

PHY131H1F - Class 15

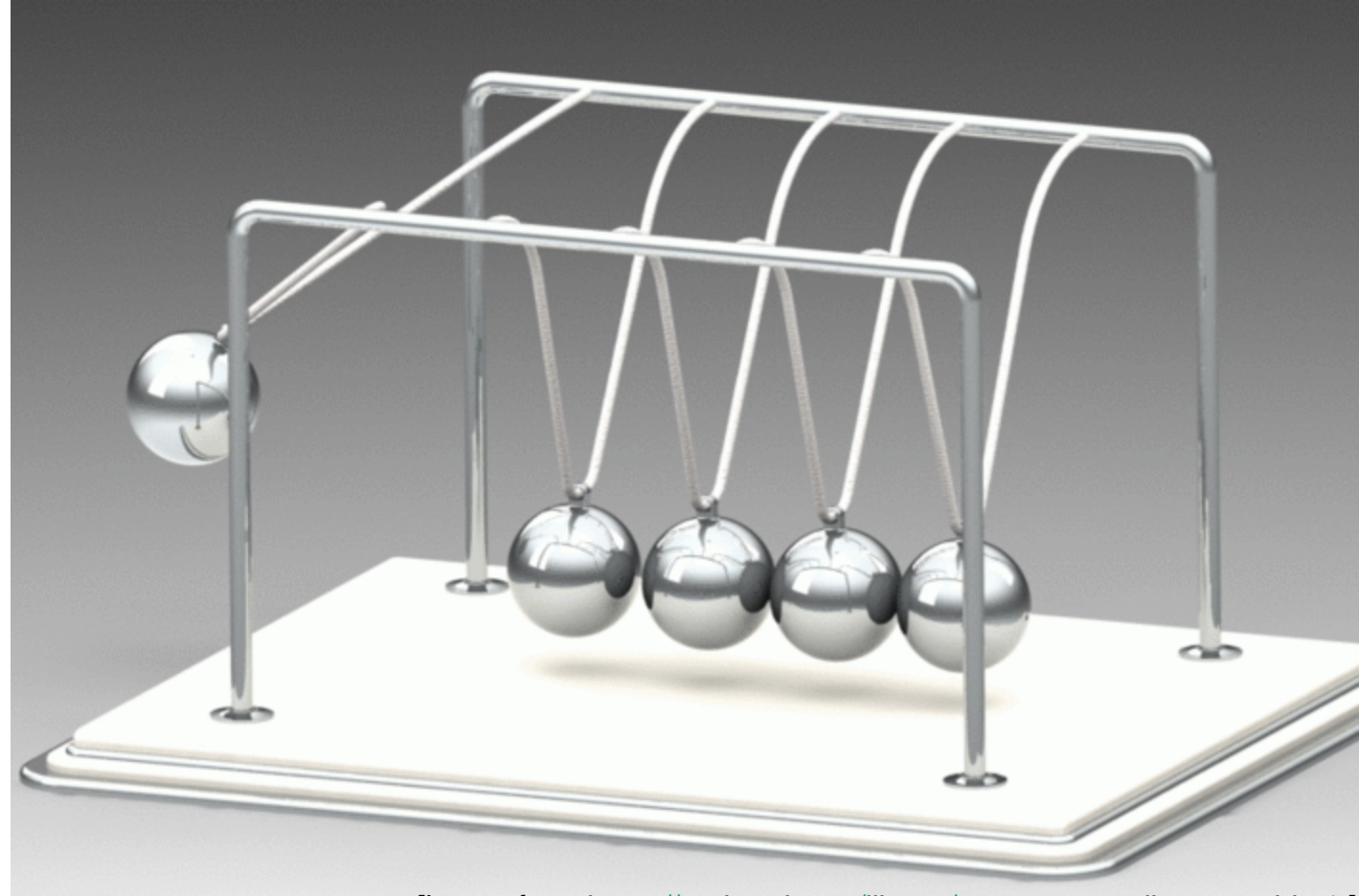
Today, we are finishing Chapter 9 on
Momentum:

Impulse and Momentum

Energy in Collisions

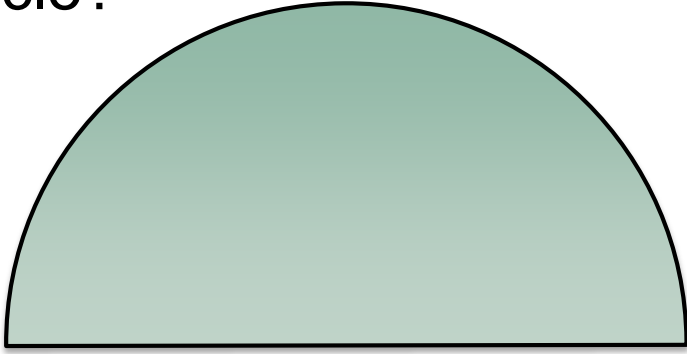
Totally Inelastic Collisions

Elastic Collisions



[image from <https://grabcad.com/library/newton-s-cradle-assembly-1>]

Where is the centre of mass of a solid semicircle?



Last day I asked at the end of class:

- Consider the two integrals below. What's the difference?

$$\vec{J} = \int \vec{F} dt$$

Impulse (Ch.9)

This is the force integrated over **time**, which gives the change in **momentum**.
[Units: kg m / s]

$$W = \int \vec{F} \cdot d\vec{r}$$

Work (Ch. 6)

This is the force integrated over **distance**, which gives the change in **energy**. [Units: Joules]

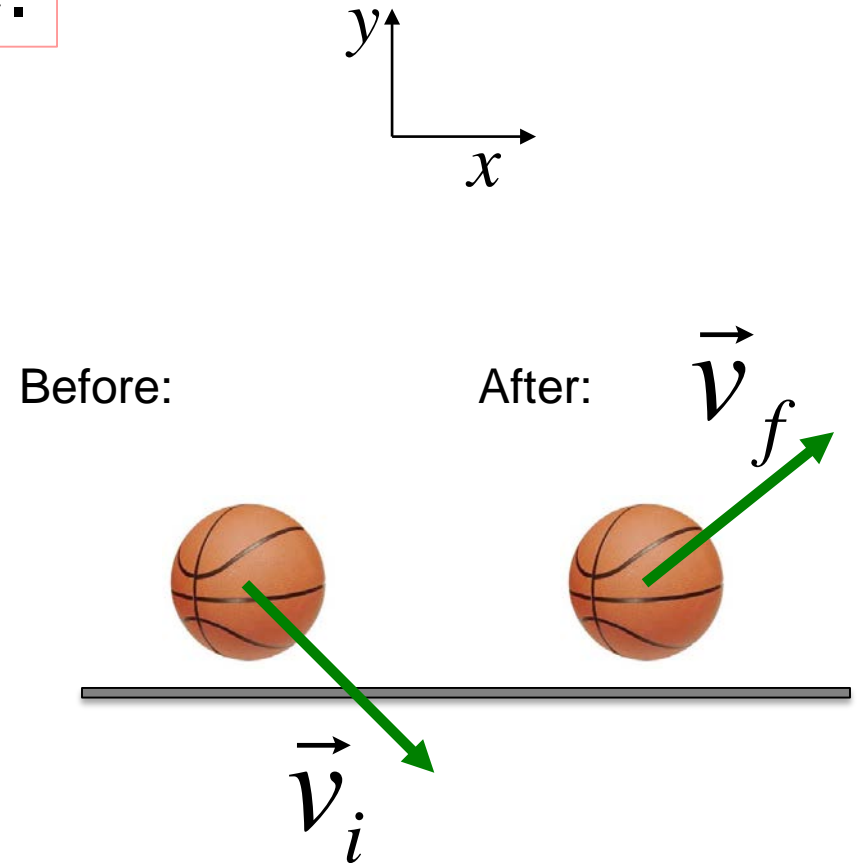
$$\vec{p} = m\vec{v} \text{ means } p_x = mv_x \text{ and } p_y = mv_y.$$

A basketball with mass 0.1 kg is traveling down and to the right with $v_{xi} = +5$ m/s, and $v_{yi} = -5$ m/s.

It hits the horizontal ground, and then is traveling up and to the right with $v_{xf} = +5$ m/s, and $v_{yf} = +4$ m/s.

LC Question 1 What is the change in the x -component of the ball's momentum?

LC Question 2 What is the change in the y -component of the ball's momentum?

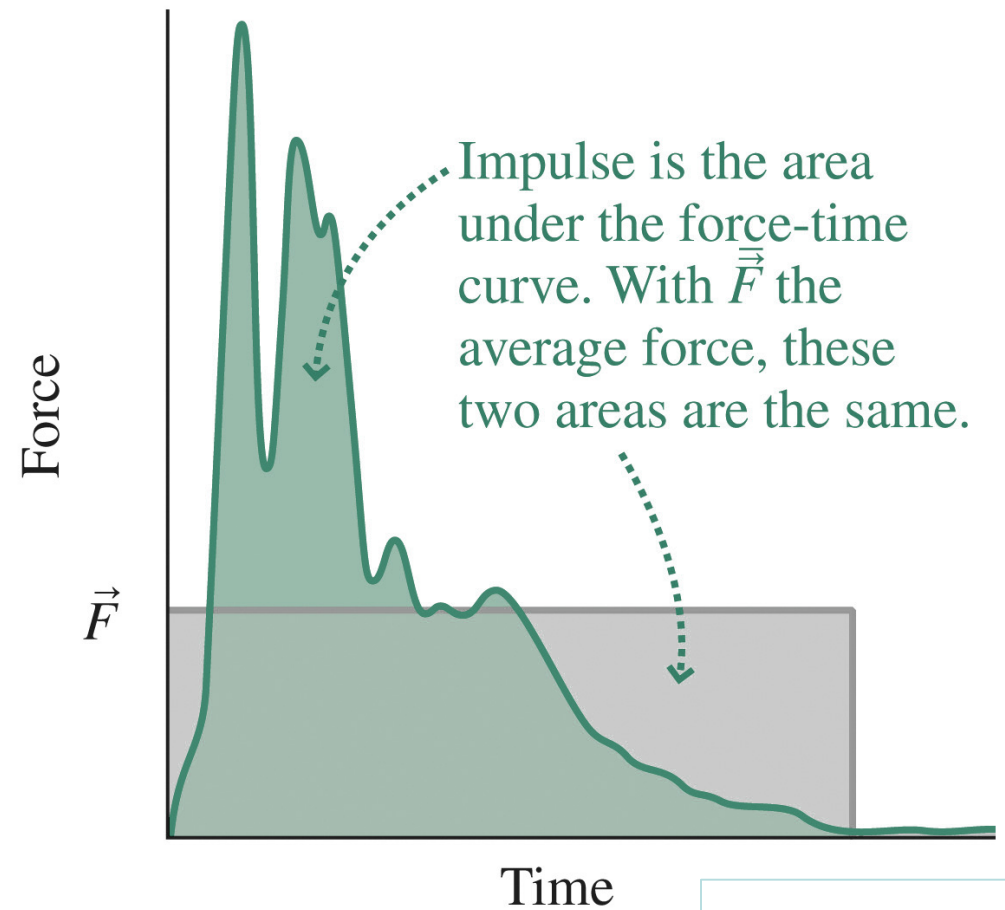


Impulse

The *impulse* upon a particle is:

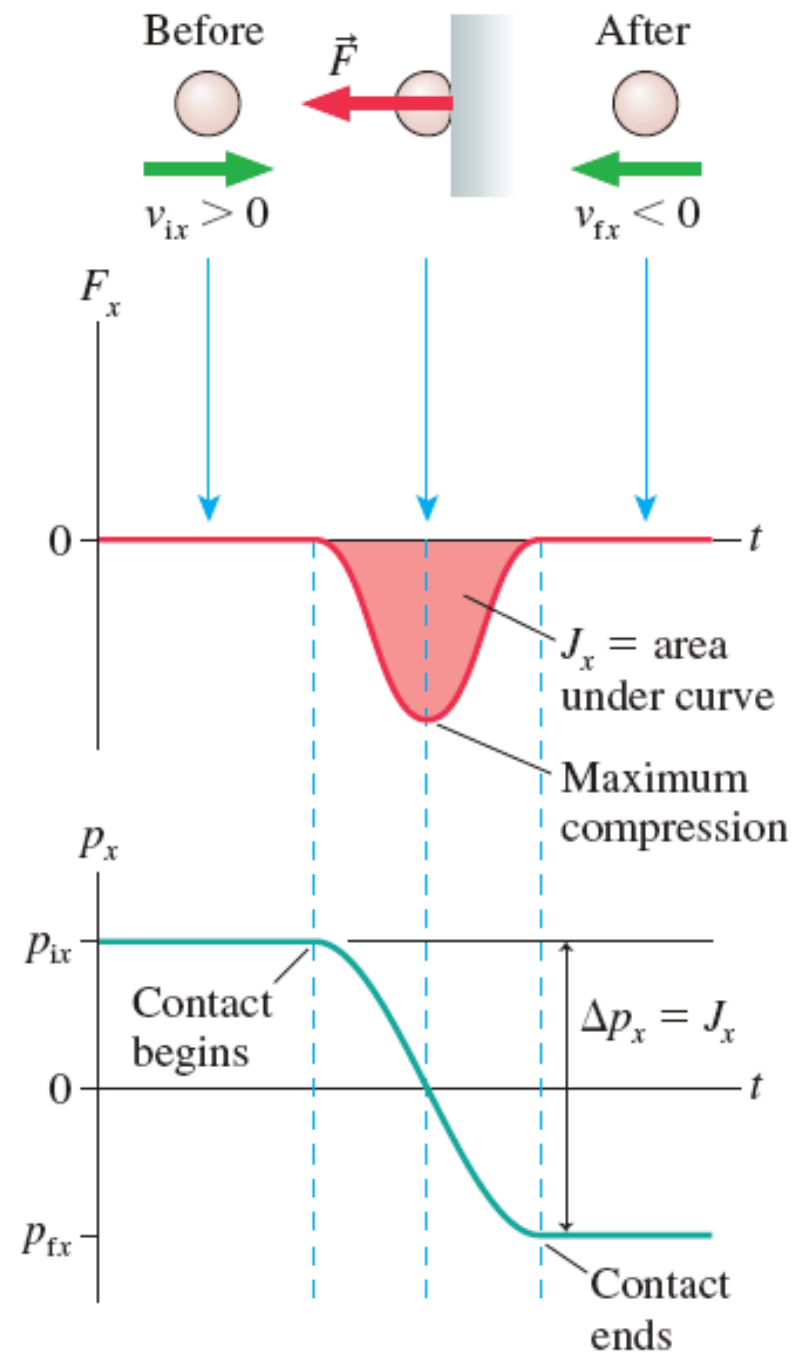
$$J_x = \int_{t_1}^{t_2} F_x dt$$

$$J_y = \int_{t_1}^{t_2} F_y dt$$



- Impulse has units of N s, but you should be able to show that N s are equivalent to kg m/s.
- The **impulse-momentum theorem** states that the change in a particle's momentum is equal to the impulse on it:

$$\Delta p_x = J_x \quad \Delta p_y = J_y$$



A 0.50 kg cart rolls to the right at +1.2 m/s.

It collides with a force sensor.

A plot of force versus time (with positive force defined as towards the right) gives an area of -1.0 N s .

What is the velocity of the cart immediately after the collision?

- Consider a car accident in which a car, initially traveling at 50 km/hr, collides with a large, massive bridge support.
- The car comes to an abrupt stop.
- Why is it better to hit the airbag as opposed to the hard plastic steering wheel or dashboard?
- ANSWER:
- The people must reduce their momentum from mv to zero. This requires a force applied over some amount of time. If the time is very short, the force must be very large (ie hitting steering wheel).
- If the person hits the airbag, this squishes during impact, lengthening the time of the stop. If the stopping process **takes longer**, then the maximum force is **less**.



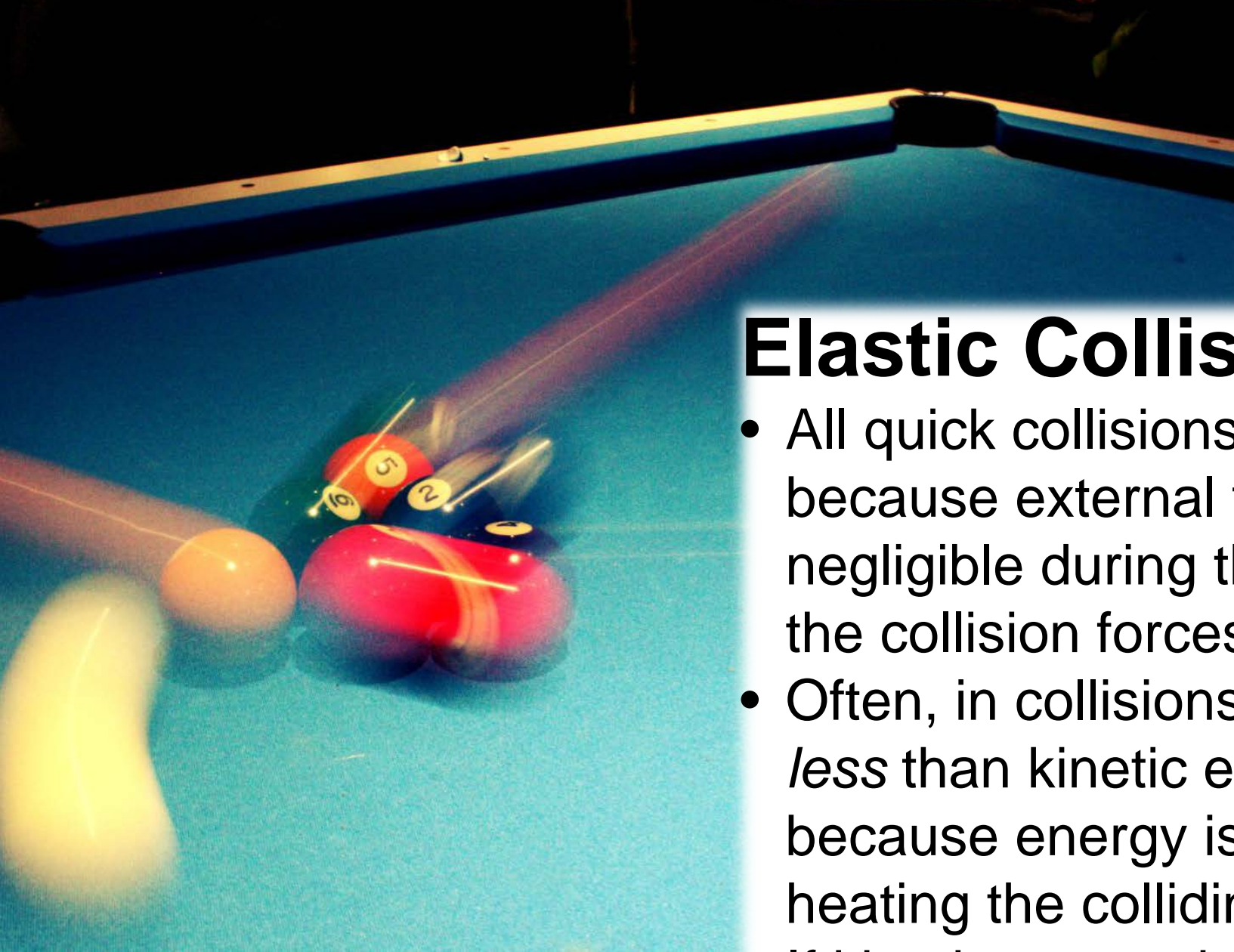
Learning Catalytics Question 3

A 100 g rubber ball and a 100 g damp cloth are dropped on the floor from the same height. They both are traveling at the same speed just before they hit the floor.

The rubber ball bounces, the damp cloth does not.

Which object receives a larger upward impulse from the floor?

- A. They receive equal impulses.
- B. The damp cloth receives a larger impulse.
- C. The rubber ball receives a larger impulse.

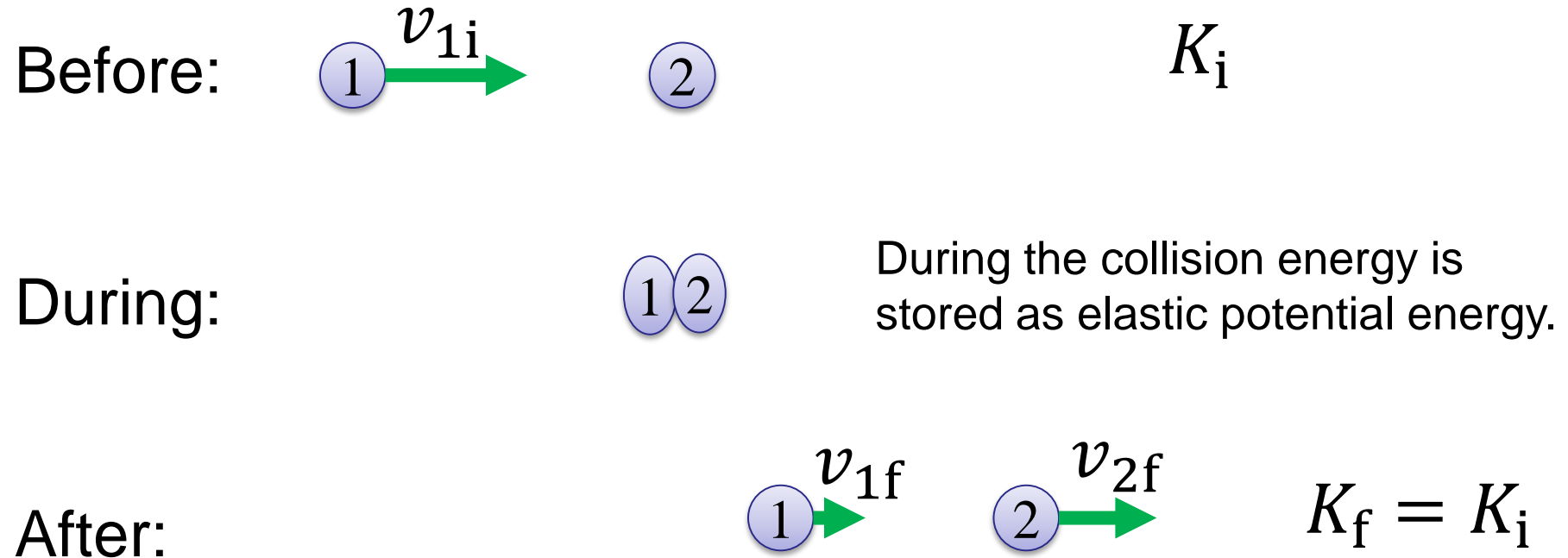


Elastic Collisions

- All quick collisions conserve momentum, because external forces are usually negligible during the collision compared to the collision forces themselves.
- Often, in collisions, kinetic energy after is *less* than kinetic energy before. That's because energy is used up in deforming or heating the colliding objects.
- If kinetic energy is conserved, the collision is said to be **elastic**.

Elastic Collision in 1 Dimension when ball 2 is initially at rest.

Consider a head-on, perfectly elastic collision of a ball of mass m_1 having initial velocity v_{1i} , with a ball of mass m_2 that is initially at rest.



The balls' velocities after the collision are v_{1f} and v_{2f} .

Elastic Collision in 1 Dimension when ball 2 is initially at rest.

Momentum conservation: $m_1 v_{1f} + m_2 v_{2f} = m_1 v_{1i}$

Kinetic energy conservation: $\frac{1}{2} m_1 v_{1f}^2 + \frac{1}{2} m_2 v_{2f}^2 = \frac{1}{2} m_1 v_{1i}^2$

There are two equations, and two unknowns: v_{1f} and v_{2f} .

Solving for the unknowns gives:

Eq. 9.15:

$$v_{1f} = \frac{m_1 - m_2}{m_1 + m_2} v_{1i}$$

$$v_{2f} = \frac{2m_1}{m_1 + m_2} v_{1i}$$

(Elastic collision
with ball 2 initially at
rest.)

Elastic Collision in 1 Dimension when ball 2 is initially at rest.

Eq. 9.15

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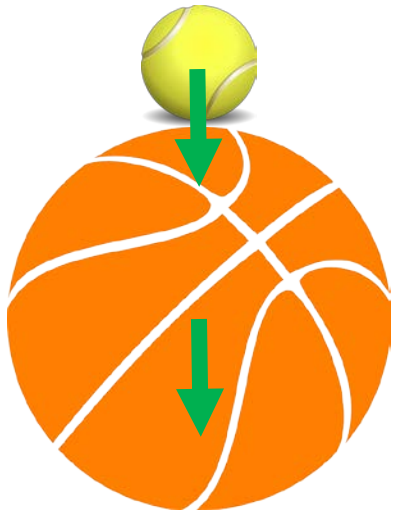
These equations come in especially handy, because you can always switch into an inertial reference frame in which ball 2 is initially at rest!

Demonstration and Example

- A 0.50 kg basketball and a 0.05 kg tennis ball are stacked on top of each other, and then dropped from a height of 0.82 m above the floor.
- How high does the tennis ball bounce?
- Assume all perfectly elastic collisions.



Segment 1:
freefall of both
balls as they
fall, $v_i = 0$.



Segment 2:
Elastic
collision of
basketball with
floor. Tennis
ball continues
downward,
unaffected.



Segment 3:
Elastic
collision of
upward
moving
basketball (1)
with downward
moving tennis
ball (2).



Segment 4:
freefall of
upward
moving tennis
ball.



Demonstration and Example

- Divide motion into segments.
- **Segment 1:** free-fall of both balls from a height of $h = 0.82$ m. Use conservation of energy: $U_f + K_f = U_i + K_i$

$$0 + \frac{1}{2} m v_f^2 = mgh + 0$$

$$v_f = \pm[2gh]^{1/2} = -4.0 \text{ m/s, for both balls.}$$

- **Segment 2:** basketball bounces elastically with the floor, so its new velocity is $+4.0$ m/s.



Demonstration and Example

- **Segment 3:** A 0.50 kg basketball moving upward at 4.0 m/s strikes a 0.05 kg tennis ball, initially moving downward at 4.0 m/s.
- Their collision is perfectly elastic.
- What is the speed of the tennis ball immediately after the collision?



- A 0.50 kg basketball moving upward at 4.0 m/s strikes a 0.05 kg tennis ball, initially moving downward at 4.0 m/s.
- Their collision is perfectly elastic. What is the speed of the tennis ball immediately after the collision?

Demonstration and Example

- **Segment 4:** freefall of tennis ball on the way up. $v_{i2} = +10.5$ m/s.
- Use conservation of energy: $U_f + K_f = U_i + K_i$

$$mgh + 0 = 0 + \frac{1}{2} m v_i^2$$

$$h = v_i^2 / (2g) = 5.6 \text{ m.}$$

- So the balls were dropped from 0.82 m, but the tennis ball rebounds up to 5.6 m! (Assuming no energy losses.)



Before Class 16 next Monday Nov. 13

- Complete Problem Set 7 on Chapters 8 and 9 by Monday Nov.13 at 11:59pm.
- Read the first 3 sections of Chapter 10 and/or watch the Preclass 16 video.
- Have a great Reading Week!



Something to think about: Why is a door easier to open when the handle is far from the hinge, and more difficult to open when the handle is in the middle?

