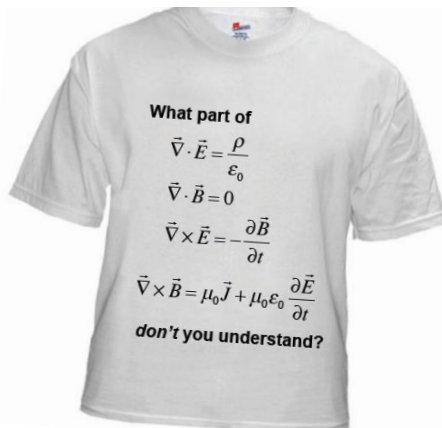
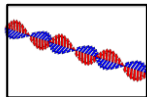


PHY385-H1F Introductory Optics

Class 3 – Outline: Sec. 3.1, 3.2

- Maxwell's Equations in a Vacuum
- Magnetic Field: \vec{B} and Magnetizing Field: \vec{H}
- Intuitive Look at EM waves
- Spherical Waves
- Electromagnetic Waves: speed, general complex-exponential form
- Constraints on the EM-wave imposed by Maxwell's Equations

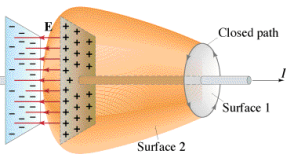


Discussion Question 1

- Ampère's Law is:

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{through}}$$

Where I_{through} is the current passing through a surface, and the loop integral is carried out around a closed path which encircles this surface.



Consider the surfaces shown near a discharging capacitor. What is the current through surface 1?

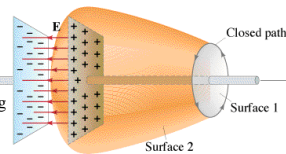
1. $+I$
2. $-I$
3. zero

Discussion Question 2

- Ampère's Law is:

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{through}}$$

Where I_{through} is the current passing through a surface, and the loop integral is carried out around a closed path which encircles this surface.



Consider the surfaces shown near a discharging capacitor. What is the current through surface 2?

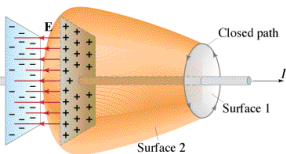
1. $+I$
2. $-I$
3. zero

Discussion Question 3

- Ampère's Law is:

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{through}}$$

Where I_{through} is the current passing through a surface, and the loop integral is carried out around a closed path which encircles this surface.



Consider the loop integral of B around the closed path shown.

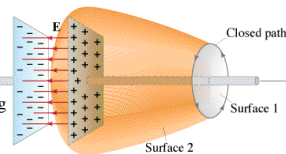
1. The loop integral is non-zero when considering Surface 1, but zero when considering Surface 2.
2. The loop integral is non-zero when considering Surface 2, but zero when considering Surface 1.
3. The loop integral should be the *same* no matter what surface you consider.

Discussion Question 4

- Ampère's Law is:

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{through}}$$

Where I_{through} is the current passing through a surface, and the loop integral is carried out around a closed path which encircles this surface.



How can Ampère's Law be applied to this situation?

1. There must be a current through Surface 2 we don't know about.
2. Ampère's Law is incomplete and cannot be applied to this situation.
3. It is not possible to discharge a capacitor in such a way as to introduce current through Surface 1.

Electromagnetic Waves: An intuitive look...

[These following slides have been used in class with the gracious permission of their author, Dr. Lawrence P. Staunton, of Drake University <http://www.drake.edu/artsci/physics/>
I have made a couple of small changes to adapt the slides for my PHY385 course – any errors that result are entirely my fault.]

Maxwell's Equations: Partial Differential Form

Faraday's Induction Law in partial differential form [B is magnetic field in Tesla]:
$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

Gauss's Law – Electric:
$$\vec{\nabla} \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

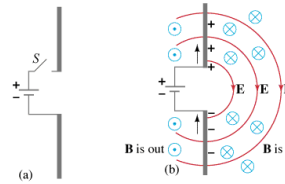
Gauss's Law – Magnetic:
$$\vec{\nabla} \cdot \vec{B} = 0$$

Ampère's Circuital Law [B is magnetic field in Tesla]:
$$\vec{\nabla} \times \vec{B} = \mu \vec{J} + \mu \epsilon \frac{\partial \vec{E}}{\partial t}$$

Electromagnetic Waves

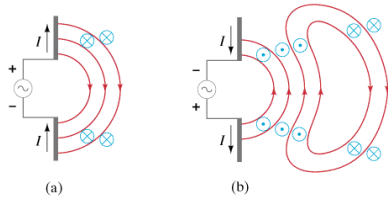
- So, a magnetic field will be produced in space if there is a changing electric field [Ampere's Law, using "displacement current" $d\Phi_E/dt$]
- But, this magnetic field is changing since the electric field is changing [derivative of cosine is sine and vice-versa]
- A changing magnetic field produces an electric field that is also changing [Faraday's Law]
- We have a self-perpetuating system!

Electromagnetic Waves



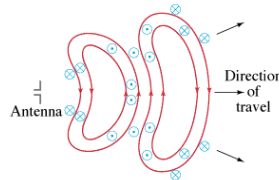
- Close switch and current flows briefly
- Sets up electric field
- Current flow sets up magnetic field as little circles around the wires
- Fields not instantaneous, but form in time
- Energy is stored in fields and cannot move infinitely fast

Electromagnetic Waves

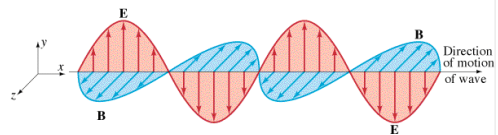


- Picture (a) shows first half cycle
- When current reverses in picture (b), the fields reverse
- See the first disturbance moving outward: These are the electromagnetic waves.

Electromagnetic Waves



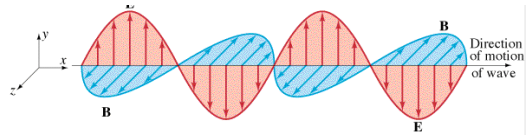
- Notice that the electric and magnetic fields are at right angles to one another
- They are also perpendicular to the direction of motion of the wave



Speed of EM Waves

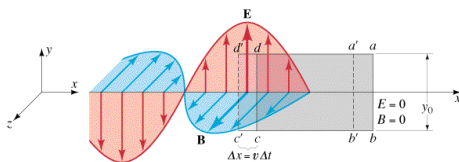
- Now that we have shown how the waves are formed from oscillating charges, we need to see if we can predict how fast they move
- We move far away from the source so that the wave fronts are essentially flat
- Just like dropping a rock in a pond and looking at the waves a few metres away from the impact point

Speed of EM Waves



- This picture defines the coordinate system used in Hecht
- Wave propagates along the x-axis
- The electric field varies in the y-direction and the magnetic field in the z-direction.

Speed of EM Waves



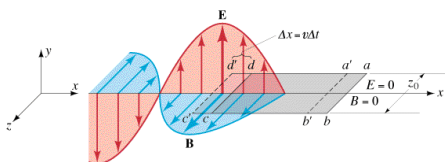
We are going to apply Faraday's Law to the imaginary moving rectangle *abcd*. Compute the magnetic flux change:

$$emf = \frac{\Delta\Phi_B}{\Delta t} = \frac{B\Delta A}{\Delta t} = \frac{By_0v\Delta t}{\Delta t} = By_0v$$

Speed of EM Waves

- We can say the emf around the loop is the sum of the individual emfs going along each straight line segment in the loop
- We look at the work done in moving a test charge around the loop
- $emf = W/q = Fd/q = Ed$
- $emf = Ey_0 = By_0v$
- $E = Bv$

Speed of EM Waves



Now we are going to look at the change in electric flux. Set a new imaginary rectangle and play the same game as before:

$$\sum B_i \Delta l = \mu_0 \epsilon_0 \frac{\Delta\Phi_E}{\Delta t} = \mu_0 \epsilon_0 \frac{Ez_0v\Delta t}{\Delta t} = \mu_0 \epsilon_0 Ez_0v$$

Speed of EM Waves

$$Bz_0 = \mu_0 \epsilon_0 Ez_0v$$

$$B = \mu_0 \epsilon_0 Ev$$

From before: $E = Bv$

$$B = \mu_0 \epsilon_0 (Bv)v$$

$$1 = \mu_0 \epsilon_0 v^2$$

$$v = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$

$$v = \frac{1}{\sqrt{8.85 \times 10^{-12} \times 4\pi \times 10^{-7}}}$$

$$v = 3 \times 10^8$$