

PHY138 – Waves, Lecture 5  
*Today's overview*

- The Principle of Superposition
- Standing Waves
- The Guitar: Stringed Instruments
- The Trumpet: Wind Instruments

Doppler Effect, Section 20.7

- When the observer is stationary, and the source is moving at speed  $v_s$  directly toward or away from the observer:

$$f_+ = \frac{f_0}{1 - v_s/v} \quad f_- = \frac{f_0}{1 + v_s/v}$$

- When the source is stationary, and the observer is moving at speed  $v_o$  directly toward or away from the source:

$$f_+ = (1 + v_o/v)f_0 \quad f_- = (1 - v_o/v)f_0$$

Which statement is true?

Adrienne is standing in the middle of the road, as a police car approaches her at a constant speed,  $v$ . The siren on the police car emits a “rest frequency” of  $f_0$ .

- A. The frequency she hears rises steadily as the police car gets closer and closer.
- B. The frequency she hears steadily decreases as the police car gets closer and closer.
- C. The frequency she hears does not change as the police car gets closer.

Which statement is true?

Adrienne is standing still as a police car approaches her at a constant speed,  $v$ . Suzanne is in her cadillac moving at the same constant speed,  $v$ , toward an identical police car which is standing still. Both hear a siren.

- A. The frequency Suzanne hears is lower than the frequency Adrienne hears.
- B. The frequency Suzanne hears is higher than the frequency Adrienne hears.
- C. The frequencies that Suzanne and Adrienne hear are exactly the same.

Actual Answer!  
 Check eq.20.38  
 and 20.39!

(Almost correct)

### Message from Dr. Savaria....

- If you have a conflict at 6:00-7:30 PM on Dec.4 and wish to write Test 2 at an alternate time:
  - Send an email to [phy138y@physics.utoronto.ca](mailto:phy138y@physics.utoronto.ca) (or reply to seeley) confirming that you wish to re-register, if you registered for the alternate sitting of Test 1.

or

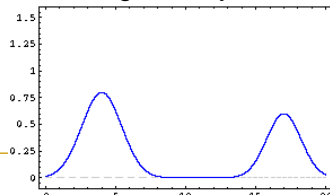
- Visit April Seeley in MP129 or MP302 to register for the first time you will write in an alternate time.
- The deadline for confirming / registering is Nov.26 by 5:00PM.

### Reading Assignment

- This week's reading assignment from the text by Knight is: **Chapter 21**, Sections 21.1-21.8
- Suggested Chapter 21 Exercises and Problems for Practice: 7, 19, 25, 31, 49, 65, 71, **83 (skip part b – just use result)**
- Waves Quarter **Written Team Problem Set** is due Friday by 5:00 PM in T.A. drop box. – You must work in the teams assigned to you in tutorial.

### Chapter 21: Principle of Superposition

- If two or more waves combine at a given point, the resulting disturbance is the *sum* of the disturbances of the individual waves.
- Two traveling waves can pass through each other without being destroyed or even altered!

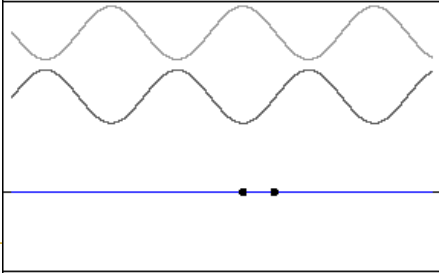


### Some *Results* of Superposition:

- 21.2-21.4: Two waves, same wavelength and frequency, opposite direction:  
**Standing Wave**
- 21.5-21.7: Two waves, same wavelength and frequency, similar direction, different phase:  
**Interference**
- 21.8: Two waves, same direction, slightly different frequency and wavelength:  
**Beats!**

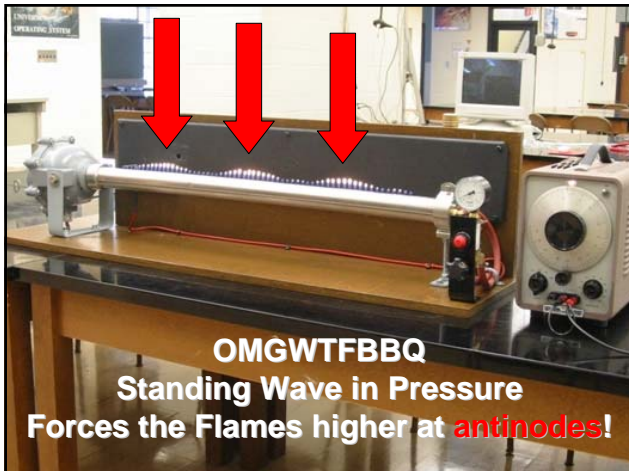
### Standing Wave:

The superposition of two 1-D sinusoidal waves traveling in opposite directions.



### Standing Waves

- Are a form of “resonance”
- There are multiple resonant frequencies called harmonics
- The boundary conditions and speed of waves determine which frequencies are allowed.
- The ends of the resonant cavity have forced nodes or antinodes
- With a wave on a string, it is possible to force an intermediate node



### Harmonic frequencies on a violin

Transverse standing wave on a string clamped at both ends: there are nodes in displacement at both ends.

$$f_m = m \frac{v}{2L} \quad (m = 1, 2, 3, \dots)$$

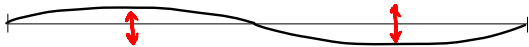
A violin and all other stringed instruments almost always operate in the  $m = 1$  or fundamental frequency.

### Violin Demonstration

A-string, fundamental frequency (A-note)



A-string, second harmonic (m = 2, A-note)

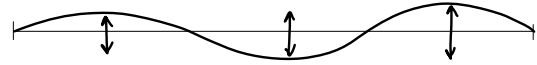


Higher octave A-note played in the normal way

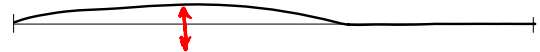


### Violin Demonstration

A-string, third harmonic (m = 3, D-note)



D-note played in the normal way



Harmonic notes in sheet music: boxes



### Harmonic frequencies in air column

Standing sound wave in a tube open at both ends: there are nodes in pressure both ends.

$$f_m = m \frac{v}{2L} \quad (m = 1, 2, 3, \dots)$$

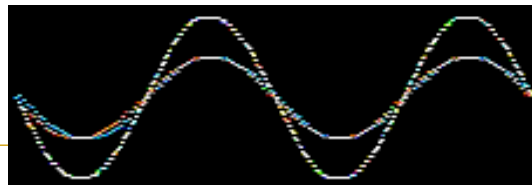
Standing sound wave in a tube closed at one end: there is a node in pressure at the open end, and an anti-node at the closed end.

$$f_m = m \frac{v}{4L} \quad (m = 1, 3, 5, \dots)$$

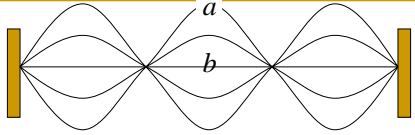
### Standing Wave Quiz

The white wave is the sum of the blue and red waves. It is the

- A. Fundamental Frequency (m=1)
- B. Second Harmonic (m=2)
- C. Third Harmonic (m=3)
- D. Fourth Harmonic (m=4)**
- E. Fifth Harmonic (m=5)

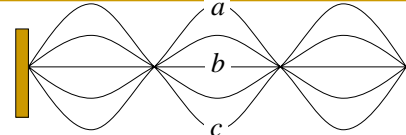


Quiz



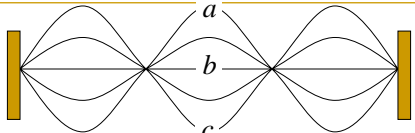
- A string is clamped at both ends and plucked so creates a standing wave. Define upward motion to be positive velocities. When the string is in position *a*, the instantaneous velocity of points along the string
- A. is zero everywhere
- B. is positive everywhere
- C. is negative everywhere
- D. depends on location

Quiz



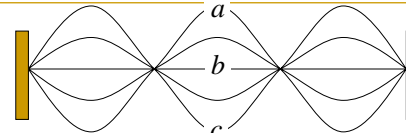
- A string is clamped at both ends and plucked so creates a standing wave. Define upward motion to be positive velocities. When the string is in position *b*, the instantaneous velocity of points along the string
- A. is zero everywhere
- B. is positive everywhere
- C. is negative everywhere
- D. depends on location

Quiz



- A string is clamped at both ends and plucked so creates a standing wave. Define upward motion to be positive velocities. When the string is in position *c*, the instantaneous velocity of points along the string
- A. is zero everywhere
- B. is positive everywhere
- C. is negative everywhere
- D. depends on location

Quiz



- A string is clamped at both ends and plucked so creates a standing wave. Define upward motion to be positive velocities. When the string is in position *b*, the instantaneous **acceleration** of points along the string
- A. is zero everywhere
- B. is positive everywhere
- C. is negative everywhere
- D. depends on location