PHY385-H1F Introductory Optics

Class 19 - Outline: 9.1 to 9.3

- Jones Matrices
- Two-slit interference
- Young's 2-slit Experiment
- Temporal and Spatial Coherence
- Fresnel-Arago Laws
- Other wavefront splitting
 interfometers

Notes from Table 8.5 on pg. 375:

•
$$\mathscr{P}$$
- state at -45° $\frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$

- \mathscr{R} state $\frac{1}{\sqrt{2}} \begin{bmatrix} 1\\ -i \end{bmatrix}$
- \mathscr{Q} state $\frac{1}{\sqrt{2}} \begin{bmatrix} 1\\i \end{bmatrix}$

Notes from Table 8.6 on pg. 378:

- Linear Polarizer at –45° $\frac{1}{2} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix}$
- QWP, fast axis along $y e^{i\pi/4} \begin{bmatrix} 1 & 0 \\ 0 & -i \end{bmatrix}$
- QWP, fast axis along $x e^{i\pi/4} \begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}$

Horizontally polarized light with Jones Vector E0 = $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$ first passes through a linear polarizer at 45°, M1, then through a vertical polarizer M2.

SI

$$M1 = \begin{bmatrix} 0.5 & 0.5 \\ 0.5 & 0.5 \end{bmatrix} \qquad M2 = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$$

After passing through M1, the unnormalized Jones vector of the light is

 $\begin{array}{c} 1. & \begin{bmatrix} 0 \\ 0 \end{bmatrix} \\ 2. & \begin{bmatrix} 0 \\ 0.5 \end{bmatrix} \\ 3. & \begin{bmatrix} 0.5 \\ 0 \end{bmatrix} \\ 4. & \begin{bmatrix} 0.5 \\ 0.5 \end{bmatrix} \end{array}$

Horizontally polarized light with Jones Vector E0 = $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$ first passes through a linear polarizer at 45°, M1, then through a vertical polarizer M2.

$$M1 = \begin{bmatrix} 0.5 & 0.5 \\ 0.5 & 0.5 \end{bmatrix} \qquad M2 = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$$

If M1 is removed and the light E0 passes only through M2, the Jones vector of the resulting light is

 $\begin{array}{c} 1. \begin{bmatrix} 0 \\ 0 \end{bmatrix} \\ 2. \begin{bmatrix} 0 \\ 0.5 \end{bmatrix} \\ 3. \begin{bmatrix} 0.5 \\ 0 \end{bmatrix} \\ 4 \end{bmatrix}$

Horizontally polarized light with Jones Vector E0 = $\begin{bmatrix} 1\\0 \end{bmatrix}$ first passes through a linear polarizer at 45°, M1, then through a vertical polarizer M2.

$$M1 = \begin{bmatrix} 0.5 & 0.5 \\ 0.5 & 0.5 \end{bmatrix} \qquad M2 = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$$

What is the correct Jones Matrix for the system?

 $\begin{array}{c} 1. \begin{bmatrix} 0 & 0.5 \\ 0 & 0.5 \end{bmatrix} \\ 2. \begin{bmatrix} 0 & 0 \\ 0.5 & 0.5 \end{bmatrix} \\ 3. \begin{bmatrix} 0.5 & 0 \\ 0.5 & 0 \end{bmatrix} \\ 4. \begin{bmatrix} 0.5 & 0.5 \end{bmatrix} \end{array}$

Horizontally polarized light with Jones Vector E0 = $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$ first passes through a linear polarizer at 45°, M1, then through a vertical polarizer M2. The system matrix is

$$M2 \times M1 = \begin{bmatrix} 0 & 0\\ 0.5 & 0.5 \end{bmatrix}$$

After passing through the system, the unnormalized Jones vector of the light is

$$\begin{array}{c}
1. & \begin{bmatrix} 0 \\ 0 \end{bmatrix} \\
2. & \begin{bmatrix} 0 \\ 0.5 \end{bmatrix} \\
3. & \begin{bmatrix} 0.5 \\ 0 \end{bmatrix} \\
4. & \begin{bmatrix} 0.5 \\ 0.5 \end{bmatrix}$$

Interference Chapter 9, Sections 9.1 to 9.3



Two flashlight beams, each of irradiance I_0 , pass through the same small window of area A. The total irradiance passing through this window at any moment is



3. $2I_0$

4. $4I_0$

Two monochromatic beams of light, each of irradiance I_0 , pass through the same small window of area A. The maximum possible irradiance passing through this window at any moment is

- 1. 0
- $\begin{array}{ccc} 2. & I_0 \\ 3. & 2I_0 \end{array}$
- 4. 4*I*₀

Two monochromatic beams of light, each of irradiance I_0 , pass through the same small window of area A. The minimum possible irradiance passing through this window at any moment is

1.	0
2.	I_0
2	21

3. $2I_0$ 4. $4I_0$

Two types of "coherence"



Temporal Coherence Random fluctuations in the spacing of the wavefronts



Spatial Coherence Random fluctuations in the shape of the wavefronts

Source: http://skullsinthestars.com/2008/09/03/optics-basics-coherence/

A Michelson interferometer



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A Michelson interferometer



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A Young Double Slit Experiment



- When d exceeds a critical value, D, the fringes disappear
- D = "Transverse Coherence Length" for this particular light source
- πD^2 is the "Coherence Area"
- Coherence area for filtered sunlight: A ~ 10^{-2} mm²
- \bullet Coherence area for filtered starlight: A ~ 6 m^2

Source: http://skullsinthestars.com/2008/09/03/optics-basics-coherence/





temporal coherence: random fluctuations in the *spacing* of the wavefronts

spatial coherence: random fluctuations in the *shape* of the wavefronts

• Very monochromatic sources tend to have longer values of coherence time. These are "temporally coherent".

• Light from point-sources tends to have larger values of coherence area. These are "spatially coherent". The larger the angular size of the source, the less spatially coherent it will be.

Source: http://skullsinthestars.com/2008/09/03/optics-basics-coherence/