

Note:  $T = \frac{J_R}{J_I} = \frac{|t_{trans}|^2 V_{trans}}{|r_{inc}|^2 V_{inc}}$

$$\frac{V_{II}}{V_I} = \frac{k_{II}}{k_I} \quad \therefore \begin{matrix} P_{trans} \\ \parallel \\ R \\ \parallel \\ k_I \end{matrix}$$

Similarly for R

< prob current >

$$J(x,t) = -\frac{i\hbar}{2m} \left( \Psi^* \frac{\partial \Psi}{\partial x} - \Psi \frac{\partial \Psi^*}{\partial x} \right)$$

For steady-state (unique  $\Psi$ )

Continuity:  $\left[ \frac{\partial |\Psi|^2}{\partial t} + \nabla \cdot \vec{J} = 0 \right]$

$$\Psi \rightarrow \Psi$$

Note:  $J_I = J_{II}$   ~~$J_{III}$~~  Conservation of Prob Density

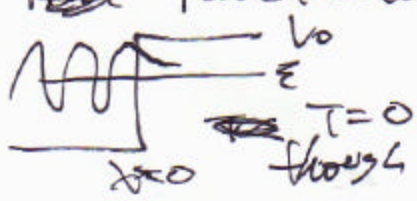


$$\begin{aligned} \Psi_I(x) &= A_0 e^{ik_1 x} + A e^{-ik_1 x} \\ \Psi_{II}(x) &= B e^{ik_2 x} + C e^{-ik_2 x} \\ \Psi_{III}(x) &= D e^{ik_1 x} \end{aligned}$$

resonant transmission:  $(k_2 L = n\pi)$

$$4k_1 k_2 A_0 = (C e^{ik_2 L} + B e^{-ik_2 L}) e^{-ik_1 L} - (k_2 - k_1) e^{ik_1 L} e^{ik_2 L} e^{ik_1 L}$$

Penetration vs. Tunneling



through  $|t(\omega)|^2 \neq 0$

$T \propto e^{-2\alpha L}$   
 $\alpha L \gg 1$