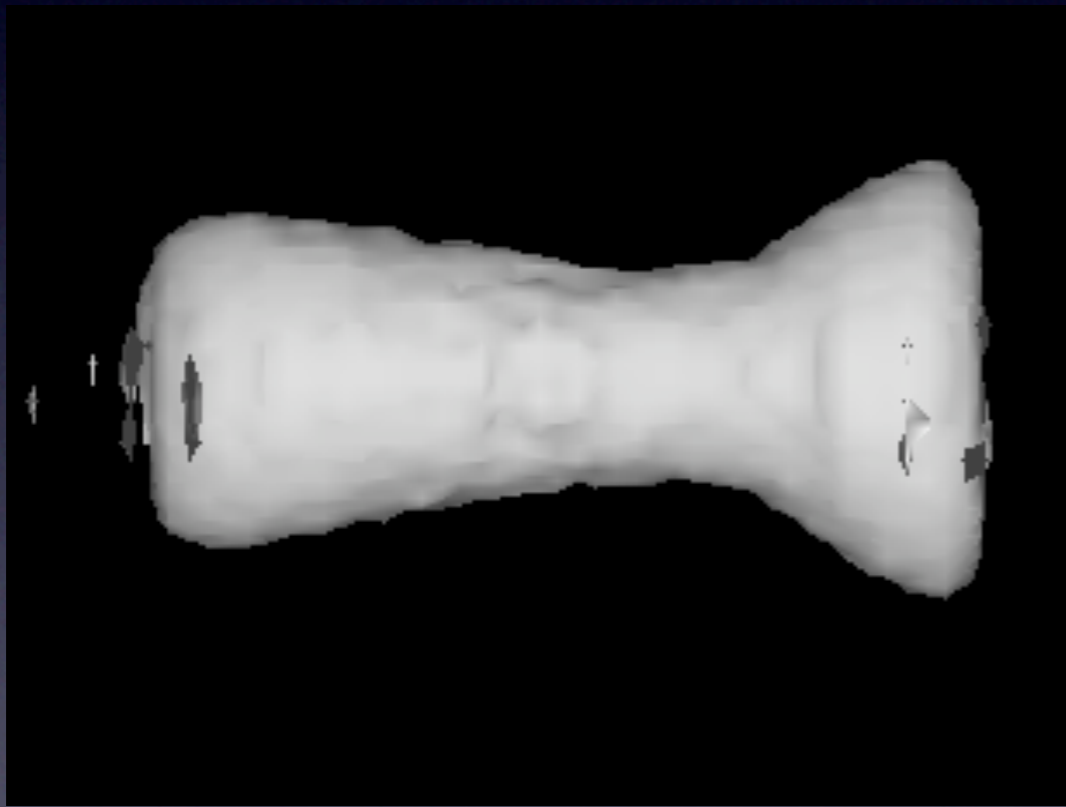
Two-phase flow

Latest measurements are in hydrodynamic cavitation: the formation of bubbles in a flow field.



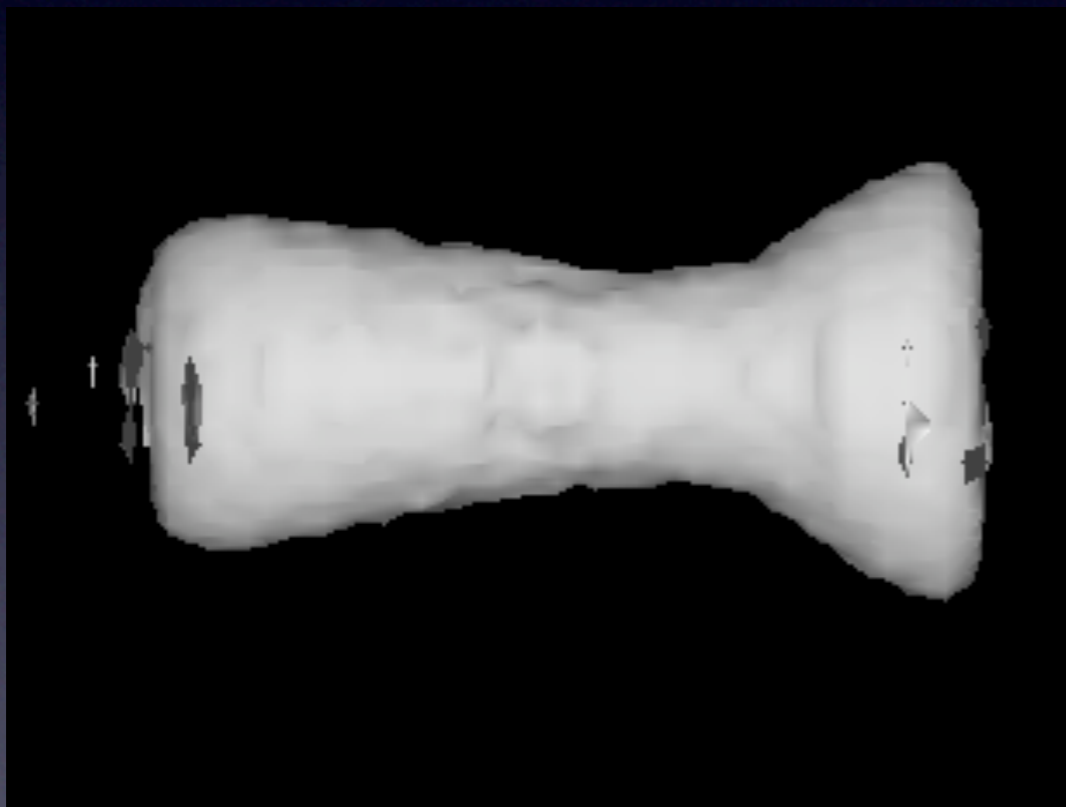
Hydrodynamic Cavitation

The formation of bubbles in a flow field.

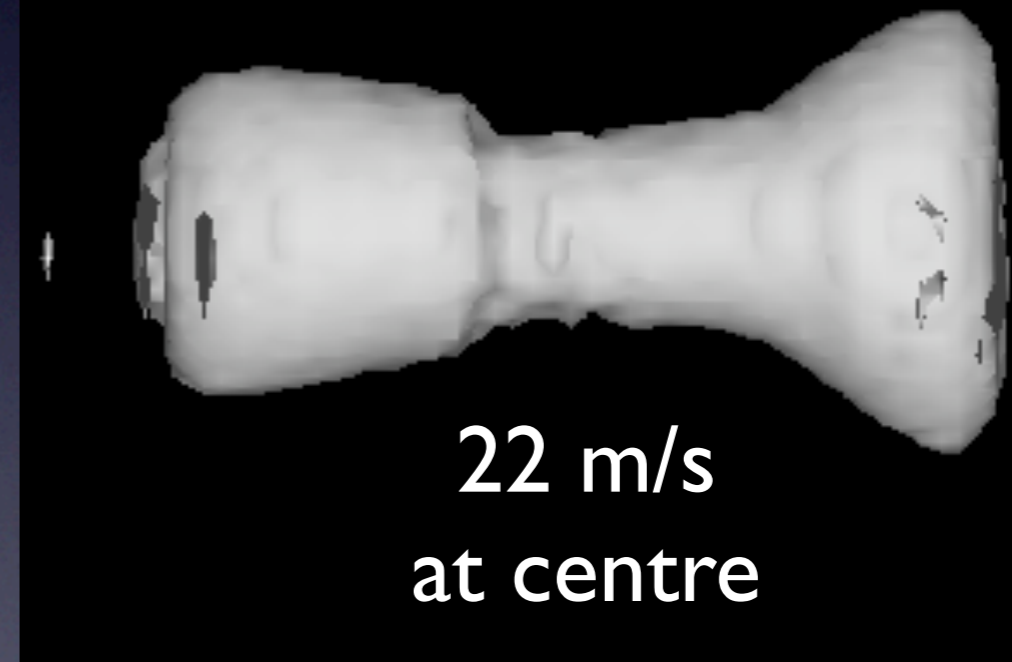


Hydrodynamic Cavitation

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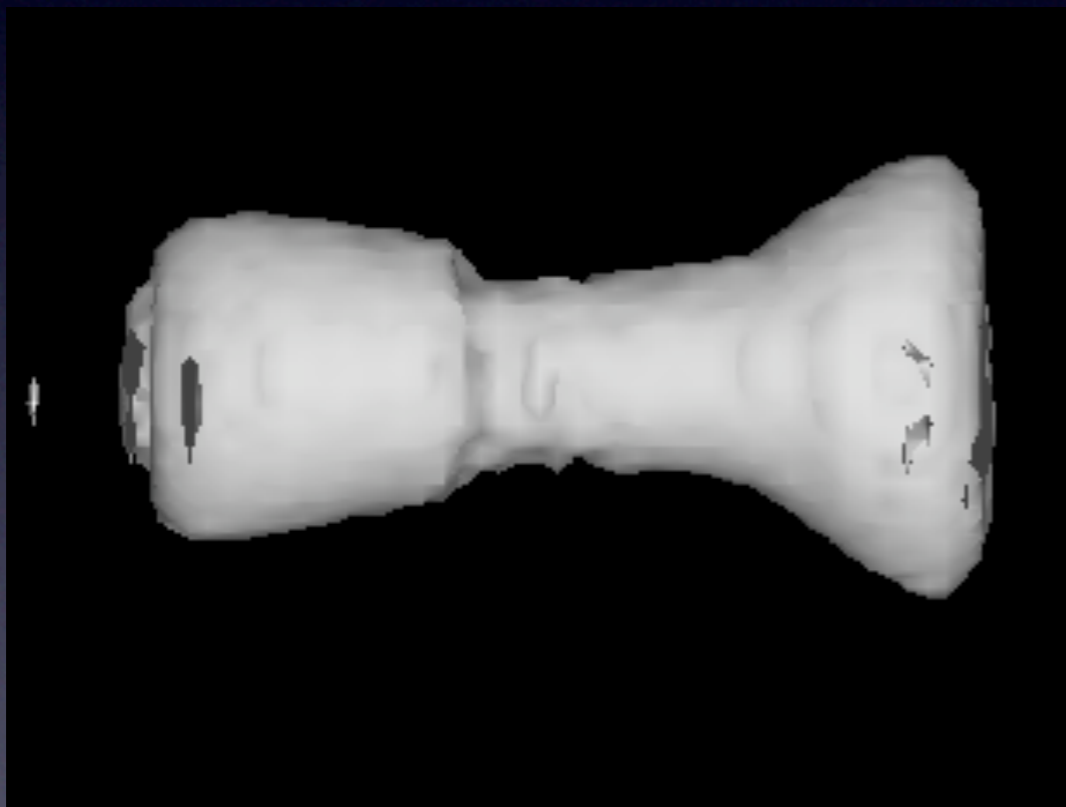


e.g. $t_p = 150 \mu\text{s}$

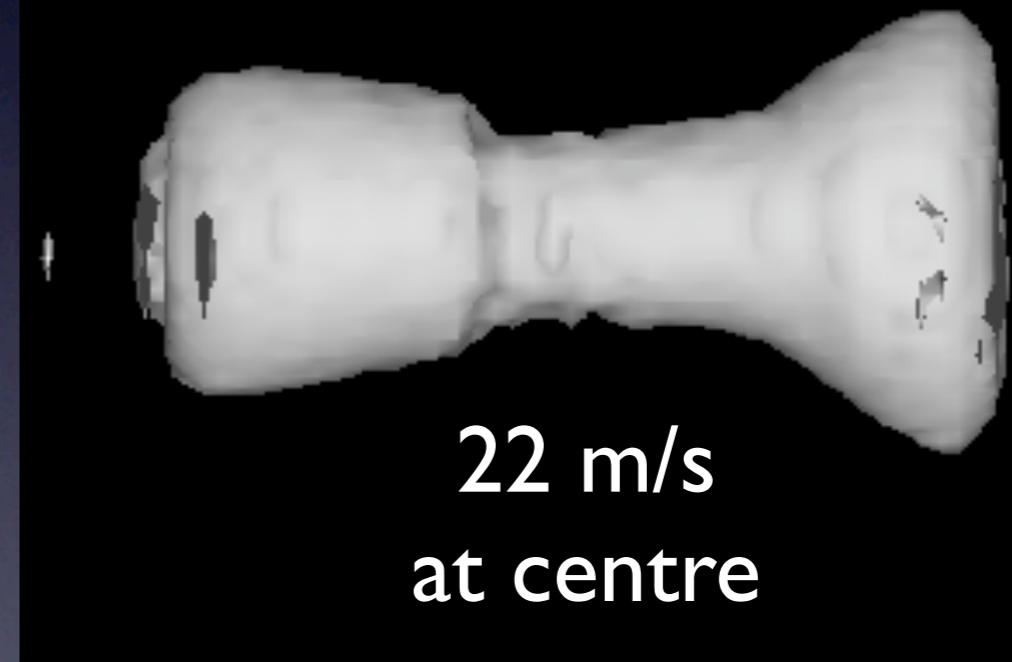


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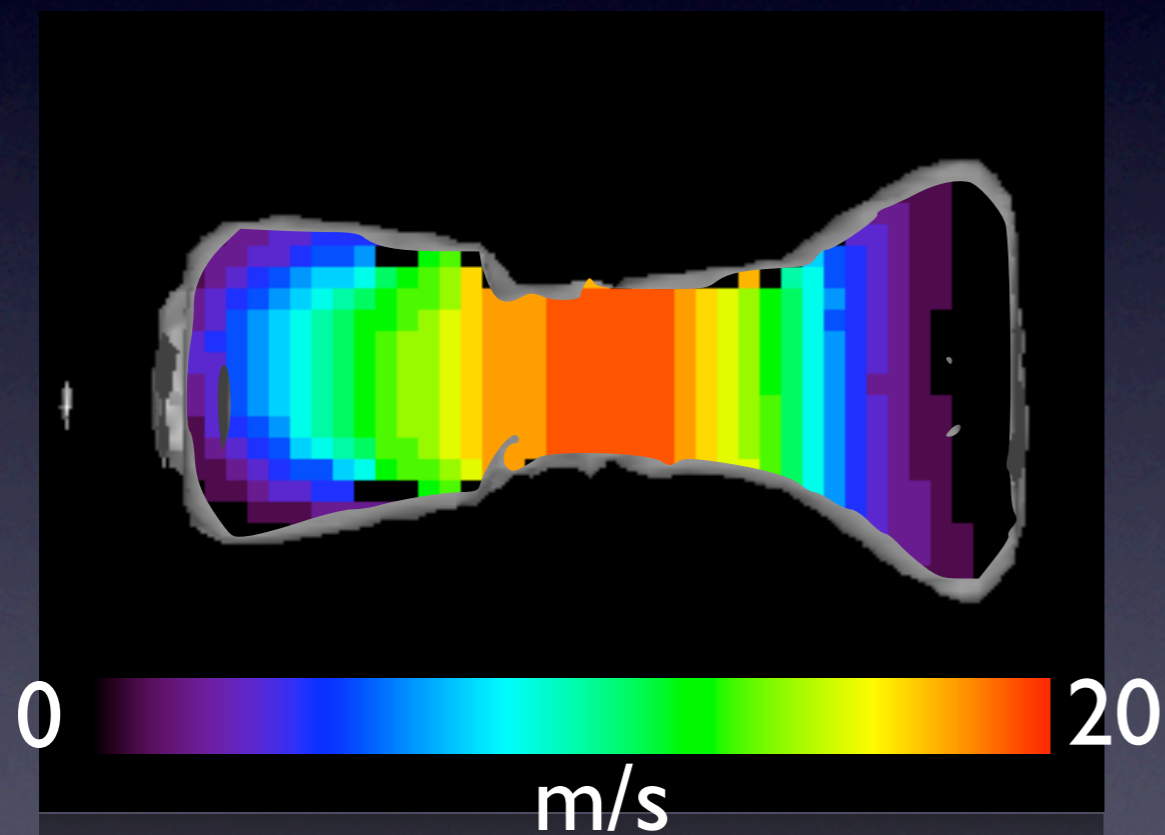


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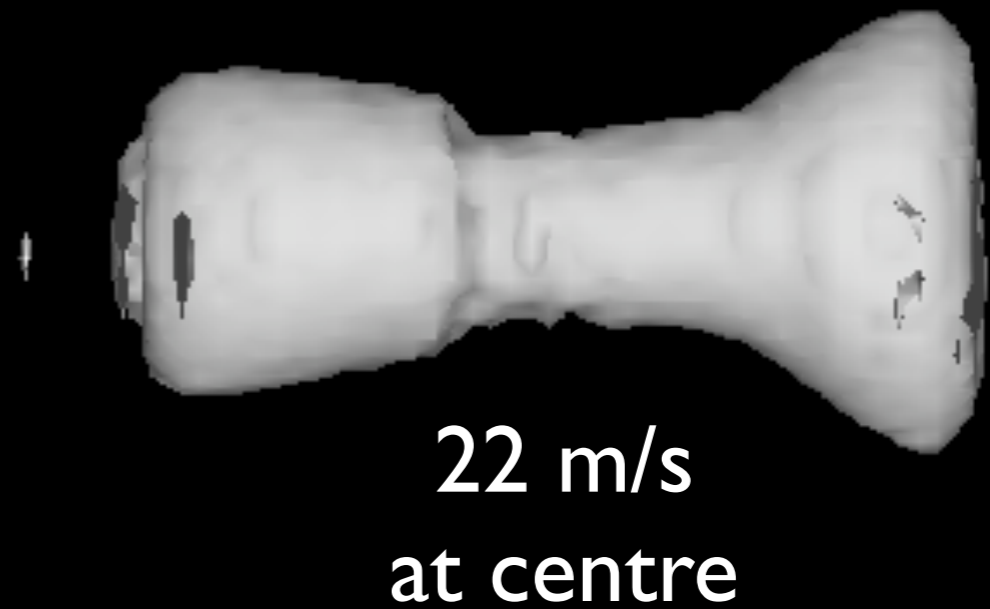


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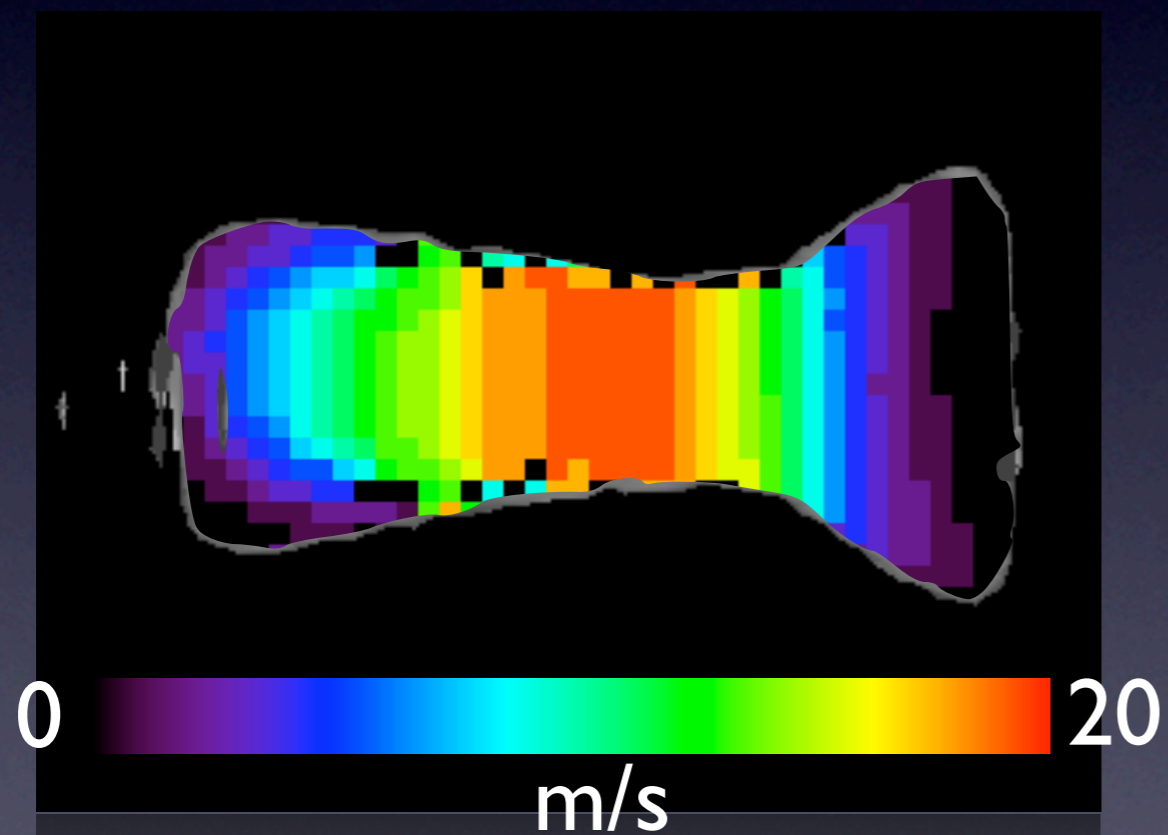


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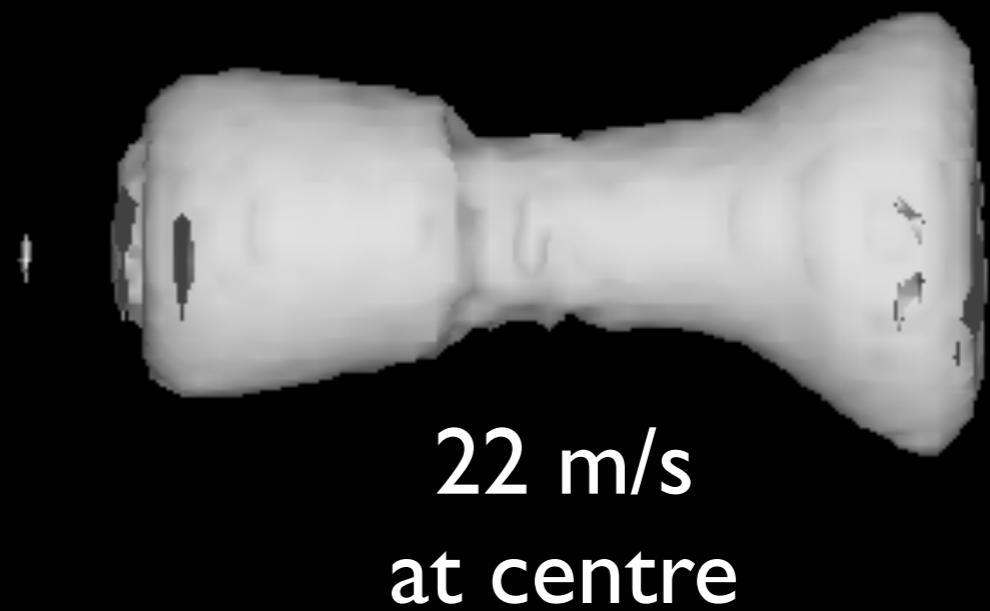


Hydrodynamic Cavitation

Only SPRITE could do this (among MRI),



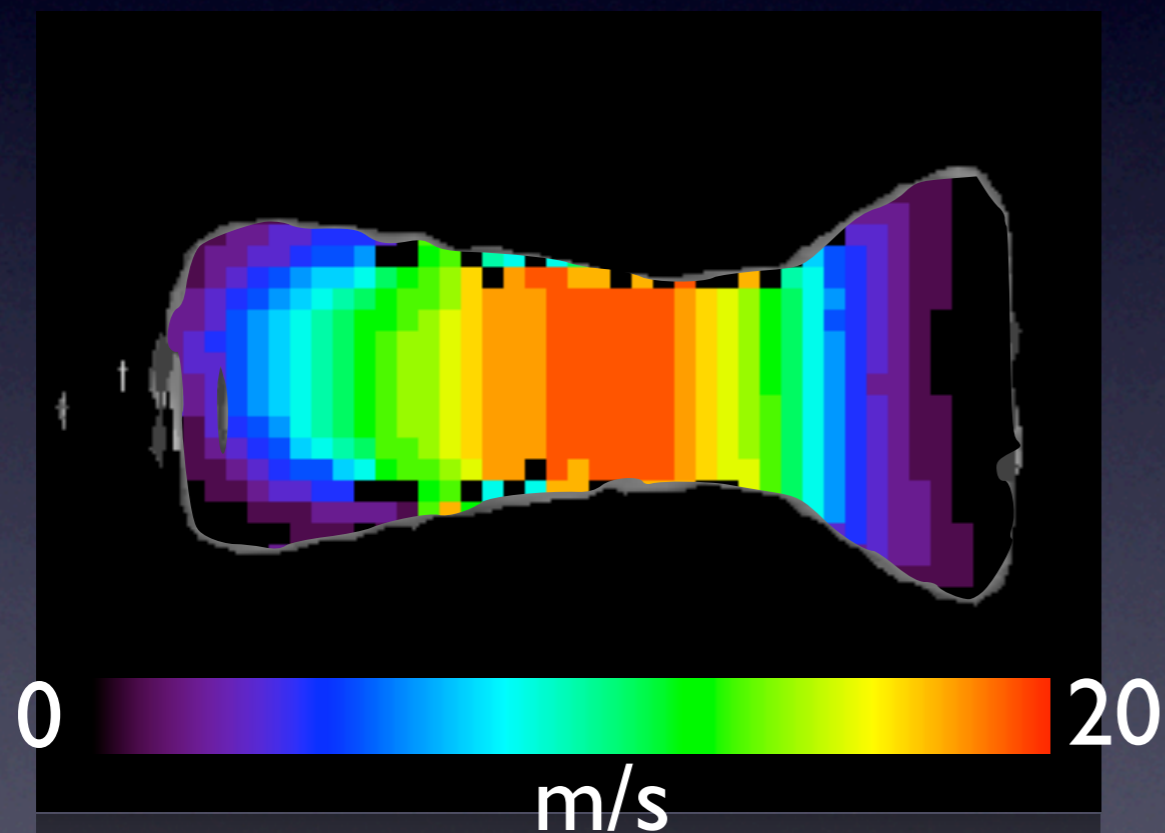
e.g. $t_p = 150 \mu\text{s}$



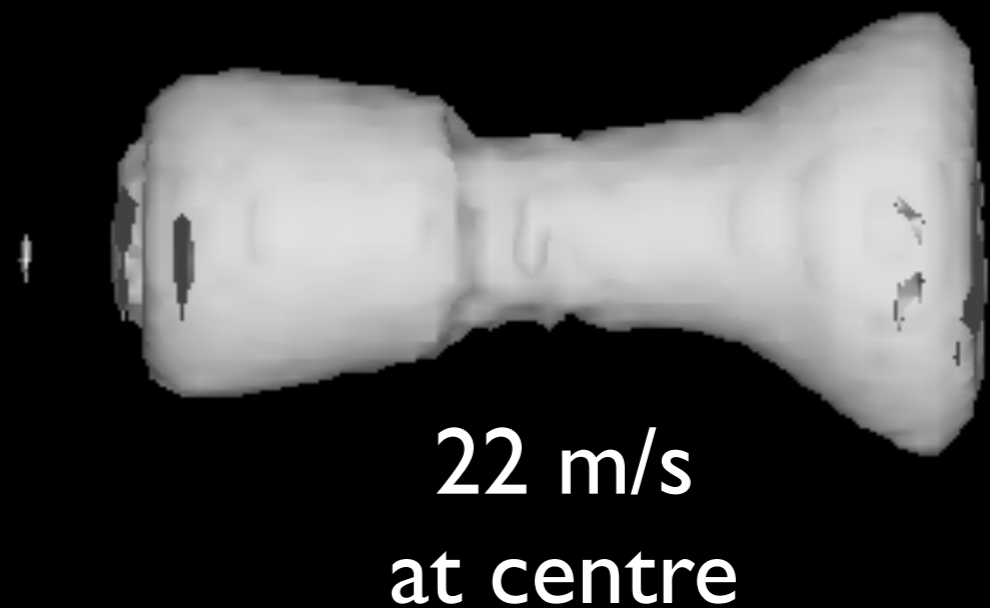
because t_p is short **and** constant.

Hydrodynamic Cavitation

Only SPRITE could do this (among MRI),



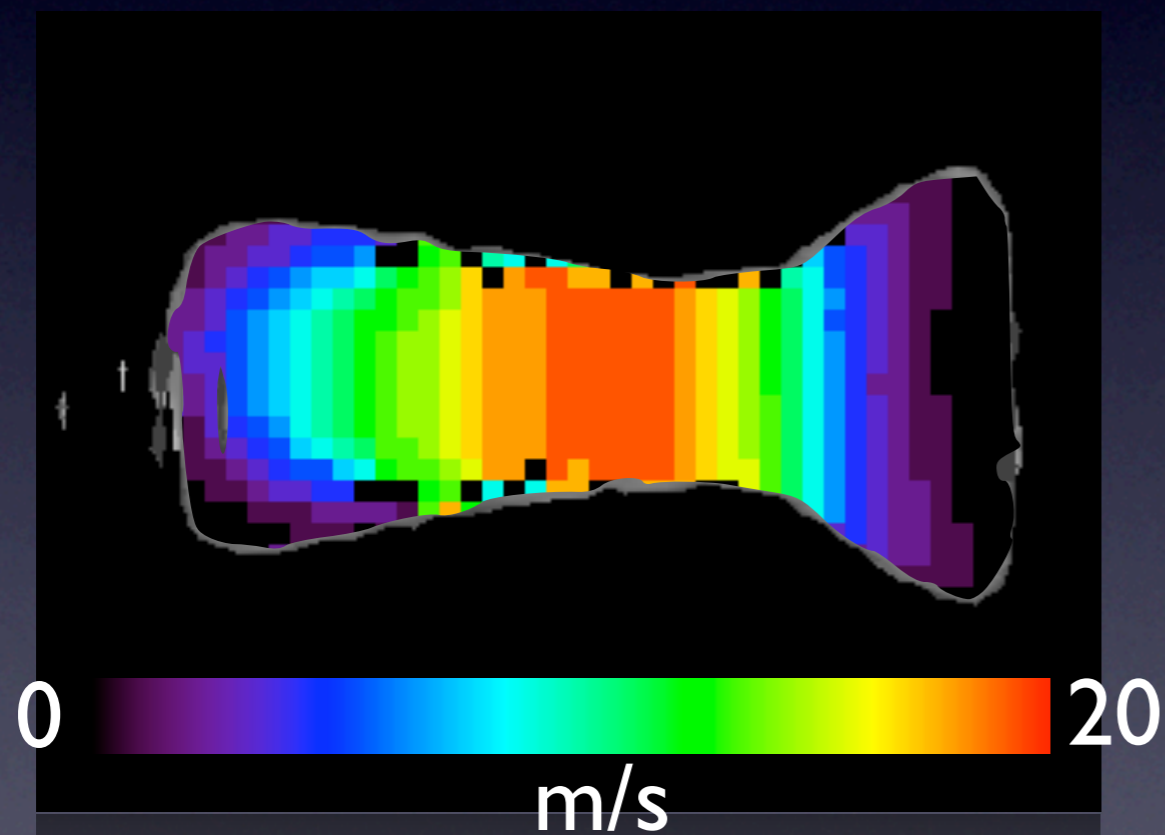
e.g. $t_p = 50, 75, 100, 150 \dots \mu\text{s}$



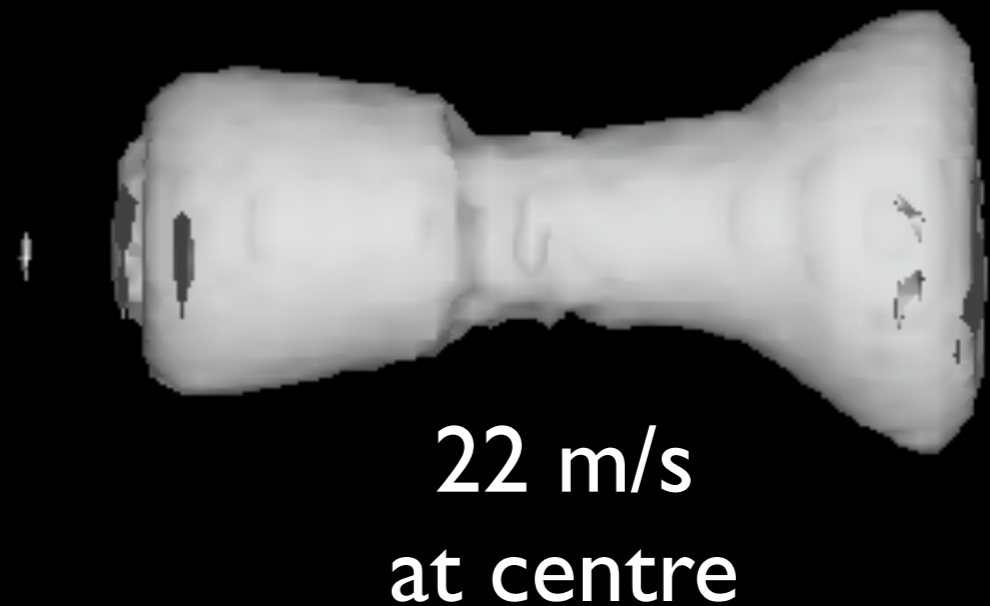
because t_p is short **and** constant.

Hydrodynamic Cavitation

Multiple t_p data allow us to fit the decay and back extrapolate to $t_p = 0$ s, giving volume fraction.



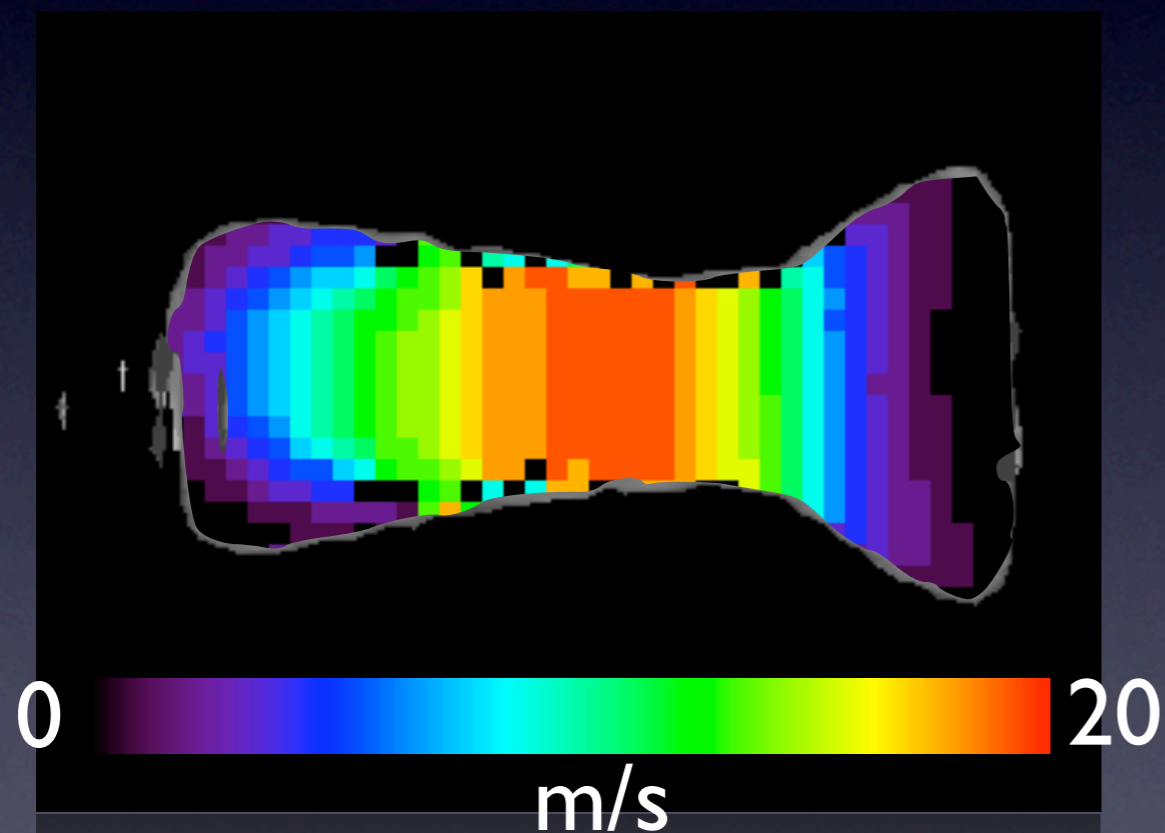
e.g. $t_p = 50, 75, 100, 150 \dots \mu\text{s}$



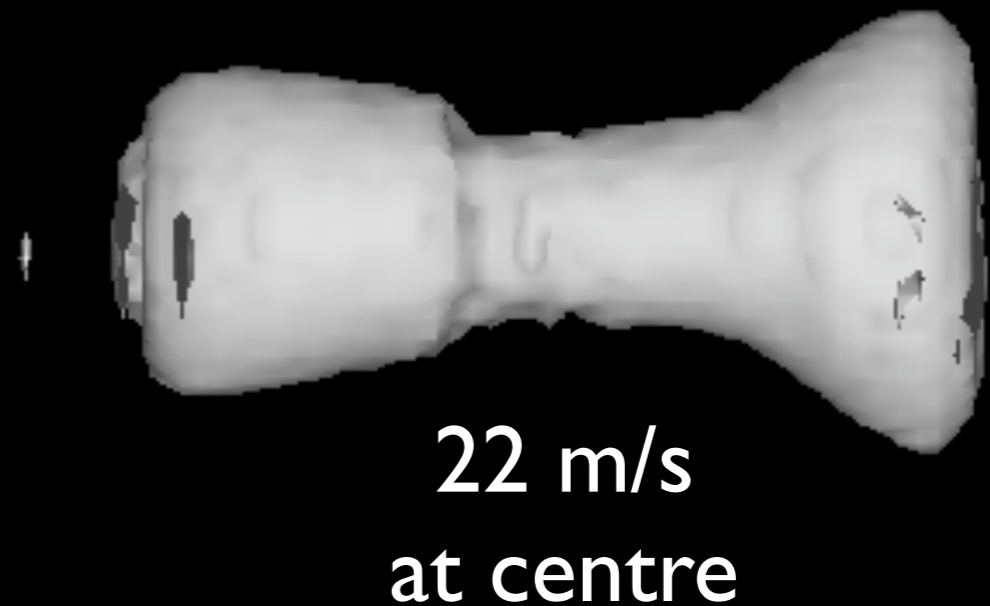
The decay is potentially also informative.

Hydrodynamic Cavitation

Multiple t_p data allow us to fit the decay and back extrapolate to $t_p = 0$ s, giving volume fraction.



e.g. $t_p = 50, 75, 100, 150 \dots \mu\text{s}$



Reminder

www.unb.ca/physics/mri



MRI measures average propagators non-invasively, even in the dark.

SPRITE MRI can do it even when there are liquid/gas interfaces (**two-phase flow**) **or** just gas (**subsonic flow**) ... and when the flow is fast.

The propagator contains information about average velocity **and** velocity fluctuation.

Thanks to Rod, Murray, 2(Brian)



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