

#### Chapter 6 Dynamics I: Motion Along a Line



Chapter Goal: To learn how to solve linear force-and-motion problems.

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**Quick Note:** We will not be covering the material from Knight Section 6.4 on "Rolling Friction"

Chapter Goal: To learn how to solve linear force-and-motion problems.

#### Static Friction

- A shoe pushes on a wooden floor but does not slip.
- On a microscopic scale, both surfaces are "rough" and high features on the two surfaces form molecular bonds.
- These bonds can produce a force tangent to the surface, called the static friction force.

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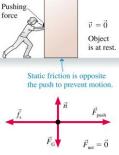
Two surfaces in contact Very few points are actually in contact.

Molecular bonds form between the two , materials. The molecular springs pull and push tangential to the surface, providing the static friction force.

## Static Friction

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- The figure shows a person pushing on a box that, due to static friction, isn't moving.
- Looking at the free-body diagram, the *x*-component of Newton's first law requires that the static friction force must exactly balance the pushing force: f<sub>s</sub> = F<sub>push</sub>



•  $\vec{f}_s$  points in the direction *opposite* to the way the object would move if there were no static friction.

# Static Friction

Static friction acts in

response to an

applied force.

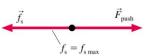
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 $\vec{F}_{\text{push}}$  is balanced by  $\vec{f}_{\text{s}}$  and the box does not move.

 $\vec{f_{s}}$  $\vec{F}_{\text{push}}$ 

As  $\vec{F}_{\text{push}}$  increases,  $\vec{f}_{\text{s}}$  grows . . .



... until  $f_s$  reaches  $f_{s \max}$ . Now, if  $\vec{F}_{push}$  gets any bigger, the object will start to move.

#### Static Friction

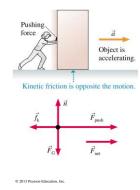
- Static friction force has a maximum possible size  $f_{\rm s\ max}$ .
- An object remains at rest as long as f<sub>s</sub> < f<sub>s max</sub>.
- The object just begins to slip when  $f_s = f_{s max}$ .
- A static friction force f<sub>s</sub> > f<sub>s max</sub> is not physically possible.

$$f_{\rm s max} = \mu_{\rm s} n$$

where the proportionality constant  $\mu_{\rm s}$  is called the coefficient of static friction.

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#### **Kinetic Friction**



 The kinetic friction force is proportional to the magnitude of the normal force:

$$f_k = \mu_k n$$

where the proportionality constant  $\mu_k$  is called the coefficient of kinetic friction.

- The kinetic friction direction is opposite to the velocity of the object relative to the surface.
- For any particular pair of surfaces, μ<sub>k</sub> < μ<sub>s</sub>.

## Coefficients of Friction

Materials	Static $\mu_{s}$	Kinetic $\mu_k$
Rubber on concrete	1.00	0.80
Steel on steel (dry)	0.80	0.60
Steel on steel (lubricated)	0.10	0.05
Wood on wood	0.50	0.20
Wood on snow	0.12	0.06
Ice on ice	0.10	0.03

## **Rolling Motion**

- If you slam on the brakes so hard that the car tires slide against the road surface, this is kinetic friction.
- Under normal driving conditions, the portion of the rolling wheel that contacts the surface is stationary, not sliding.



 If your car is accelerating or decelerating or turning, it is the static friction of the road on the wheels that provides the net force which accelerates the car.

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# A Model of Friction

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- The actual causes of friction involve microscopic surface properties and molecular bonds.
- Experiments show that reasonable predictions are produced by a model of friction — a simplification of reality:

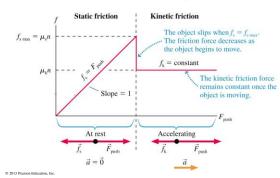
Static:  $\vec{f}_s \leq (\mu_s n, \text{direction as necessary to prevent motion})$ Kinetic:  $\vec{f}_k = (\mu_k n, \text{direction opposite the motion})$ 

- Here "motion" means "motion relative to the surface."
- Force of kinetic friction is proportional to the normal force of the surface on the object.
- The *maximum* static friction force is proportional to the normal force of the surface on the object.

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#### A Model of Friction

The friction force response to an increasing applied force:



#### Section 6.5: Drag

- The air exerts a drag force on objects as they move through the air.
- Faster objects experience a greater drag force than slower objects.
- The drag force on a high-speed motorcyclist is significant.
- The drag force direction is opposite the object's velocity.



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# Drag

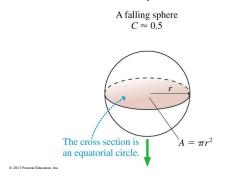
 For normal-sized objects on earth traveling at a speed v which is less than a few hundred meters per second, air resistance can be modeled as:

 $\vec{D} = (\frac{1}{2}C\rho Av^2)$ , direction opposite the motion)

- A is the cross-section area of the object.
- $\rho$  is the density of the air, which is about 1.2 kg/m<sup>3</sup>.
- C is the drag coefficient, which is a dimensionless number that depends on the shape of the object.

# Drag

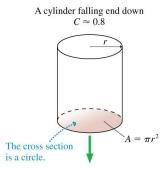
Cross-section areas for objects of different shape.



#### Drag

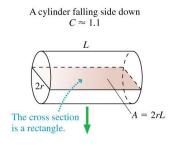
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#### Cross-section areas for objects of different shape.



#### Drag

Cross-section areas for objects of different shape.



## **Terminal Speed**

- The drag force from the air increases as an object falls and gains speed.
- If the object falls far enough, it will eventually reach a speed at which D = F<sub>G</sub>.

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Terminal speed is reached when the drag force exactly balances the gravitational force:  $\vec{a} = \vec{0}$ .

 At this speed, the net force is zero, so the object falls at a *constant* speed, called the **terminal speed** v<sub>term</sub>.

 $\vec{F}_{G}$ 

$$v_{\text{term}} = \sqrt{\frac{2mg}{C\rho A}}$$

## The velocity starts at zero, then becomes increasingly negative **Terminal Speed** (motion in -y-direction). As drag increases with increasing speed, the slope V., decreases in magnitude. 0 Vtern The slope approaches zero (no further acceleration) as the object approaches terminal speed v<sub>term</sub>. Without drag, the graph is a straight line with slope $a_y = -g$ .

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# Section 6.6: More Examples of Newton's 2<sup>nd</sup> Law



Please work through the examples in Section 6.6.

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# **General Strategy**

#### **Equilibrium Problems**

Object at rest or moving with constant velocity.

MODEL Make simplifying assumptions.

· Translate words into symbols.

· Identify forces. · Draw a free-body diagram.

SOLVE Use Newton's first law:

$$\vec{F}_{\rm net} = \sum_i \vec{F}_i = \vec{0}$$

"Read" the vectors from the free-body diagram. ASSESS Is the result reasonable?

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# **General Strategy**

#### **Dynamics Problems**

Object accelerating.

MODEL Make simplifying assumptions.

#### VISUALIZE

- · Translate words into symbols.
- · Draw a sketch to define the situation. • Draw a motion diagram.
- · Identify forces.
- Draw a free-body diagram.

SOLVE Use Newton's second law:

#### $\vec{F}_{net} = \sum \vec{F}_i = m\vec{a}$

"Read" the vectors from the free-body diagram. Use kinematics to find velocities and positions. ASSESS Is the result reasonable?

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