


# PHY131 F Fall 2020 Class 15

## Today:

- We finish up Chapter 5 on Circular Motion
- We will take 10 minutes in the middle of class to do a **Group Discussion Quiz** by you opening



1

Technology & Science 

## Russian-U.S. crew launches on fast track to the space station

Crew spent weeks in quarantine ahead of launch

The Associated Press · Posted: Oct 14, 2020 2:41 AM ET | Last Updated: October 14



In this image made from video footage released by the Roscosmos Space Agency, a Soyuz-2.1a rocket booster with a Soyuz MS-17 space ship carrying a new crew to the International Space Station blasts off from the Baikonur cosmodrome in Kazakhstan today. (Roscosmos Space Agency via The Associated Press)

A trio of space travelers has launched successfully to the International Space Station, for the first time using a fast-track manoeuvre to reach the orbiting outpost in just three hours.

NASA's Kate Rubins along with Sergey Ryzhikov and Sergey

Poll

## *Crazy Friday:* Let's Choose a Zoom-Filter my face today

What Studio Filter would you prefer on my face today?

A. "We Can Do It!"



D. Goatie



B. "Movember"



E. Red lipstick



C. Beret



2



# PHY131 Help Centre moving to Zoom



The PHY131 Help Centre has moved to Zoom:

<https://zoom.us/j/93809642256>

Passcode: 723874

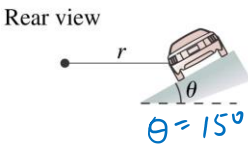
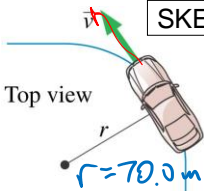
- Sundays: 1:30-2:30pm
- Mondays: 12:00-1:30pm
- Tuesdays: 9:30-10:30am, 3:00-4:00pm
- Wednesdays: 12:00-1:30pm
- Thursdays: 9-10am (updated)
- Fridays: 12:00-1:30pm

3

## Banked Curve Example

A highway curve of radius 70.0 m is banked at a  $15^\circ$  angle. At what speed  $v_0$  can a car take this curve without assistance from friction?

SKETCH & TRANSLATE.



Constant speed  $v_0$   
circular path

$$a_r = \frac{v_0^2}{r}$$

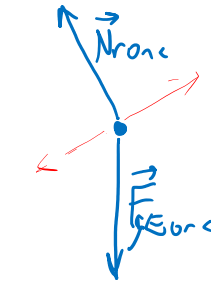
without friction.

$$f_s = 0$$

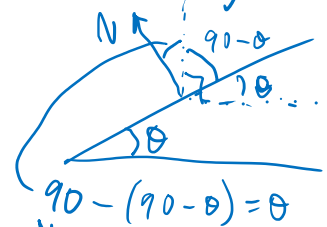
Define system = car  $\neq$  road.

## SIMPLIFY & DIAGRAM

Rear view:



Assume only forces are normal & gravity



$$N_r = N \sin \theta$$

$$N_y = N \cos \theta$$

$$a_y = 0$$

Define  $+y$   
 $+r$

4

### Banked Curve Example

A highway curve of radius 70.0 m is banked at a  $15^\circ$  angle. At what speed  $v_0$  can a car take this curve without assistance from friction?

REPRESENT MATHEMATICALLY

	r-comp	y-comp
N	$N \sin \theta$	$N \cos \theta$
$F_g$	0	$-m_c g$

$$a_y = 0 \Rightarrow \sum F_y = 0 = N \cos \theta - m_c g$$

$$N = \frac{m_c g}{\cos \theta}$$

$$a_r = \frac{\sum F_r}{m_c} = \frac{N \sin \theta}{m_c} = \frac{m_c g \sin \theta}{m_c \cos \theta}$$

$$a_r = \frac{g \sin \theta}{\cos \theta} = \frac{v_0^2}{r}$$

Solve for  $v_0$

SOLVE & EVALUATE

$$v_0^2 = g r \frac{\sin \theta}{\cos \theta} \quad \text{choose positive root.}$$

$$v_0 = \sqrt{g r \frac{\sin \theta}{\cos \theta}} = \sqrt{9.8 \times 70 \times \frac{\sin 15}{\cos 15}}$$

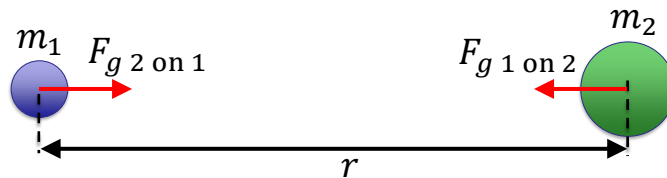
$$v_0 = 13.56 \text{ m/s}$$

$$v_0 = 14 \text{ m/s} \quad \leftarrow \sim 50 \frac{\text{km}}{\text{h}} \rightarrow \text{typical road.}$$

5

## Gravity

It was Newton who first recognized that **gravity is an attractive, long-range force between any two objects.**



When two objects have masses  $m_1$  and  $m_2$  and centers are separated by distance  $r$ , each object attracts the other with a force given by Newton's law of gravity, as follows:

$$F_{g \ 1 \ \text{on} \ 2} = F_{g \ 2 \ \text{on} \ 1} = \frac{G m_1 m_2}{r^2}$$

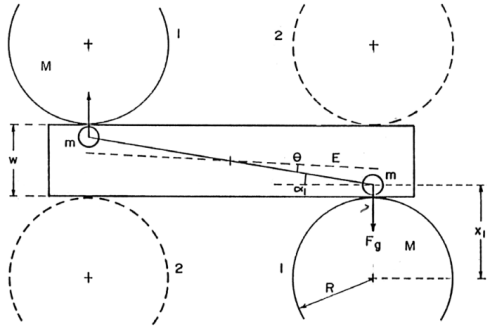
where  $G = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$  is the Gravitational constant (the same everywhere in the universe).

6

# Cavendish Experiment

Done in second year labs (PHY224).

A required **in-person** course.



You end up measuring a force of about  $10^{-8}$  N (10 nano-Newtons!) which is equivalent to the weight of  $0.1 \mu\text{g}$ .

But it is doable in less than 2 weeks.

7

## Gravity Example

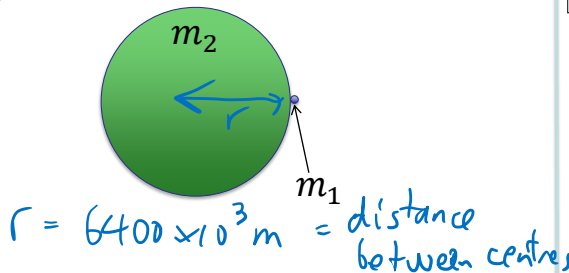
“Object 1”, with mass  $m_1$ , sits at the surface a giant spherical rock which is floating in space.

The giant rock called “object 2” has a mass of  $m_2 = 6 \times 10^{24}$  kg and a radius of 6400 km.

(a) What is the force of gravity of 2 on 1?

(b) Can you think of a good name for object 2?

SKETCH & TRANSLATE.



SIMPLIFY & DIAGRAM

Assume these are isolated objects  $\rightarrow$  no other objects.  
Define system =  $m_1$   $\vec{F}_{g2on1}$

REPRESENT MATHEMATICALLY

Use  $F_{g2on1} = \frac{G m_1 m_2}{r^2}$

SOLVE & EVALUATE

$$F_g = \frac{6.67 \times 10^{-11} \cdot m_1 \cdot 6 \times 10^{24} \text{ kg}}{(6400 \times 10^3)^2}$$

$$F_g = 9.8 m_1 \quad \text{units: } \frac{\text{N}}{\text{kg}} \text{ or } \text{m/s}^2$$

(b) “Earth”

8

# Gravity for Earthlings

If you happen to live on the surface of a large planet with radius  $R$  and mass  $M$ , you can write the gravitational force more simply as:

$$\vec{F}_G = (mg, \text{straight down}) \quad (\text{gravitational force})$$

where the quantity  $g$  is defined to be:

$$g = \frac{GM}{R^2}$$

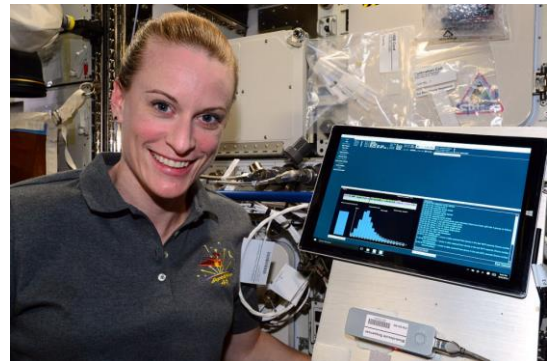
At sea level,  $g = 9.83 \text{ m/s}^2$ .

At 39 km altitude,  $g = 9.71 \text{ m/s}^2$ .



9

- Kate Rubins launched on her second mission to the International Space Station on Wednesday (also her 42nd birthday!)
- She is currently in orbit, working with Russian cosmonauts Sergey Ryzhikov and Sergey Kud-Sverchkov.
- Her return to Earth is scheduled for April 2021.



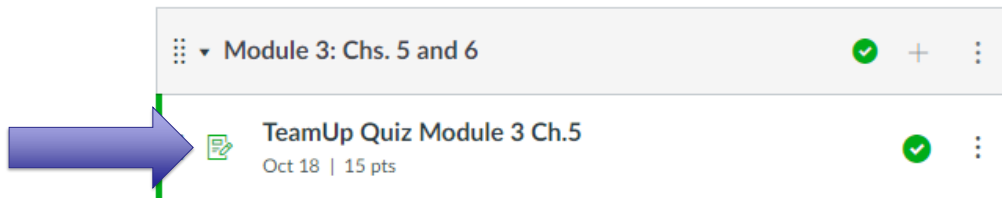
- She has a Bachelor of Science in molecular biology, and a Ph.D. in cancer biology from Stanford.
- In 2016 she was the first person to perform DNA sequencing in space.

10

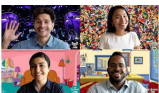


# TeamUp Time!!

- Today you will be doing three multiple choice questions, all from Chapter 5, as a team of 2-4 students in your Practicals Pod.
- Your pod-team shares the mark!
- I'm going to mute here for 10 minutes; right now you should open Microsoft Teams and someone (most recent Facilitator) should place a **video call** to all 3 or 4 members of your Pod-Chat.



11



## Now: TeamUp! You have 10 minutes

- The first step is to decide who will be the TeamUp **Driver**
- All students must log-in to Quercus [You will now have three windows open: my zoom lecture, Microsoft Teams, and Quercus]
- **Non-drivers:** Wait!
- **Driver:** Go to the TeamUp Quiz in this module, click Go to Tool, then Create a Group. Let everyone in the Breakout Room know the session ID. Then WAIT – don't drive off alone!
- **Non-drivers:** Once you get the session ID, go to the TeamUp Quiz in this module, click Go to Tool, then Join Session and type the ID you were given.
- Once everyone in your room arrives in TeamUp, start going through the questions. Please **achieve consensus** before the driver submits.
- **YOU MAY BEGIN!** Note: if your pod-mates are available on Microsoft Teams right now, go to the PHY131 Help Centre and I'll set up breakout rooms there.



12

## Question 1 Discussion

- Astronaut Kate Rubins is currently living on the International Space Station, which orbits at 370 km above the surface of the Earth (low earth orbit).
- Assuming Kate has not changed her mass since moving to space, what is the force of gravity of the Earth on Kate?



- A. Zero
- B. The same as the force of gravity on her while she was on earth.
- C. A little bit less than the force of gravity on her while she was on earth.
- D. Not exactly zero, but much, much less than the force of gravity on her while she was on earth.

13

## Question 2 Discussion

- You are right now a certain distance from the centre of the Earth.
- Astronaut Kate Rubins is currently living on the International Space Station, which orbits at 370 km above the surface of the Earth (low earth orbit).
- How much farther from the center of the Earth is Kate than you?



- A. 1.06 times as far
- B. 1.5 times as far
- C. Twice as far
- D. 10.6 times as far

$$\begin{aligned} \text{Radius of Earth} &= 6400 \text{ km} \\ \text{Kate's d from centre of Earth} &= 6400 + 370 \\ &= 6770 \text{ km} \\ \frac{6770}{6400} &= 1.06 \end{aligned}$$

14

## Question 3 Discussion



- The International Space Station is accelerating toward the Earth at  $8.9 \text{ m/s}^2$ . Why doesn't it crash into the Earth?

A. Bad question: it is not actually accelerating at  $8.9 \text{ m/s}^2$  toward the Earth.

B. Because, as it accelerates toward the Earth, it also moves in a sideways direction, so it misses the Earth.

*Circular path.*

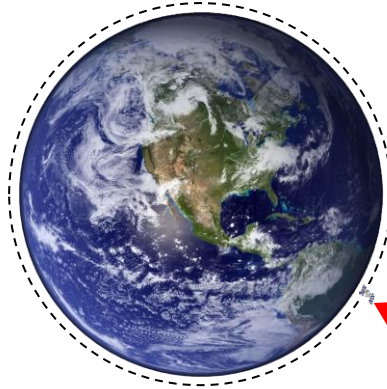
C. This acceleration is compensated for by rocket blasters which continuously point away from the Earth.

D.  $8.9 \text{ m/s}^2$  is not a noticeable acceleration – it would take millions of years to travel 370 km in a straight line at that acceleration.

15

## International Space Station

Orbit is drawn **to scale**



*"weight" you feel is actually the normal force! :*

Kate **feels** weightless because she is in freefall!



Radius of the Earth: 6400 km,  $g = 9.8 \text{ m/s}^2$

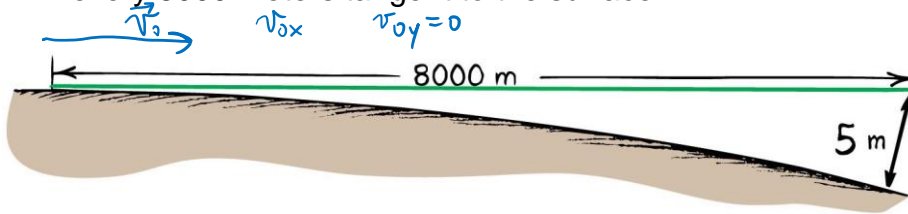
Altitude of Space Station: 370 km,  $g = 8.9 \text{ m/s}^2$  (about 10% less)

16



# The Curvature of the Earth

- Earth surface drops a vertical distance of 5 meters for every 8000 meters tangent to the surface.



## Ball Launched Horizontally

- Consider a ball launched horizontally, so the initial y-component of the velocity is zero.
- How far down does it fall in 1 second?

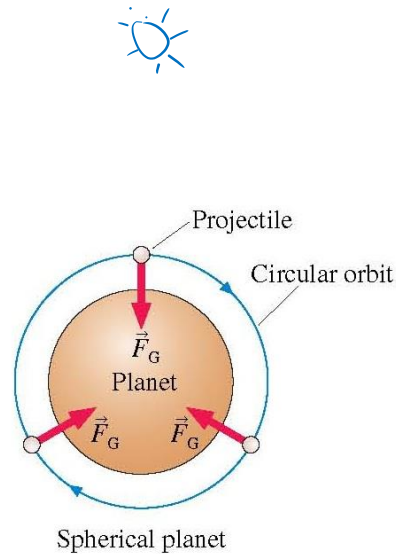
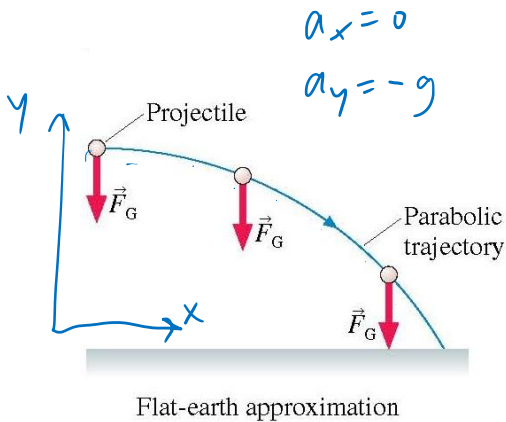
$$y = \frac{1}{2} a_y t^2$$

$$= \frac{1}{2} (-9.8)(1)^2$$

$$= -4.9 \text{ m}$$

If you go  $8000 \text{ m/s}$ , the surface stay same distance away. about 5 m down. the curvature of the Earth makes

17

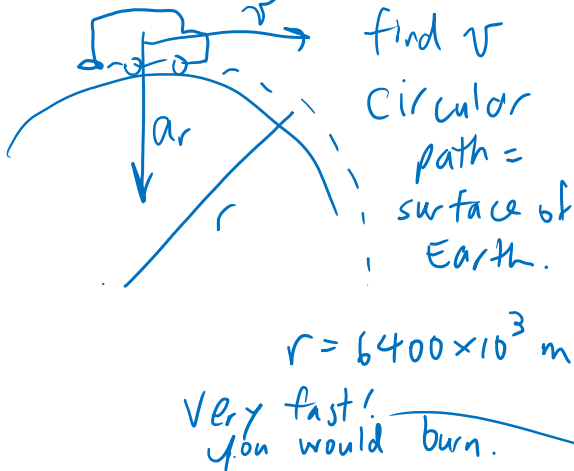


18

### Example

How fast would you have to drive in order to be “weightless” – ie, no normal force needed to support your car?

SKETCH & TRANSLATE.



SIMPLIFY & DIAGRAM

Assume  $\vec{N}_{s \text{ on } c} = 0$

$$a_r = \frac{v^2}{r}$$

Define  $\downarrow +r$

$$\sum F_r = m_c g$$

REPRESENT MATHEMATICALLY

$$a_r = \frac{v^2}{r} = \frac{\sum F_r}{m_c} = \frac{m_c g}{m_c}$$

$$\frac{v^2}{r} = g$$

choose +

$$v^2 = gr$$

$$v = \sqrt{gr}$$

SOLVE & EVALUATE

$$v = \sqrt{9.8 \cdot 6400 \times 10^3} = 7900 \frac{\text{m}}{\text{s}}$$

19

## Before Class 16 on Monday

- Next week we start on Chapter 6 on Impulse and Linear Momentum!!
- Please read:
  - 6.1 Conservation of Mass
  - 6.2 Conservation of Momentum
- Something to think about: When a ball is thrown up in the air and then falls back down, is its momentum conserved during freefall?
- For the next 30 minutes I will be in the PHY131 Help Centre
- Zoom Meeting ID: 938 0964 2256
- Passcode: 723874



20