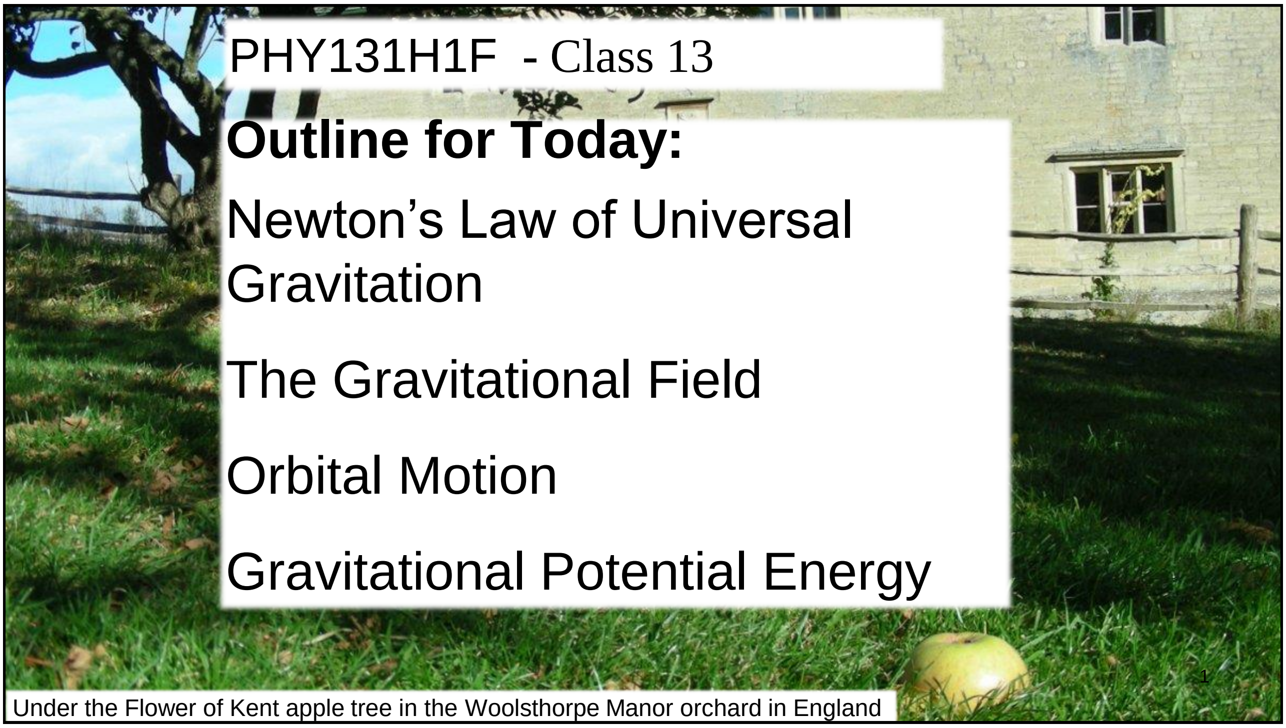


PHY131H1F - Class 13

Outline for Today:

Newton's Law of Universal Gravitation

The Gravitational Field

Orbital Motion

Gravitational Potential Energy

1

Under the Flower of Kent apple tree in the Woolsthorpe Manor orchard in England

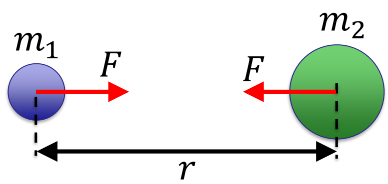
Hello!

- My name is Jason Harlow, and I'll be your physics teacher for the rest of this semester.
- I graduated from U of T with a Specialist in Physics and Astronomy in 1993
- I got my Ph.D. in Astronomy and Astrophysics from Penn State University in 2000
- I've been a Teaching Faculty here at U of T since 2004.
- I have a lot of kids, I am a Muslim, I play hockey and I ride my bike to work.
- Brian said he finished up chapters 1-7, so, today I'll start in with Chapter 8 on Universal Gravitation

2

Gravity

It was Newton who first recognized that **gravity is an attractive, long-range force between *any* two objects.**



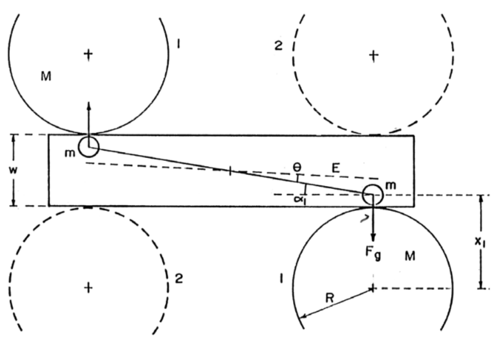
When two objects have masses m_1 and m_2 and centers are separated by distance r, each object attracts the other with a force given by Newton's law of gravity, as follows:

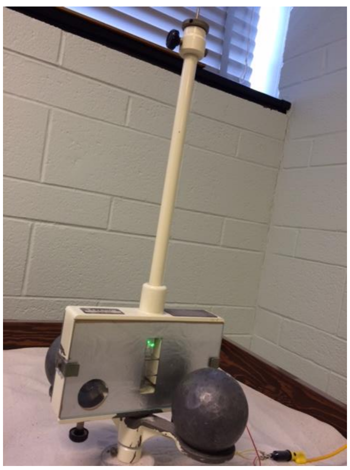
where $G = 6.67 \times 10^{-11}\ \mathrm{N\ m^2\ kg^{-2}}$ is the Gravitational constant (the same everywhere in the universe).

3

Cavendish Experiment

Done in second year labs (PHY224H1).





You end up measuring a force of about 10^{-8} N (10 nano-Newtons!) which is equivalent to the weight of 0.1 μg.

But it is doable in less than 2 weeks.

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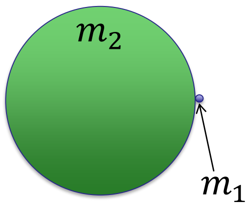
Gravity Example

A mass, m_1, sits at the surface a giant spherical rock which is floating in space.

The giant rock has a mass of $m_2 = 6 \times 10^{24}$ kg and a radius of 6400 km.

(a) What is the force of gravity on the mass due to the giant rock, in terms of m_1?

(b) Can you think of a good name for this giant rock?



Gravity for Earthlings

If you happen to live on the surface of a large planet with radius R and mass M, you can write the gravitational force more simply as:

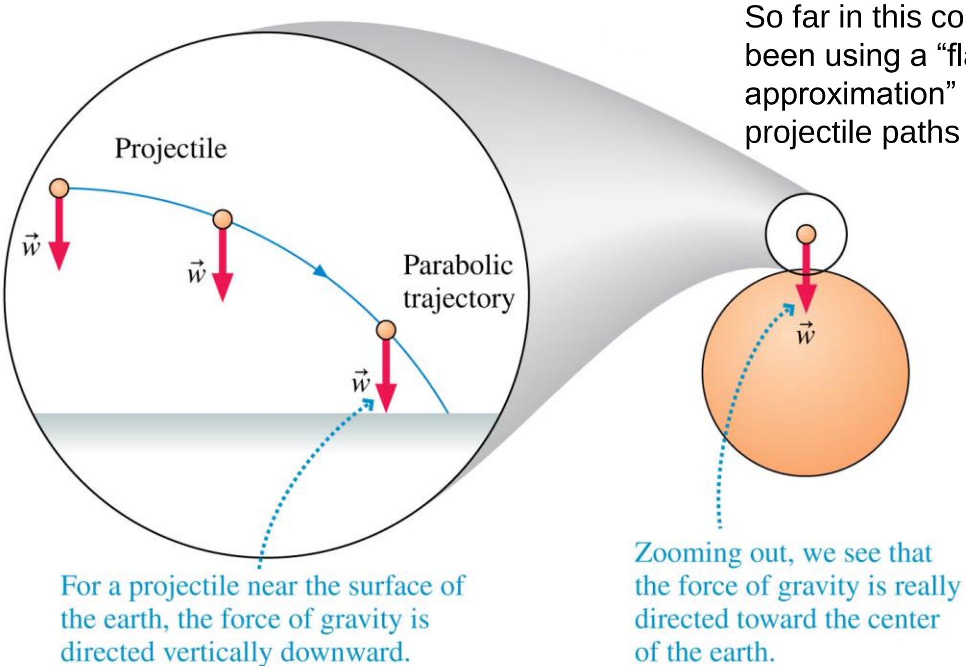
$$\vec{F}_{\mathrm{G}} = (mg, \text{straight down}) \qquad \text{(gravitational force)}$$

where the quantity g is defined to be:

$$g = \frac{GM}{R^2}$$

At sea level, $g = 9.83\ \mathrm{m/s^2}$.
At 39 km altitude, $g = 9.71\ \mathrm{m/s^2}$.

So far in this course, we have been using a "flat earth approximation" in which projectile paths are parabolas.



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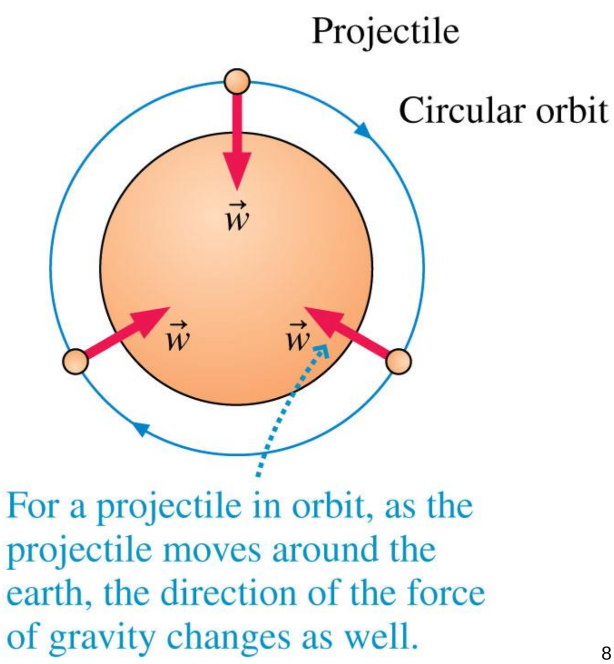
Orbital Motion

- If the launch speed of a projectile is sufficiently large, there comes a point at which the curve of the trajectory and the curve of the earth are parallel.
- Such a *closed trajectory* is called an **orbit**.
- An orbiting projectile is in **free fall.**



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Learning Catalytics Question 1

- Astronaut Randy Bresnik (Twitter @AstroKomrade) is currently living on the International Space Station, which orbits at 370 km above the surface of the Earth (low earth orbit).
- Assuming Randy has not changed his mass since moving to space, what is the force of gravity on Randy?

A. Zero
B. The same as the force of gravity on him while he was on earth.
C. A little bit less than the force of gravity on him while he was on earth.
D. Not exactly zero, but much, much less than the force of gravity on him while he was on earth.

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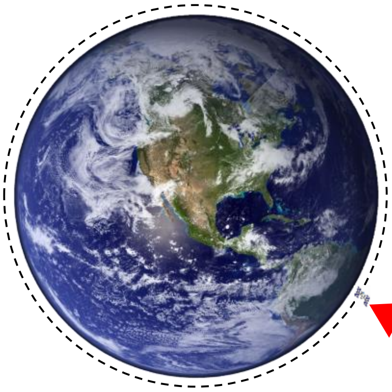
International Space Station

Orbit is drawn **to scale**



Randy ***feels*** weightless because he is in freefall!

Radius of the Earth: 6400 km, $g = 9.8\ \text{m/s}^2$

Altitude of Space Station: 370 km, $g = 8.9\ \text{m/s}^2$ (about 10% less)

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Example

How fast would you have to drive in order to be "weightless" – ie, no normal force needed to support your car?

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Circular Orbits

An object moving in a circular orbit of radius r at speed v_{orbit} will have centripetal acceleration of

$$a_r = \frac{(v_{\text{orbit}})^2}{r} = g$$

That is, if an object moves parallel to the surface with the speed

$$v_{\text{orbit}} = \sqrt{rg}$$

then the free-fall acceleration provides exactly the centripetal acceleration needed for a circular orbit of radius r.

Near the surface of the Earth, this speed is about 8 km/s.

An object with any other speed will not follow a circular orbit.

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Learning Catalytics Question 2

It costs upwards of $100 million to launch a communications satellite. What is the main reason why big companies do this?

A. To get outside Earth's gravitational pull so the satellite doesn't fall down
B. To get closer to the Sun in order to collect more solar power
C. To get away from air resistance so they can move fast and not burn up
D. To get away from radio interference on Earth
E. To get far enough so they can communicate with the entire Earth at one time

Circular Satellite Orbits

- Positioning: beyond Earth's atmosphere, where air resistance is almost totally absent
- Example: Low-earth orbit communications satellites are launched to altitudes of 150 kilometers or more, in order to be above air drag
- But even the ISS, as shown, experiences *some* air drag, which is compensated for with periodic upward boosts.

The state of physics around 1650…

- In 1609 Galileo started observing the sky with a telescope.
- Around that same time, Kepler was investigating careful observations of the apparent positions of planets in the sky.
- It was determined that planets orbit the Sun, and that Earth was the third planet out from the Sun.
- Kepler noted that the shapes of the orbits of all the planets were not quite circles, but actually ellipses.

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How to draw an Ellipse

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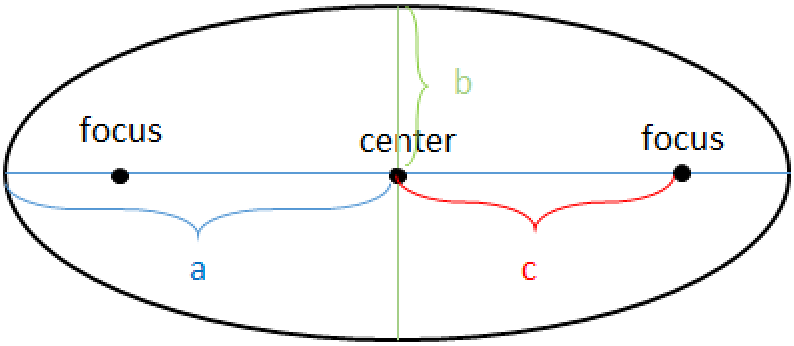
An ellipse is a mathematical shape.

- The furthest distance from the centre of an ellipse to its edge is called the "semi-major axis" a.
- The eccentricity, $e = c/a$, tells you how squished the orbit is.
- A circle is a special case of an ellipse, when $e = 0$.



$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

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Kepler's Laws of Planetary Motion

1. Planets, asteroids and comets move in orbits whose shapes are ellipses, with the sun at one focus of the ellipse. (Planetary orbits normally have low eccentricity: almost circular.)
2. A line drawn between the sun and a planet sweeps out equal areas during equal intervals of time. (They go faster when they are closer to the sun.)
3. The square of a planet's orbital period is proportional to the cube of the semimajor-axis length. ($T^2 = C\, r^3$, where C is some constant.)

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Newton's Laws

• Kepler's Laws are empirical, like Hooke's Law, or the equation for kinetic friction or drag. They were written down in order to describe the observations. Kepler did not know "why" the planets moved in this way.

• Many scientists at the time, including Edmund Halley, believed that there was some kind of force from the Sun pulling the planets, asteroids and comets toward it.

• In 1687 Isaac Newton published one simple theory which explained all of Kepler's laws, as well as motion observed here on Earth:

  • The 3 Newton's Laws you already learned, plus:
  • "Newton's Law of Gravity"

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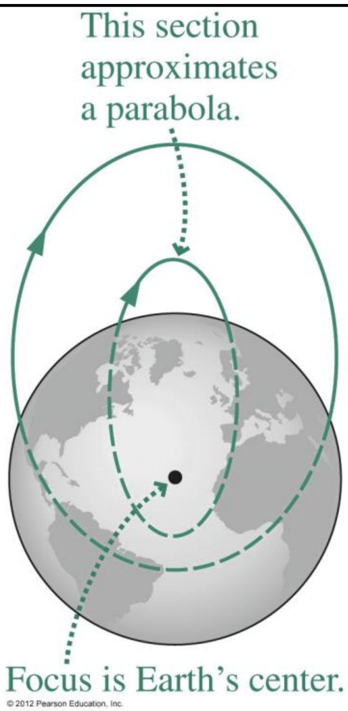
Projectile Motion and Orbits

- The "parabolic" trajectories of projectiles near Earth's surface are actually sections of elliptical orbits that intersect Earth.
- The trajectories are parabolic only in the approximation that we can neglect Earth's curvature and the variation in gravity with distance from Earth's center.



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Gravitational Potential Energy

When two isolated masses m_1 and m_2 interact over large distances, they have a gravitational potential energy of

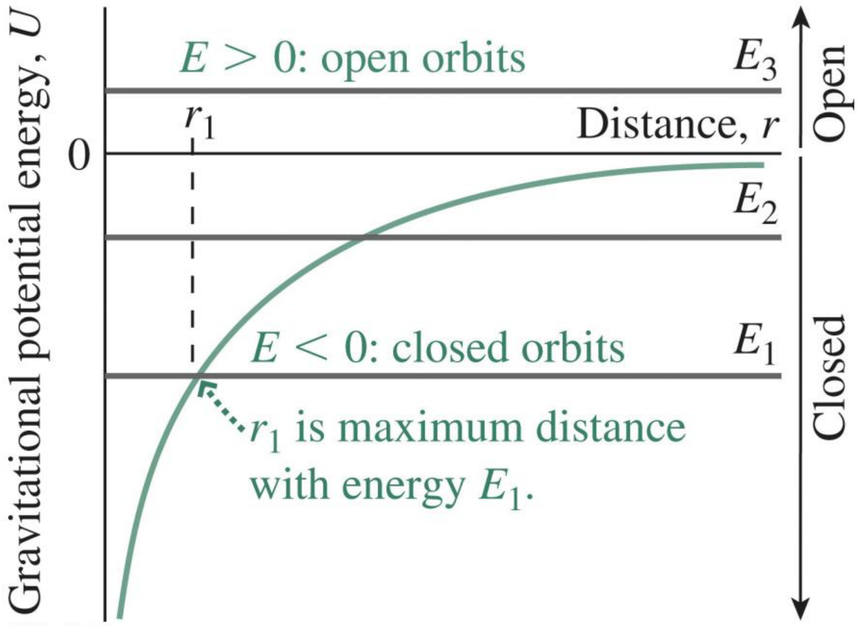
where we have chosen the zero point of potential energy at $r = \infty$, where the masses will have no tendency, or potential, to move together.

Note that this equation gives the potential energy of masses m_1 and m_2 when their *centers* are separated by a distance r.

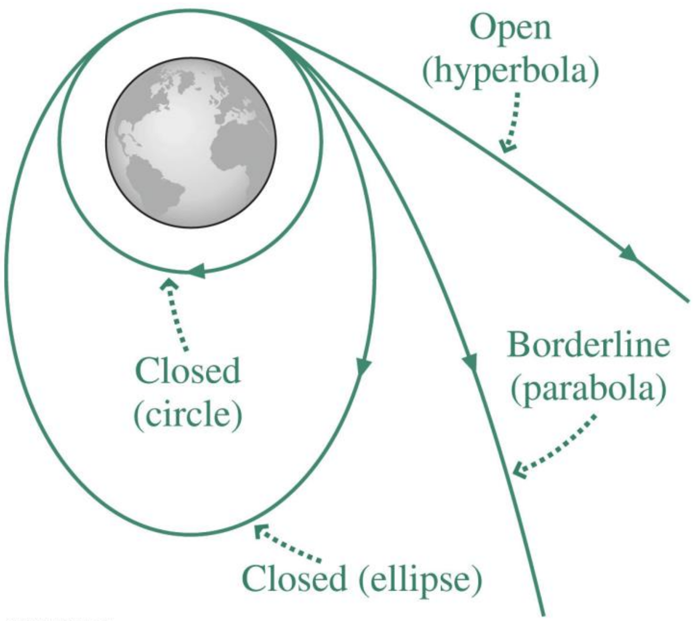
Energy and Orbits

- By our definition of zero point at infinity, U is always negative.
- K is always positive.
- The sign of the total energy $E = K + U$ determines the type of orbit an object:
- $E < 0$: The object is in a bound, elliptical orbit.
  - Special cases include circular orbits and the straight-line paths of falling objects.
- $E > 0$: The orbit is unbound and hyperbolic.
- $E = 0$: The borderline case gives a parabolic orbit.

Energy and Orbits



Energy and Orbits



- There is a saying, “What goes up must come down.” Is this always true? How fast must you throw an object upwards so that it *never* comes down?
- ANSWER:
- When the total energy = 0, then, as r approaches infinity, K will approach zero. This is “escape speed”:

Escape speed.

- The escape speed near the Earth’s surface is about 11 km/s.
- If the Earth’s radius was less than 9 mm, then the escape speed would be greater than 300,000 km/s, which is greater than the speed of light.
- Since nothing can travel faster than light, nothing would be able to escape the Earth’s surface, and the Earth would be what astronomers call a black hole.

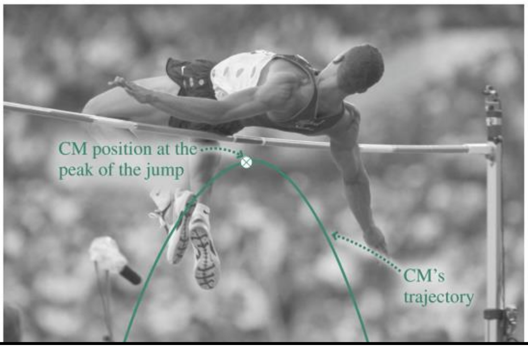
Learning Catalytics Question 3

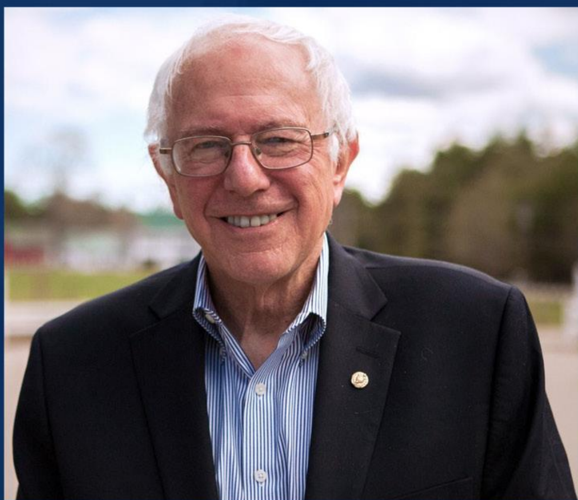
- A moon is orbiting around Planet X. Which of the following statements is always true about its kinetic energy (K), and its gravitational potential energy (U)?

A. $K < 0$ and $U < 0$
B. $K < 0$ and $U > 0$
C. $K > 0$ and U < 0
D. $K > 0$ and U > 0
E. $K < 0$ and U $= 0$

Before Class 14 on Monday

- Remember MasteringPhysics.com **Homework 6** on Ch.7 is due Monday by 11:59pm.
- Please read the first two sections of Chapter 9 on Center of Mass and Conservation of Momentum
- Something to think about:
- How is it possible to clear the bar in a high jump if your center of mass does not reach to the height of the bar?





US Senator Bernie Sanders

WHAT THE U.S. CAN LEARN FROM CANADIAN HEALTH CARE

Sunday October 29, 2017 | 11am
Live at the University of Toronto
& by webcast