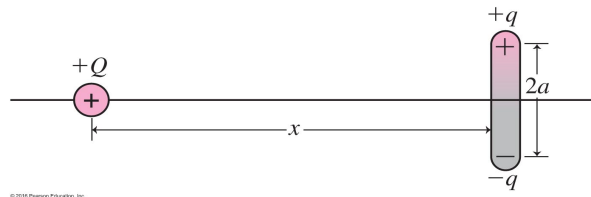


Practice Problem Set 3

#1. A dipole and a charge

A dipole with charges $\pm q$ and separation $2a$ is located a distance x from a point charge Q , oriented as shown in Figure 20.32 of the textbook (reproduced here for convenience). For both a) and b), consider the $x \gg a$ limit.

- What is the net torque (magnitude and direction) on the dipole?
- What is the net force (magnitude and direction) on the dipole?
- Does the previous answer surprise you? How could you have predicted it based on results from the chapter?



#2. A Charged Cross, or Practice With Integrals

a) Consider a thin rod of length $2a$ placed along the x axis and centered at the origin (see Figure 1). Considering the rod has a uniformly distributed charge q (where $q > 0$), find the electric field at the point P at a distance x from the origin on the positive side of the x axis (assume $x > a$). Does your result agree with your expectations in the $x \gg a$ limit?

b) Consider a thin rod, also of length $2a$, placed along the y axis and centered at the origin (see Figure 2). The rod has a uniformly distributed charge $-q$ (where $q > 0$). Find the electric field at the point P at a distance x from the origin on the positive side of the x axis. Does your result agree with your expectations in the $x \gg a$ limit?

c) Now, suppose these two metal rods are positioned as shown in Figure 3 (assume no charge is exchanged), with the negatively charged rod placed horizontally. What is the field at the point P at a distance x from the origin, on the positive side of the x axis?

Try taking the $x \gg a$ limit. In this limit, with what power of x does the electric field decay? Is this behaviour reminiscent of a specific charge distribution?

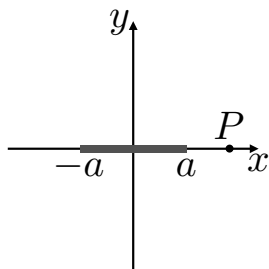


Figure 1

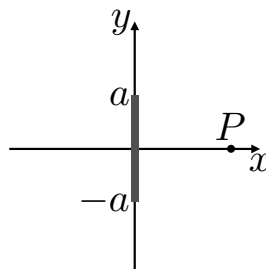


Figure 2

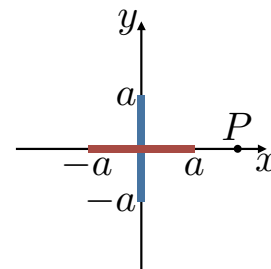


Figure 3