## Class 5 - Sections 2.5-2.7, Preclass Notes

## physics

FOR SCIENTISTS AND ENGINEERS


### 2.5 Free Fall

- The motion of an object moving under the influence of gravity only, and no other forces, is called free fall
- Two objects dropped from the same height will, if air resistance can be neglected, hit the ground at the same time and with the same speed
- Consequently, any two objects in free fall, regardless of their mass, have the same acceleration:
$\vec{a}_{\text {free fall }}=\left(9.80 \mathrm{~m} / \mathrm{s}^{2}\right.$, vertically downward $)$


The apple and feather seen here are falling in a vacuum.

Free Fall

- The velocity graph is a straight line with a slope:

$$
a_{y}=a_{\text {free fall }}=-g
$$

(a)
where $g$ is a positive number which is equal to $9.80 \mathrm{~m} / \mathrm{s}^{2}$ on the surface of the earth

- Other planets have different values of $g$
(b)


Tactics: Interpreting graphical representations of motion


### 2.6 Motion on an Inclined Plane

- Consider an object sliding down a straight, frictionless inclined plane
- $\vec{a}_{\text {free fall }}$ is the acceleration the object would have if the incline suddenly vanished.
- This vector can be broken into two pieces: $\vec{a}_{\|}$and $\vec{a}_{\perp}$
- The surface somehow "blocks" $\vec{a}_{\perp}$, so the onedimensional acceleration along the incline is:

$$
a_{s}= \pm g \sin \theta
$$




Chapter 2 Goal: To learn how to solve problems about motion in a straight line.

### 2.7 Non-Constant Acceleration

- Figure (a) shows a realistic velocity-versus-time graph for a car leaving a stop sign
- The graph is not a straight line, so this is not motion with a constant acceleration
- Figure (b) shows the car's acceleration graph
- The instantaneous acceleration $a_{s}$ is the slope of the line that is tangent to the velocity-versus-time curve at time $t$
(a) The car speeds up from rest until $a_{s}$ The value of the accel- $\begin{aligned} & \text { eration is the slope of } \\ & \text { the velocity graph. } \\ & a_{x} \\ & \text { Steep slope is large } \\ & \text { acceleration; the velocity } \\ & \text { Shallow slope is } \\ & \text { small acceleration. }\end{aligned}$ $a_{s}=\frac{d v_{s}}{d t}=$ slope of the velocity-versus-time graph at time $t$


## Finding Velocity from Acceleration

- Suppose we know an object's velocity to be $v_{\text {is }}$ at an initial time $t_{\mathrm{i}}$
- We also know the acceleration as a function of time between $t_{\mathrm{i}}$ and some later time $t_{\mathrm{f}}$
- Even if the acceleration is not constant, we can divide the motion into $N$ steps of length $\Delta t$ in which it is approximately constant
- In the limit $\Delta t \rightarrow 0$ we can compute the final velocity as

$$
v_{\mathrm{fs}}=v_{\mathrm{i} s}+\lim _{\Delta t \rightarrow 0} \sum_{k=1}^{N}\left(a_{s}\right)_{k} \Delta t=v_{\mathrm{i} s}+\int_{t_{\mathrm{i}}}^{t_{\mathrm{f}}} a_{s} d t
$$

-The integral may be interpreted graphically $a_{s}$ the area under the acceleration curve as between $t_{\mathrm{i}}$ and $t_{\mathrm{f}}$

