PHY132 Introduction to Physics II
Class 12 - Outline:

- Electric Potential of:
- Parallel Plate Capacitor
- Point Charge
- Many Charges



## Last time I asked you to consider...

- A battery is designed to supply a steady amount of which of the following quantities?
- Energy
- Power
- Electric potential difference
- Electric current


## The Electric Field Inside a Parallel-Plate Capacitor

This is a review of Chapter 26.


$$
\begin{aligned}
\vec{E} & =\left(\frac{\eta}{\epsilon_{0}}, \text { from positive toward negative }\right) \\
& =(500 \mathrm{~N} / \mathrm{C}, \text { from right to left })
\end{aligned}
$$

## The Electric Potential Inside a Parallel-Plate Capacitor

- The electric potential inside a parallel-plate capacitor is

$$
V=E s \quad \text { (electric potential inside a parallel-plate capacitor) }
$$

where $s$ is the distance from the negative electrode.

- The potential difference $\Delta V_{\mathrm{C}}$, or "voltage" between the two capacitor plates is

$$
\Delta V_{\mathrm{C}}=V_{+}-V_{-}=E d
$$



## Units of Electric Field

- If we know a capacitor's voltage $\Delta V$ and the distance between the plates $d$, then the electric field strength within the capacitor is:

$$
E=\frac{\Delta V_{\mathrm{C}}}{d}
$$

- This implies that the units of electric field are volts per meter, or V/m.
- Previously, we have been using electric field units of newtons per coulomb.
- In fact, as you can show as a homework problem, these units are equivalent to each other:

$$
1 \mathrm{~N} / \mathrm{C}=1 \mathrm{~V} / \mathrm{m}
$$

## The Electric Potential Inside a Parallel-Plate Capacitor



## The Electric Potential Inside a Parallel-Plate Capacitor



Two protons, one after the other, are launched from point 1 with the same speed. They follow the two trajectories shown. The protons' speeds at
 points 2 and 3 are related by
A. $\quad v_{2}>v_{3}$.
B. $v_{2}=v_{3}$.
C. $v_{2}<v_{3}$.
D. Not enough information to compare their speeds.

## The Parallel-Plate Capacitor

- The figure shows the contour lines of the electric potential and the electric field vectors inside a parallel-plate capacitor.
- The electric field vectors are perpendicular to the equipotential surfaces.
- The electric field points in the direction of decreasing potential.



## The Zero Point of Electric Potential

Where you choose $V=0$ is arbitrary. The three contour maps below represent the same physical situation.


The potential difference between two points is the same in all three cases.
(b)

(c)


The electric field inside is the same in all three cases.

## The Electric Potential of a Point Charge

- Let $q$ in the figure be the source charge, and let a second charge $q^{\prime}$, a distance $r$ away, probe the electric potential of $q$.
- The potential energy of the two point charges is


$$
U_{q^{\prime}+q}=\frac{1}{4 \pi \epsilon_{0}} \frac{q q^{\prime}}{r}
$$

## The Electric Potential of a Point Charge

- The electric potential due to a point charge $q$ is
$V=\frac{U_{q^{\prime}+q}}{q^{\prime}}=\frac{1}{4 \pi \epsilon_{0}} \frac{q}{r} \quad$ (electric potential of a point charge)
- The potential extends through all of space, showing the influence of charge $q$, but it weakens with distance as $1 / r$.
- This expression for $V$ assumes that we have chosen $V=0$ to be at $r=\infty$.

What is the ratio $V_{\mathrm{B}} / V_{\mathrm{A}}$ of the electric potentials at the two points?
A. 9 .
B. 3 .

C. $1 / 3$.
D. $1 / 9$.
E. Undefined without knowing the charge.

## The Electric Potential of a Point Charge



## Quick Equations Quiz.. [1/4] Which is which?

The magnitude of the force, in Newtons, on a point charge that is near another point charge is:
A. $K \frac{q}{r}$
B. $K \frac{q}{r^{2}}$
C. $K \frac{q_{1} q_{2}}{r}$
D. $K \frac{q_{1} q_{2}}{r^{2}}$

$$
K=\frac{1}{4 \pi \varepsilon_{0}}
$$

## Quick Equations Quiz.. [2/4] Which is which?

The magnitude of the Electric Field, in
Newtons per Coulomb, near a point charge is:
A. $K \frac{q}{r}$
C. $K \frac{q_{1} q_{2}}{r}$
B. $K \frac{q}{r^{2}}$
D. $K \frac{q_{1} q_{2}}{r^{2}}$

$$
K=\frac{1}{4 \pi \varepsilon_{0}}
$$

## Quick Equations Quiz.. [3/4] Which is which?

The electric potential energy, in Joules, of two point charges is:
A. $K \frac{q}{r}$
C. $K \frac{q_{1} q_{2}}{r}$
B. $K \frac{q}{r^{2}}$
D. $K \frac{q_{1} q_{2}}{r^{2}}$

$$
K=\frac{1}{4 \pi \varepsilon_{0}}
$$

## Quick Equations Quiz.. [4/4] Which is which?

The electric potential, in Volts, near a point charge is:
A. $K \frac{q}{r}$
C. $K \frac{q_{1} q_{2}}{r}$
B. $K \frac{q}{r^{2}}$
D. $K \frac{q_{1} q_{2}}{r^{2}}$

$$
K=\frac{1}{4 \pi \varepsilon_{0}}
$$

The Electric Potential of a Point Charge


## The Electric Potential of a Charged Sphere

Outside a uniformly charged sphere of radius $R$, the electric potential is identical to that of a point charge $Q$ at the center.

$$
V=\frac{1}{4 \pi \epsilon_{0}} \frac{Q}{r}
$$


where $r>R$.
If the potential at the surface $V_{0}$ is known, then the potential at $r>R$ is:

$$
V=\frac{R}{r} V_{0}
$$

An electron follows the trajectory shown from point 1 to point 2. At point 2,
A. $\quad v_{2}>v_{1}$.

B. $v_{2}=v_{1}$.
C. $v_{2}<v_{1}$.
D. Not enough information to compare the speeds at these points.

## The Electric Potential of Many Charges

- The electric potential $V$ at a point in space is the sum of the potentials due to each charge:

$$
V=\sum_{i} \frac{1}{4 \pi \epsilon_{0}} \frac{q_{i}}{r_{i}}
$$

where $r_{i}$ is the distance from charge $q_{i}$ to the point in space where the potential is being calculated.

- The electric potential, like the electric field, obeys the principle of superposition.

Problem 28.66
The arrangement of charges shown is called a linear electric quadrupole. The positive charges are located at $y= \pm s$.
Find an expression for the electric potential on the $y$-axis at a distance $y \gg s$.


## The Electric Potential of an Electric Dipole

(a) Contour map

(b) Elevation graph


## The Electric Potential of a Human Heart

- Electrical activity within the body can be monitored by measuring equipotential lines on the skin.
- The equipotentials near the heart are a slightly distorted but recognizable electric dipole.


At the midpoint between these two equal but opposite charges,
A. $\vec{E}=\overrightarrow{0} ; V=0$.
B. $\vec{E}=\overrightarrow{0} ; V>0$.
C. $\vec{E}=\overrightarrow{0} ; V<0$.
D. $\vec{E}$ points right; $V=0$.
E. $\vec{E}$ points left; $V=0$.

At which point or points is the electric potential zero?

E. More than one of these.

## The next test...

- Term Test 2 is in 4 weeks:
- Tuesday, Mar. 10 6:10pm in room TBA
- This will cover Chapters 25, 26, 28, 29 and conceptual questions (clicker-style questions) from Chapter 30
- Remember the second half of chapter 23 on lenses will not be tested on the midterm or final exam.


## Have a great Reading Week!!

- Happy Valentine's Day tomorrow!
- Sorry, no office hours for me next week.
- When you get back on Feb. 23, Professor Meyertholen will start where I am leaving off: Chapter 29, connecting Electric Potential with Electric Field.
- I hope you enjoy the rest of your semester, and please keep coming to see me in office hours; you are my students until the final exam is done!
- And even after you are no longer my students, please stay in touch and drop by whenever you like!
- Best wishes and see you around!

