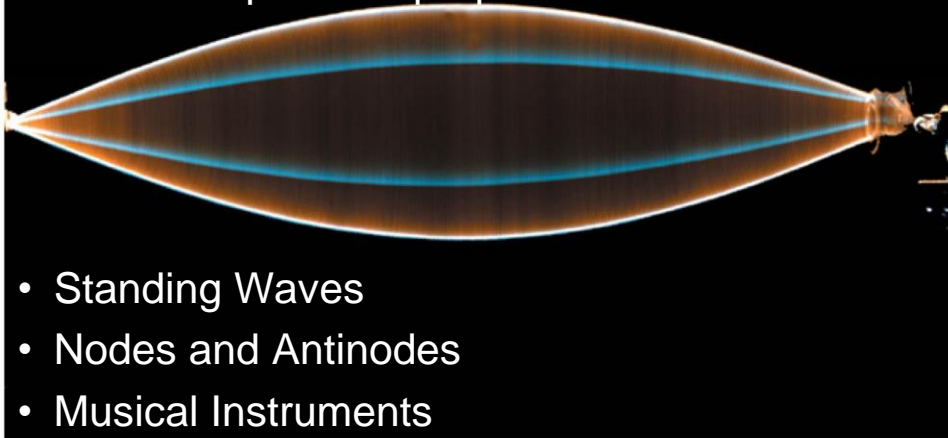


PHY132 Introduction to Physics II

Class 3 – Outline:

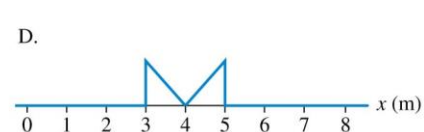
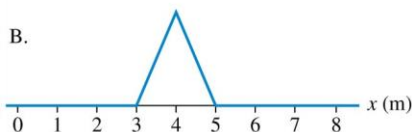
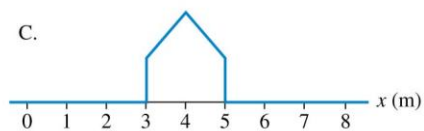
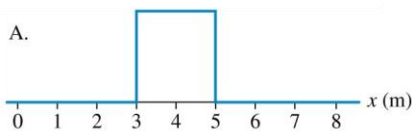
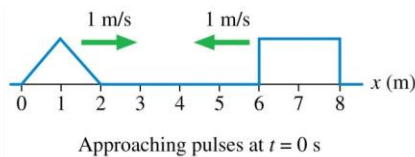
- Ch. 21, sections 21.1-21.4
- The Principle of Superposition



- Standing Waves
- Nodes and Antinodes
- Musical Instruments

i-Clicker Discussion Question

Two wave pulses on a string approach each other at speeds of 1 m/s. How does the string look at $t = 3$ s?



Particles and Waves

- Particles cannot occupy the same space. They **collide**.



- Waves pass right through each other. They **interfere**.



[Animations from <http://www.physicsclassroom.com/mmedia/newtlaws/mb.cfm> and <http://www.acs.psu.edu/drussell/demos/superposition/superposition.html>]

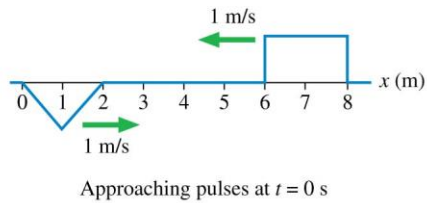
The Principle of Superposition

If two or more waves combine at a given point, the resulting disturbance is the *sum* of the disturbances of the individual waves.

$$D = D_1 + D_2$$

i-Clicker Discussion Question

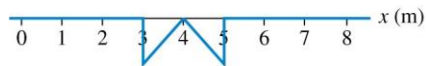
Two wave pulses on a string approach each other at speeds of 1 m/s. How does the string look at $t = 3$ s?



A.



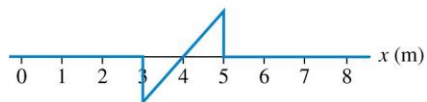
C.



B.



D.



Reflection of Transverse Wave Pulse



- A pulse traveling to the right on a heavy string attached to a lighter string
- Speed suddenly increases

[Animation courtesy of Dan Russell, Penn State]

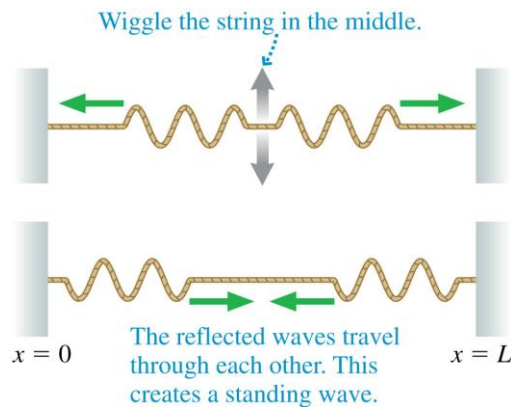
Reflection of Transverse Wave Pulse



- A pulse traveling to the right on a light string attached to a heavier string
- Speed suddenly decreases

[Animation courtesy of Dan Russell, Penn State]

Standing Waves on a String



Reflections at the ends of the string cause waves of *equal amplitude and wavelength* to travel in opposite directions along the string, which results in a standing wave.

The Mathematics of Standing Waves

According to the principle of superposition, the net displacement of a medium when waves with displacements D_R and D_L are present is

$$D(x, t) = D_R + D_L = a \sin(kx - \omega t) + a \sin(kx + \omega t)$$

We can simplify this by using a trigonometric identity, and arrive at:

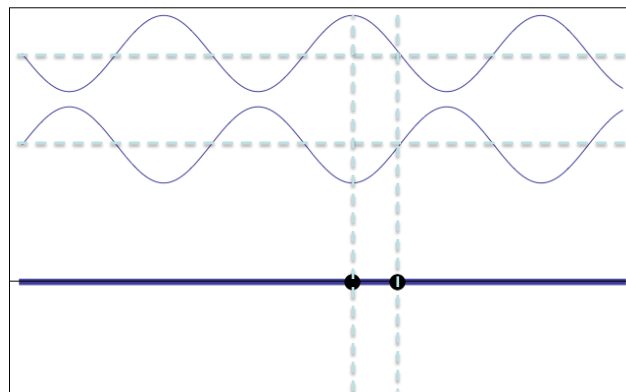
$$D(x, t) = A(x) \cos(\omega t)$$

where $A(x) = 2a \sin(kx)$

For a standing wave, the pattern is not propagating!

Standing Wave:

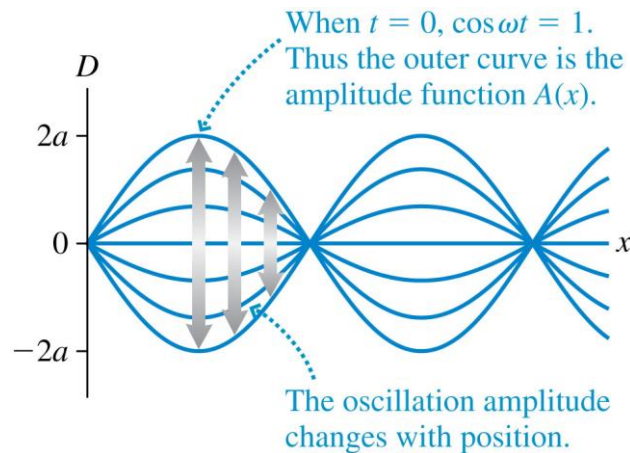
The superposition of two 1-D sinusoidal waves traveling in opposite directions.



[Animation courtesy of Dan Russell, Penn State]

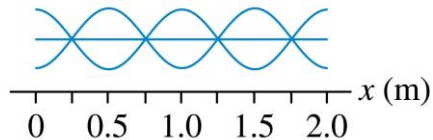
The Mathematics of Standing Waves

The amplitude reaches a maximum value of $A_{\max} = 2a$ at points where $\sin(kx) = 1$.



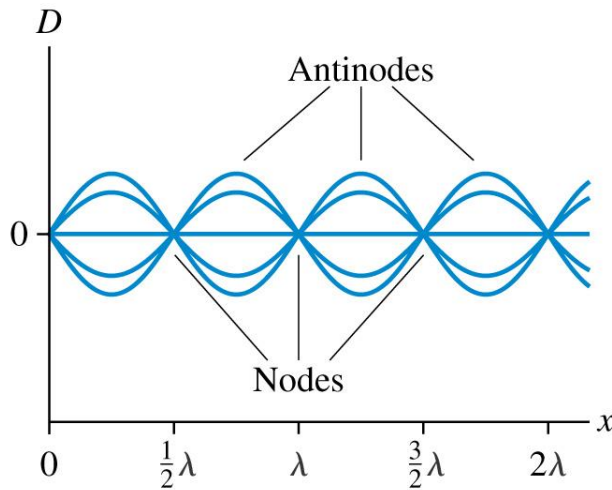
i-Clicker Discussion Question

What is the wavelength of this standing wave?



- A. 0.25 m.
- B. 0.5 m.
- C. 1.0 m.
- D. 2.0 m.
- E. Standing waves don't have a wavelength.

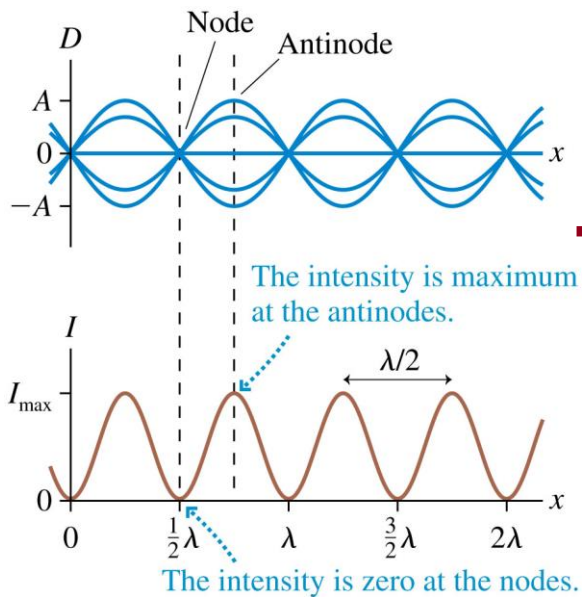
Node Spacing on a String



The nodes and antinodes are spaced $\lambda/2$ apart.

Copyright © 2004 Pearson Education, Inc., publishing as Addison Wesley

Standing Waves



- In Chapter 20 you learned that the *intensity* of a wave is proportional to the square of the amplitude: $I \propto A^2$.
- Intensity is maximum at points of constructive interference and zero at points of destructive interference.

Standing Waves in a Microwave Oven

- Microwaves are electromagnetic waves, which travel at the speed of light.
- I removed the turntable from my microwave oven, and poured egg whites into a flat plate



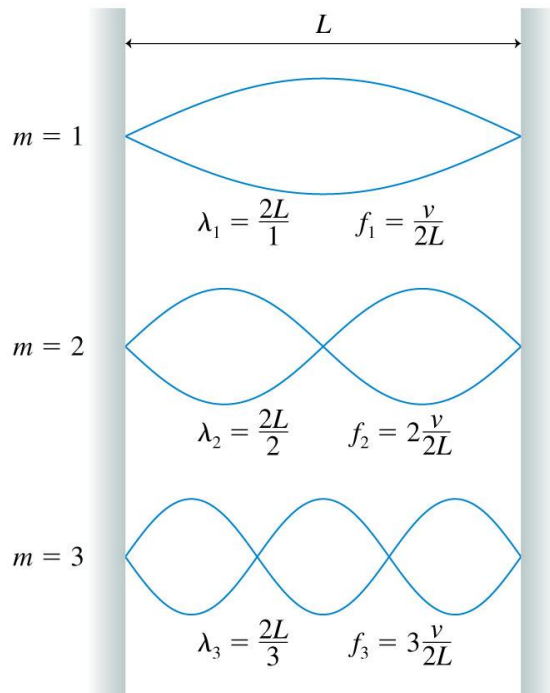
Standing Waves in a Microwave Oven

- The egg whites heat faster around the edges. This is because the microwaves attenuate as they travel through the egg.
- There also is a pattern of “hot spots”. These are antinodes in 3-dimensional standing wave pattern



Standing Waves in a Microwave Oven

- I measured the distance between antinodes to be about $6 \text{ cm} \pm 1 \text{ cm}$
- This should be about $\lambda/2$, so $\lambda = 12 \text{ cm} \pm 2 \text{ cm}$
- My microwave manual says in specifications that its cooking frequency is 2450 MHz



On a string of length L with fixed end points,
 $D(0, t) = 0$ and $D(L, t) = 0$

Only oscillations with specific wavelengths are allowed.

i-Clicker Discussion Question

What is the mode number of this standing wave?



- A. 4.
- B. 5.
- C. 6.
- D. Can't say without knowing what kind of wave it is.

Standing Waves on a String

There are three things to note about the normal modes of a string.

1. m is the number of *antinodes* on the standing wave.
2. The *fundamental mode*, with $m = 1$, has $\lambda_1 = 2L$.
3. The frequencies of the normal modes form a series: $f_1, 2f_1, 3f_1, \dots$. These are also called **harmonics**. $2f_1$ is the “second harmonic”, $3f_1$ is the “third harmonic”, etc.

Musical Instruments

- Instruments such as the harp, the piano, and the violin have strings fixed at the ends and tightened to create tension.
- A disturbance generated on the string by plucking, striking, or bowing it creates a **standing wave** on the string.
- The fundamental frequency is the musical note you hear when the string is sounded:



$$f_1 = \frac{v}{2L} = \frac{1}{2L} \sqrt{\frac{T_s}{\mu}}$$

where T_s is the tension in the string and μ is its linear density.

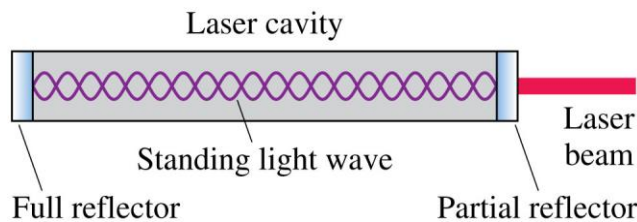
i-Clicker Discussion Question

The frequency of the third harmonic of a string is

- A. One-third the frequency of the fundamental.
- B. Equal to the frequency of the fundamental.
- C. Three times the frequency of the fundamental.
- D. Nine times the frequency of the fundamental.

Standing Electromagnetic Waves

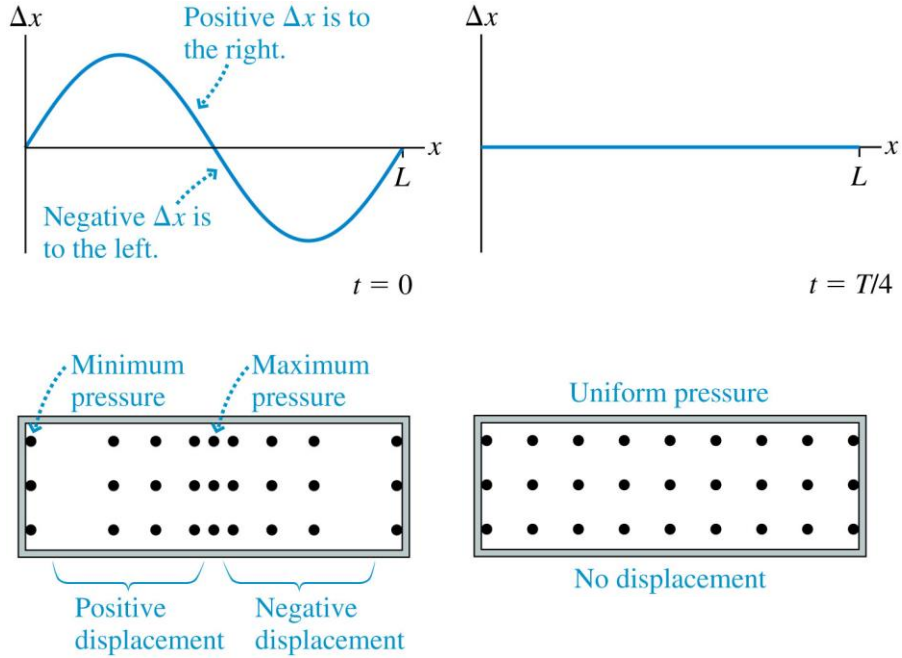
- Standing electromagnetic waves can be established between two parallel mirrors that reflect light back and forth.
- A typical laser cavity has a length $L \approx 30$ cm, and visible light has a wavelength $\lambda \approx 600$ nm.
- The standing light wave in a typical laser cavity has a mode number m that is $2L/\lambda \approx 1,000,000!$



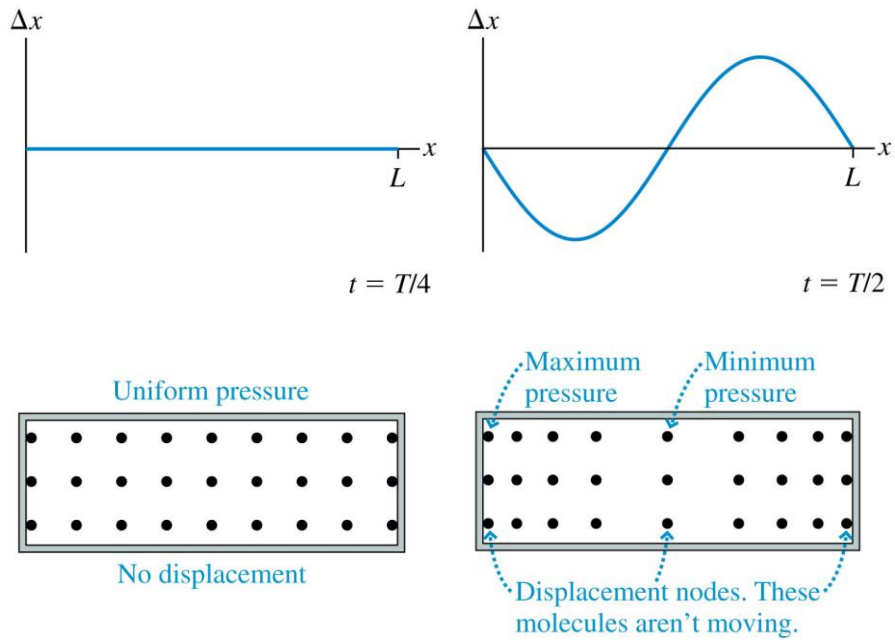
Standing Sound Waves

- A long, narrow column of air, such as the air in a tube or pipe, can support a longitudinal standing sound wave.
- A closed end of a column of air must be a displacement node. Thus the boundary conditions — nodes at the ends — are the same as for a standing wave on a string.
- It is often useful to think of sound as a pressure wave rather than a displacement wave. The pressure oscillates around its equilibrium value.
- The nodes and antinodes of the pressure wave are interchanged with those of the displacement wave.

Standing Sound Waves



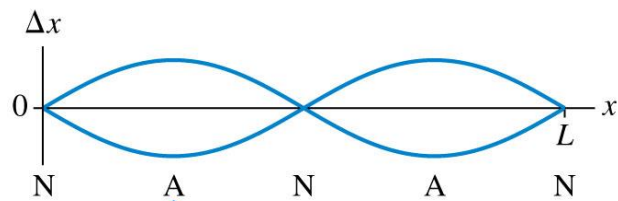
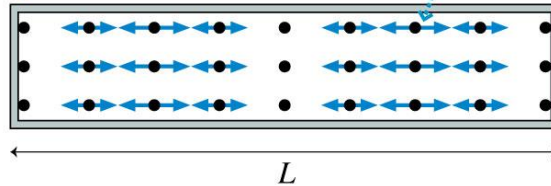
Standing Sound Waves



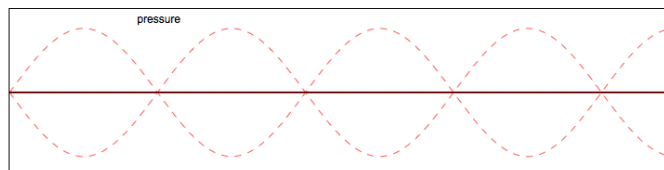
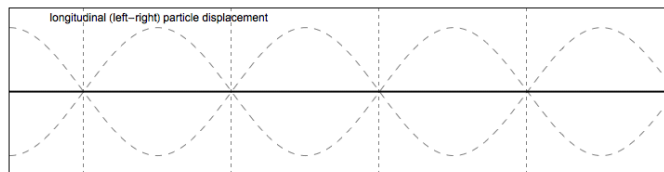
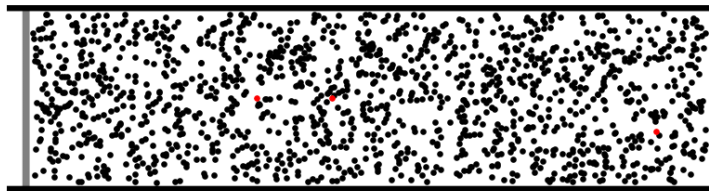
- Displacement Δx and pressure graphs for the $m = 2$ mode of standing sound waves in a closed-closed tube.
- The nodes and antinodes of the pressure wave are interchanged with those of the displacement wave.

The closed end is a displacement node and a pressure antinode.

Air molecules undergo longitudinal oscillations. This is a displacement antinode and a pressure node.

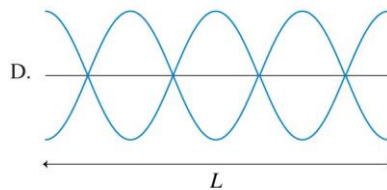
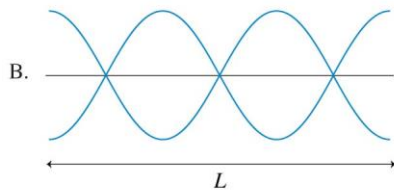
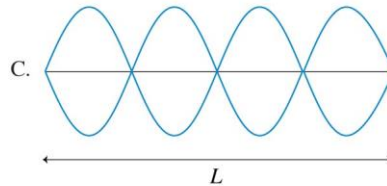
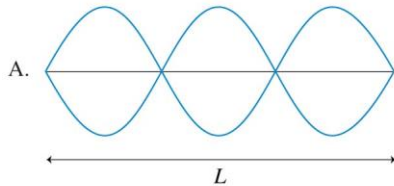
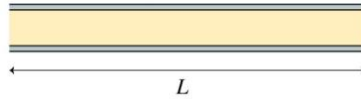


The displacement and pressure nodes



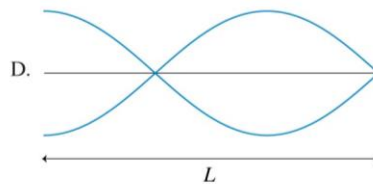
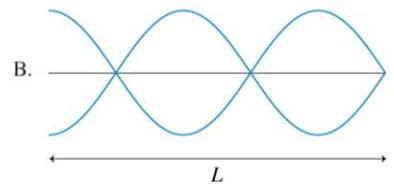
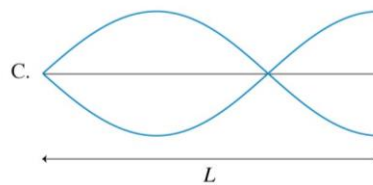
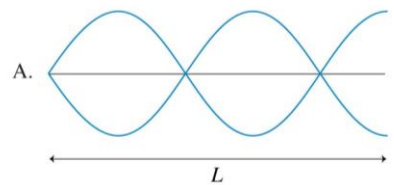
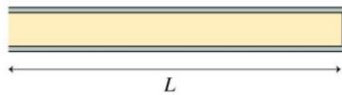
i-Clicker Discussion Question

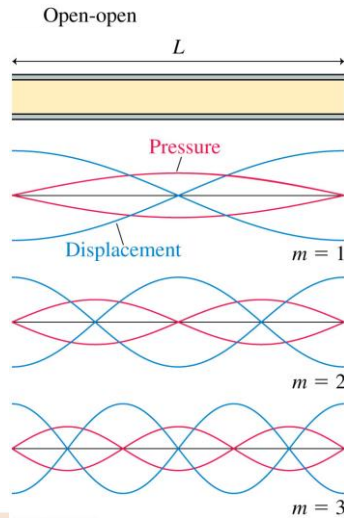
An open-open tube of air has length L . Which is the displacement graph of the $m = 3$ standing wave in this tube?



i-Clicker Discussion Question

An open-closed tube of air of length L has the closed end on the right. Which is the displacement graph of the $m = 3$ standing wave in this tube?

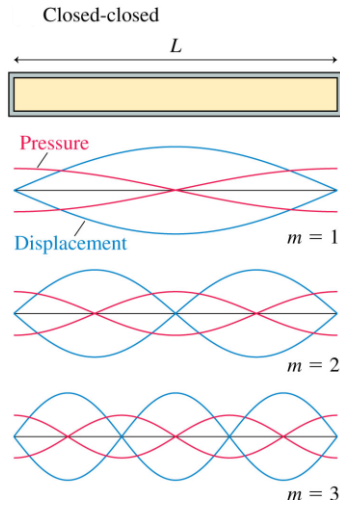




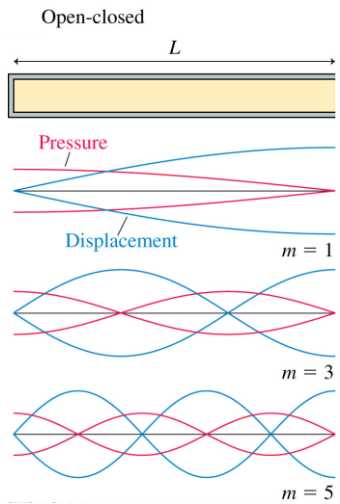
$$\begin{cases} \lambda_m = \frac{2L}{m} \\ f_m = m \frac{v}{2L} = mf_1 \end{cases} \quad \begin{array}{l} m = 1, 2, 3, 4, \dots \\ \text{(open-open or closed-closed tube)} \end{array}$$

Example from a past test

A metal pipe, open at both ends, can create a standing wave in the second harmonic with a frequency of 483 Hz. What is the length of the pipe?



$$\begin{cases} \lambda_m = \frac{2L}{m} \\ f_m = m \frac{v}{2L} = mf_1 \end{cases} \quad \begin{array}{l} m = 1, 2, 3, 4, \dots \\ \text{(open-open or closed-closed tube)} \end{array}$$



$$\begin{cases} \lambda_m = \frac{4L}{m} \\ f_m = m \frac{v}{4L} = mf_1 \end{cases} \quad \begin{array}{l} m = 1, 3, 5, 7, \dots \\ \text{(open-closed tube)} \end{array}$$

Musical Instruments

- With a wind instrument, blowing into the mouthpiece creates a standing sound wave inside a tube of air.
- The player changes the notes by using her fingers to cover holes or open valves, changing the length of the tube and thus its fundamental frequency:

$$f_1 = \frac{v}{2L} \quad \text{for an open-open tube instrument, such as a flute}$$

$$f_1 = \frac{v}{4L} \quad \text{for an open-closed tube instrument, such as a clarinet}$$

- In both of these equations, v is the speed of sound in the air *inside* the tube.
- Overblowing wind instruments can sometimes produce higher harmonics such as $f_2 = 2f_1$ and $f_3 = 3f_1$.

i-Clicker Discussion Question

At room temperature, the fundamental frequency of an open-open tube is 500 Hz. If taken outside on a cold winter day, the fundamental frequency will be

- A. Less than 500 Hz.
- B. 500 Hz.
- C. More than 500 Hz.

Before Class 4 on Wednesday

- Please read Knight Ch. 21, sections 21.5-21.8 (finish the chapter)
- Please do the short pre-class quiz on MasteringPhysics by Tuesday evening.
- Something to think about: What is “constructive interference”? How can you interfere with something and **increase** its strength?

