

1. a)

$$y(x, t) = A \sin\left(\frac{2\pi}{\lambda}(x - vt)\right)$$

$$\lambda = \frac{2\pi}{k} = \frac{2\pi}{4\pi \text{ m}^{-1}} = 0.5 \text{ m}$$

b)

$$f = \frac{v}{\lambda} = \frac{4 \text{ m/s}}{0.5 \text{ m}} = 8 \text{ Hz}$$

c)

$v = 4 \text{ m/s}$ in the positive x direction

2. a)

$$\lambda = 4L = (4)(2.4 \text{ m}) = 9.6 \text{ m}$$

$$f = \frac{v}{\lambda} = \frac{343 \text{ m/s}}{9.6 \text{ m}} = 35.7 \text{ Hz}$$

b)

The beat produced is at 0.7 Hz, so $f_{beat} = 0.7 \text{ Hz} = |f_{organ} - f_{fork}|$

$$f_{organ} = f_{fork} \pm 0.7 \text{ Hz} = 391.3 \text{ Hz or } 392.7 \text{ Hz}$$

Dividing these by the fundamental frequency of the organ we get $n = 10.96$ and $n = 11$

So the beat is caused by the 11th harmonic of the organ

3. The car emits the sound traveling at $v = 24 \text{ km/h} = 6.67 \text{ m/s}$ towards the wall. It is then reflected back towards the car, so the shift is:

$$f = \left(\frac{c + v_r}{c + v_s}\right) f_0$$

$$f = \left(\frac{(343 + 6.67) \text{ m/s}}{(343 - 6.67) \text{ m/s}}\right) (250 \text{ Hz}) = 259.9 \text{ Hz}$$

So the beat frequency is $259.9 \text{ Hz} - 250 \text{ Hz} = 9.9 \text{ Hz}$

4. a) The background + computer is at 50 dB and the background is at 40 dB. 10 dB difference -> ratio of 10x

b) The headphones are at 85 dB and the background + computer is at 50 dB. 35 dB difference so

$$35 \text{ dB} = 10 \log\left(\frac{I_{headphones}}{I_{computer}}\right)$$

$$\frac{I_{headphones}}{I_{computer}} = 10^{3.5} = 3162$$