



Exact

Approximate.

~~$t_4 = 5.38$ s WOODS.~~

$t_5 = 7.53$ s

7.38 s

7.47 s

7.43 s

~ 1800 Gauss discovered repeated measurements produce a distribution of answers.

Histogram looks like a bell.

$$N(x) = A e^{\left[\frac{-(x-\bar{x})^2}{2\sigma^2} \right]}$$

where $N(x)$ = number of measurements whose value is near x .

A = arbitrary constant

$$e = 2.7182\dots$$

\bar{x} = mean or average
 σ = standard deviation

} these can be estimated from the data.

Error propagation.

Sum Rule

Product Rule

Multiply by an exact constant rule

Example: 5 oscillations take
 7.53 ± 0.06 seconds

What is the period? 1.506

error?

or
 1.51 ± 0.01

→ multiplying by exact constant $\frac{1}{5}$

error: 0.012

answer: $T = 1.506 \pm 0.012$

Error in mean of n measurements

$$\bar{x} = \frac{(x_1 \pm \Delta x) + (x_2 \pm \Delta x) + \dots}{n}$$

Sum: $X_{\text{sum}} = x_1 + x_2 + \dots + x_n$

Mean: $\bar{x} = X_{\text{sum}}/n$

$$\Delta X_{\text{sum}} = \sqrt{\Delta x^2 + \Delta x^2 + \dots}$$

n times

$$\Delta X_{\text{sum}} = \sqrt{n \Delta x^2}$$
$$= \sqrt{n} (\Delta x)$$

Error in mean:

$$\Delta \bar{x} = \frac{\sqrt{n}}{n} (\Delta x)$$

$$\Delta \bar{x} = \frac{\Delta x}{\sqrt{n}}$$

error in mean

Error in a "quoted value" is \pm half last digit

$$\text{ie } c = 3.00 \times 10^8 \text{ m/s}$$

$$\downarrow \pm 0.005 \times 10^8 \text{ m/s}$$

calculation: 7.076 ± 0.705

0.7
↑
tenths place
is most
significant

↑

$$\boxed{7.1 \pm 0.7}$$