

PHY131H1F - Class 10

Today:

- Equilibrium
- Mass, Weight, Gravity



Which of the following objects described below is in *dynamic equilibrium*?

- A. A 100 kg barbell is held *at rest* over your head.
- B. A steel beam is lifted upward at *constant speed* by a crane.
- C. A baseball is flying through the air and *air resistance is negligible*.
- D. A steel beam is being lowered into place. It is *slowing down*.
- E. A box in the back of a truck doesn't slide *as the truck is slowing down*.



Last day I asked at the end of class:

A basketball and a tennis ball are in freefall.

1. Which, if either, has the larger **mass**?

ANSWER: The basketball.

2. Which, if either, experiences the larger **force of gravity**?

ANSWER: The basketball. ( $F_g = mg$ )

3. Which, if either, experiences the larger **acceleration**?

ANSWER: Neither.  $a_y = -g$  for both.

4. Which, if either, has the larger **weight**?

ANSWER: Neither. They are both "weightless".

Preparation for Practicals this week:

- Take a ride on the Burton Tower elevators!
- All 4 elevators in the 14-storey tower of McLennan Physical Labs are equipped with a hanging spring-scale.
- It measures the upward force necessary to support a 500 g mass. (a.k.a. "weight")
- You may find that the measured weight of this object changes as you accelerate – check it out!



- A car is driving at a steady speed on a straight and level road.

Quick quiz [1/4]: inside the car, is it...

A: Inertial Reference Frame

B: Not an inertial reference frame

**⚠ WARNING**

- Newton's Laws only apply in a "inertial reference frames". They are not valid if your reference frame is accelerating!
- An **inertial reference frame** is one that is **not accelerating**.

- A car is driving at a steady speed up a 10° incline.

Quick quiz [2/4]: inside the car, is it...

A: Inertial Reference Frame

B: Not an inertial reference frame

- A car is speeding up after leaving a stop sign, on a straight and level road.

Quick quiz [3/4]: inside the car, is it...

A: Inertial Reference Frame

B: Not an inertial reference frame

- A car is driving at a steady speed around a curve on a level road.

Quick quiz [4/4]: inside the car, is it...

A: Inertial Reference Frame

B: Not an inertial reference frame

Equilibrium  $\boxed{\Sigma \vec{F} = 0}$

- An important problem solving technique is to identify when an object is in equilibrium.
- An object has zero acceleration if and only if the net force on it is zero.
- This is called “equilibrium”.
- If an object is in **vertical equilibrium** (ie it is confined to a stationary horizontal surface) then  $(F_{\text{net}})_y = 0$ . The sum of y-components of all forces = 0.
- If an object is in **horizontal equilibrium** (ie freefall) then  $(F_{\text{net}})_x = 0$ .



## Gravity for the universe



It was Newton who first recognized that **gravity is an attractive, long-range force between any two objects**. Somewhat more loosely, gravity is a force that acts on mass. When two objects with masses  $m_1$  and  $m_2$  are separated by distance  $r$ , each object pulls on the other with a force given by Newton’s law of gravity, as follows:

$$F_{1 \text{ on } 2} = F_{2 \text{ on } 1} = \frac{Gm_1m_2}{r^2} \quad (\text{Newton's law of gravity})$$

(Sometimes called “Newton’s 4<sup>th</sup> Law”, or “Newton’s Law of Universal Gravitation”)

## Gravity for Earthlings

If you happen to live on the surface of a large planet with radius  $R$  and mass  $M$ , you can write the gravitational force even more simply as

$$\vec{F}_G = (mg, \text{ straight down}) \quad (\text{gravitational force})$$

where the quantity  $g$  is defined to be:

$$g = \frac{GM}{R^2}$$

At sea level,  $g = 9.83 \text{ m/s}^2$ .

At 39 km altitude,  $g = 9.71 \text{ m/s}^2$ .



Gravity:  $F_G = mg$  is just a short form!

$$F_{1 \text{ on } 2} = F_{2 \text{ on } 1} = \frac{Gm_1m_2}{r^2}$$

and

$$\vec{F}_G = (mg, \text{straight down})$$

are the same equation, with different notation!

The only difference is that in the second equation we have assumed that  $m_2 = M$  (mass of the earth) and  $r \approx R$  (radius of the earth).

### Weight $\neq$ Weight ???

- Physics textbooks and physics teachers do not all agree on the definition of the word "weight"!
- Sometimes "weight" means the exact same thing as "force of gravity". That is **not** how Randall Knight uses the word. (I will follow Knight's definitions.)
- In Knight, "weight" means the magnitude of the *upward* force being used to support an object.
- If the object is at rest** or moving at a constant velocity relative to the earth, then the object is in equilibrium. The upward supporting force exactly balances the downward gravitational force, so that weight =  $mg$ .



## Test 1 Marking

- You can find the percentage of your Test 1 mark under the My Grades link on portal.
- Your actual mark is this mark times 40 divided by 100.
- The free-form questions will be handed back to you in Practicals. The marks for each part are written there.
- If you subtract the sum of your free-form marks from the total mark on portal, you can figure out what you got on the multiple choice part.
- If you wish to look over the bubble-sheet you turned in for the multiple choice part, please go to MP129.
- If you are concerned about the marking of your test, you have until **Monday, October 22**, at 5:00pm, to take these concerns to the office of the Course Coordinator, Dr. Savaria (MP129). No request will be considered after that date.

### Weight - example

- When I stand on a scale in my bathroom it reads 185 pounds.  $2.2 \text{ pounds} = 9.8 \text{ Newtons}$ , so this means the upward force on my feet when I am standing still is 185 lbs ( $9.8 \text{ N} / 2.2 \text{ lbs} = 824 \text{ N}$ ).
- If I ride an elevator which is accelerating upward at  $1.5 \text{ m/s}^2$ , what is the upward force on my feet?
- [ Take a wild guess first: **A: 824 N, B: 950 N, C: 698 N, D: 0 N, E: -824 N** ]

### Knight's Definition of weight

Eq. 6.10, page 147:

The **weight** of an object is the reading of a calibrated spring scale on which the object is stationary. Weight is the result of weighing. The weight of an object with vertical acceleration  $a_y$  is

$$w = mg \left( 1 + \frac{a_y}{g} \right)$$

### Spring scale on an elevator

You are attempting to pour out 1.0 kg of flour, using a kitchen scale on an elevator which is accelerating upward at  $1.5 \text{ m/s}^2$ .

The amount of flour you pour will be

- A. too much.
- B. too little.
- C. the correct amount.



## Pan balance on an elevator

You are attempting to pour out 100 g of salt, using a pan balance on an elevator which is accelerating upward at  $1.5 \text{ m/s}^2$ . Will the amount of salt you pour be



- A. Too much
- B. Too little
- C. The correct amount

## Self-adjusting forces

- Gravity,  $F_G$ , has an equation for it which predicts the correct magnitude (it's always  $mg$  here on Earth).
- Normal force, Tension and Static friction are all self-adjusting forces: **there is no equation for these!!**
- Normal force is whatever is needed to keep the object from crashing through the surface.
- Tension is whatever is needed to keep the string or rope from breaking.
- Static friction is whatever is needed to keep the object from slipping along the surface.
- In all these cases, you must draw a free-body diagram and figure out by using equilibrium and Newton's 2<sup>nd</sup> law what the needed force is.

## Getting the piano on the truck

- A piano has a mass of 225 kg.
1. What force is required to push the piano upwards at a constant velocity as you lift it into the truck?
  2. What force is required to push the piano up a frictionless ramp at a constant velocity into the truck? Assume the ramp is 3.00 m long and the floor of the truck is 1.00 m high? What is the normal force of the ramp on the piano?

## Before Class 11 on Wednesday

- Please finish reading Chapter 6
- Take a ride on the Burton Tower elevators, do prep-work for Mechanics Module 3 Activity 2.
- Please read the rest of Knight **Chapter 6**.
- Something to think about:  
Does friction always slow things down? Can friction ever speed things up?