Photonic Crystal Architecture for Room-Temperature Equilibrium Bose-Einstein Condensation of Exciton Polaritons

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We describe photonic crystal microcavities with very strong light-matter interaction to realize room-temperature, equilibrium, exciton-polariton Bose-Einstein condensation (BEC). This goal is achieved through a careful balance between strong light trapping in a photonic band gap (PBG) and large exciton density enabled by a multiple quantum-well (QW) structure with a moderate dielectric constant. This approach enables the formation of a long-lived, dense \(10 - \mu m - 1 - \text{cm-scale cloud of exciton polaritons with vacuum Rabi splitting that is roughly } 7\% \text{ of the bare exciton-recombination energy. We introduce a woodpile photonic crystal made of Cd}_{0.6}\text{Mg}_{0.4}\text{Te with a 3D PBG of 9.2\% (gap-to-central-frequency ratio ) that strongly focuses a planar guided optical field on CdTe QWs in the cavity. For 3-nm QWs with 5-nm barrier width, the exciton-photon coupling can be as large as } h\Omega = 55 \text{ meV (i.e., a vacuum Rabi splitting of } 2h\Omega = 110 \text{ meV). The exciton-recombination energy of 1.65 eV corresponds to an optical wavelength of 750 \text{ nm. For } N = 106 \text{ QWs embedded in the cavity, the collective exciton-photon coupling per QW (} h\Omega/\sqrt{N} = 5.4 \text{ meV) is much larger than the state-of-the-art value of 3.3 \text{ meV, for the CdTe Fabry-Pérot microcavity. The maximum BEC temperature is limited by the depth of the dispersion minimum for the lower polariton branch, over which the polariton has a small effective mass of approximately } 10^{-5}m_p\text{, where } m_p\text{ is the electron mass in vacuum. By detuning the bare exciton-recombination energy above the planar guided optical mode, a larger dispersion depth is achieved, enabling room-temperature BEC. The BEC transition temperature ranges as high as 500 K when the polariton density per QW is increased to } (11a_B)^{-2}, \text{ where } a_B = 3.5 \text{ nm is the exciton Bohr radius and the exciton-cavity detuning is increased to } 30 \text{ meV. A high-quality PBG can suppress exciton radiative decay and enhance the polariton lifetime to beyond 150 ps at room temperature, sufficient for thermal equilibrium BEC.}

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I. INTRODUCTION

Semiconductor microcavities offer an unique platform to study fundamental phenomena of quantum electrodynamics in the strong-coupling regime [1–3]. Thanks to advances in growth and manipulation technologies, both excitons and cavity photons are tunable in a variety of ways that enable observations of novel phenomena [3–5]. In the last decade, nonequilibrium exciton-polariton Bose-Einstein condensation (BEC) has been observed in 1D Fabry-Pérot microcavities in various materials [4–9]. However, the polariton lifetime is often too short to achieve thermal equilibrium BEC. Moreover, the BEC temperature is limited by the weakness of photon confinement and the resulting insufficient exciton-photon-coupling strength.

In an optical cavity, an atomic excitation and a photon may couple together to form a coherent superposition when their decay rates (times \(h\)) are much smaller than their coupling. In a semiconductor microcavity [1–3], excitons and photons constitute polaritons in this manner. The quantum superposition of excitons and photons confers them with remarkable dynamics. For instance, the polariton effective mass, inherited from the cavity photon, is about \(10^{-10}\) times the mass of a rubidium atom. Consequently, the BEC transition temperature of polariton gases is usually above 1 K. In the last decade, signatures of nonequilibrium polariton BEC have been reported in semiconductor microcavities [4–9]. Although aspects of macroscopic coherence and superfluidity have been observed or claimed [6,10–13], the polariton lifetime has been too short (about 1 ps) to achieve genuine thermal equilibrium [14]. Recently high-quality-factor Fabry-Pérot microcavities have provided longer polariton lifetimes [15]. Nevertheless, polaritons can radiatively decay into extraneous and degenerate optical modes of these 1D periodic structures from a micron-scale confinement region.

Because of the half-photon and half-exciton nature of the polariton, the Bose condensate contains polariton-polariton interactions (i.e., optical nonlinearity). Such a nonlinear, coherent light source has potential applications as a laser with a low excitation threshold and novel photon statistics.
Nonlinearity can also be exploited for the development of all-optical transistors [19], diodes [20], and switches [21,22]. Unfortunately, most realizations of polariton BEC have been at cryogenic temperatures. Above room temperature, polariton BEC [23] is essential for broad practical applications. While studies on GaN [24], ZnO [25,26], and organic materials [27] have found room-temperature polariton light-emission and lasing, these polaritons are not sufficiently long lived for equilibrium BEC. These room-temperature effects are facilitated by a large exciton-binding energy $E_b$, and exciton-photon coupling $\hbar \Omega$. With a small exciton Bohr radius $a_B$, the saturation density $(5a_B)^{-2}$, at which electron-hole pairs unbind due to many-body effects (screening and phase-space filling, as revealed in Ref. [28]), is likewise very high in these materials. On the other hand, small excitons are very sensitive to local disorder, which leads to strong inhomogeneous broadening that smears the exciton and polariton dispersion. The inhomogeneous broadening in the polymer material measured from optical spectroscopy in Ref. [27] is as high as 60 meV, while the exciton-photon coupling is $\hbar \Omega = 58$ meV. The inhomogeneous broadenings in GaN and ZnO are around 16 meV [29] and 25 meV [30], respectively, while the exciton-photon couplings are 25 meV [31] and 29 meV [32], respectively. In contrast, the inhomogeneous broadening in GaAs and CdTe is around 1 meV [33]. Nevertheless, the exciton–polariton lifetime is still below 1 ps [26] in these materials due to the nature of the utilized optical cavity. Recently, the macroscopic occupation of photonic states in microcavities filled with dye molecules has been observed at room temperature [34,35]. This quasicondensate [36] in the weak-coupling regime exhibits a strongly fluctuating photon number [35], unlike BEC of polaritons in the strong-coupling regime with conserved particle number [4].

In this article, we introduce an alternative approach, using 3D photonic band-gap (PBG)-based [37,38] microcavities [39–41] to greatly enhance the exciton-photon coupling and eliminate the radiative decay of polaritons. We focus on CdTe-based photonic crystal microcavities which offer an effective balance between strong light confinement and high exciton density. The exciton-binding energy in CdTe quantum wells (QWs) has been measured to be about 20 meV (varying with QW width, temperature, etc.) [42–44], leading to an exciton Bohr radius $a_B$ of about 4 nm. An exciton-photon coupling of $\hbar \Omega = 13$ meV has been experimentally realized in CdTe-based Fabry–Pérot microcavities with $N = 16$ QWs [8]. These data indicate that neither the exciton-binding energy nor the exciton– photon coupling in CdTe structures is greater than room temperature $k_B T = 26$ meV. Bare excitons in CdTe QWs are not stable at room temperature, and the polariton BEC temperature is below room temperature in Fabry–Pérot microcavities. Indeed, nonequilibrium polariton BEC in a CdTe-based Fabry–Pérot microcavity is only 19 K [8]. On the other hand, the refractive index of CdTe is around 1 meV [33]. Nevertheless, the exciton-photon coupling regime with conserved particle number [4] denotes band-gap width, and $\omega_c$ is the PBG central frequency.) The dielectric constant of the regions with QWs is taken to be 8, which is the average value of the QW and barrier materials. Using $N = 106$ QWs, the exciton-photon coupling is as large as $\hbar \Omega = 55$ meV; i.e., the vacuum Rabi splitting is 110 meV. The exciton-photon coupling per QW of $\hbar \Omega/\sqrt{N} = 5.4$ meV is considerably larger than $13/\sqrt{16} = 3.3$ meV for the Fabry–Pérot microcavity reported in Ref. [8] (i.e., exciton-photon coupling of 13 meV for 16 QWs). We also calculate the exciton-photon coupling when the number of QWs in each rod is reduced by increasing the barrier width (keeping two QWs in the central slab). The exciton-photon coupling is 45 meV if the barrier width is increased to 10 nm, while there are seven QWs in each rod in the active region (total of 58 QWs). When the barrier width is increased to 20 nm with four QWs in each rod in the active region (total of 34 QWs), the exciton-photon coupling is 40 meV. If there are only two QWs in the central slab and no QW in the rods, the exciton-photon coupling remains as high as 33 meV. All these energies are greater than room temperature $k_B T = 26$ meV and (with positive detuning of the exciton-recombination energy from the lowest 2D guided mode) are shown below to support room-temperature polariton BEC.

Fabrication of the structure proposed [as shown in Figs. 1(a) and 1(b)] is possible using wafer fusion and the laser-beam-assisted precise alignment of rods [51,52].
PHOTONIC CRYSTAL ARCHITECTURE FOR ROOM-TEMPERATURE POLARITON BEC

FIG. 1. Photonic crystal architecture and photonic band dispersion. (a) A slab layer sandwiched between two woodpile photonic crystals induces 2D photonic bands ("guided modes") in the 3D PBG with \( \delta \omega / \omega_c = 9.2\% \), where \( \delta \omega \) is the band-gap width and \( \omega_c \) is the PBG central frequency. (b) QWs are grown in the slab and the eight nearby layers of rods. Typically, \( a = 360 \, \text{nm} \), \( w = 0.25a = 90 \, \text{nm} \), \( h = 0.3a = 110 \, \text{nm} \), and \( b = 0.06a = 20 \, \text{nm} \). There are about 100 QWs with the same width. There are two QWs in the slab layer and about 12 QWs in each rod. The QW widths are chosen to be 3, 4, 5, and 6 nm for comparison, while the width of the barrier layers between QWs is fixed to be 5 nm. QWs are made of CdTe (dielectric constant 8.5), while the barriers and photonic crystals are made of Cd\(_{0.6}\)Mg\(_{0.4}\)Te (dielectric constant 7.5). In the regions with QWs, the dielectric constant is taken to be 8 (average of the two materials). (c),(d) Dispersion of the 2D guided modes (dashed green and solid red curves) and the bulk 3D photonic bands (shaded regions). The first Brillouin zone of the 2D guided modes is \( qx; q_y < \frac{\pi}{a} \). The lowest 2D photonic band [the solid curves in (c) and (d)] is coupled with excitons [dotted curve in (d)] in QWs. The lower and upper polariton branches [solid blue curves in (d)] are depicted for exciton recombination in resonance with the lowest 2D guided mode. In this case, each QW width is 4 nm, the exciton-recombination energy is \( E_{X0} = 1.59 \, \text{eV} \), and the photonic lattice constant is chosen to be \( a = 360 \, \text{nm} \). The exciton-photon-coupling strength and the on-resonance lower-polariton dispersion depth is 48 meV. Larger dispersion depth and higher BEC temperature are achieved by detuning the exciton-recombination energy above the lowest 2D guided mode.

It has been demonstrated [40] that a layer of rods with MQWs (grown by molecular beam epitaxy and etched) can be placed in a woodpile photonic crystal. By repeated wafer fusion, laser-assisted alignment, careful etching, and polishing (monitored by thin-film interference), sandwich structures can be fabricated with high precision. Accurate fabrication of GaAs woodpile photonic crystals with a near-infrared, MQW, light-emitting layer was reported by Noda and co-workers [40]. Similar techniques can, in principle, be employed for our proposed CdTe photonic crystal structure.

3D photonic crystal microcavities have been fabricated with much higher quality factors than their counterpart Fabry-Pérot microcavities. Quality factors as high as \( 2 \times 10^6 \) have been demonstrated experimentally for microcavities in the woodpile architecture [53]. In addition, a 3D PBG eliminates the purely radiative recombination of excitons into unwanted modes when the lower polariton energy is in the PBG. In this case, the polariton lifetime is determined by exciton nonradiative recombination. In CdTe QWs at room temperature, the exciton-photoluminescence-decay time is measured to be 150 ps in Ref. [54], suggesting that the nonradiative recombination time is even longer. This time scale is sufficient for polaritons to reach thermal equilibrium since the exciton–optical-phonon scattering in CdTe at room temperature is quite efficient [55]. Our calculation reveals that room-temperature equilibrium polariton BEC can be achieved for a polariton density of \( 5 \times 10^5 \, \text{μm}^{-2} \) [exciton density in each QW of approximately \((30a_B)^{-2}\), below the saturation density of \((5a_B)^{-2}\), where \( a_B = 3.5 \, \text{nm} \) is the bare exciton Bohr radius for a QW of width 3 nm]. This condition occurs when the exciton-recombination energy is detuned 30 meV above the lowest 2D guided mode and the excitons are trapped in a box with a side length of \( 10^{-10^4} \) μm. The realization of equilibrium polariton BEC at and above room temperature may open the door to broad applications of quantum mechanics beyond the microscopic scale.

II. POLARITONS IN A 3D PHOTONIC BAND-GAP MICROCAVITY

Figures 1(a) and 1(b) depict our proposed woodpile photonic crystal heterostructure. The distance between the nearest-neighbor rods in the same layer is denoted by \( a \), the height of each rod is \( h = 0.3a \), the width of each rod is \( w = 0.25a \), and the thickness of the solid central slab is \( b = 0.06a \). In order to place the lowest 2D guided mode within the PBG in resonance with the exciton transition at 1.59 eV (for QW width 4 nm), typically, \( a = 360 \, \text{nm} \). The PBG is centered in the range of 750 nm [56]. MQWs are grown in the slab and the eight layers of rods close to the slab. The other regions above and below are the cladding woodpile photonic crystals. The QWs are made of CdTe, while the barrier layers between QWs are made of Cd\(_{0.6}\)Mg\(_{0.4}\)Te. Both materials are direct electronic band-gap semiconductors with band

031025-3
structures similar to GaAs. The electronic band gaps of CdTe and Cd$_{0.6}$Mg$_{0.4}$Te are 1.475 and 2.28 eV, respectively [57,58] (from linear interpolation between the band gaps of CdTe and MgTe, the latter being 3.49 eV). The cladding rods without QWs are also made of Cd$_{0.6}$Mg$_{0.4}$Te. The structure breaks the translation symmetry along the $z$ direction [see Fig. 1(a)] but has lattice translation symmetry in the $x$-$y$ plane. [The coordinate axes are depicted in Fig. 1(b).] There is no inversion symmetry with respect to the slab. However, the system has a $D_{2h}$ symmetry with two mirror planes: the $y$-$z$ and $x$-$z$ planes [59]. There are several 2D guided photonic bands localized around the dispersion. The slab of these confined modes within the PBG are shown in Figs. 1(c) and 1(d). The electric field in these 2D bands can be written as

$$
\tilde{E}_{ia,q}(\tilde{r}) = \sqrt{\frac{\hbar \omega_{ia,q}}{2 \epsilon_0}} \tilde{u}_{ia,q}(\tilde{r}) e^{i\tilde{q} \cdot \tilde{r}}.
$$

(1)

Here, $\epsilon_0$ is the vacuum permitivity, $S$ is the area of the structure in the $x$-$y$ plane, $\tilde{r} = (\tilde{r}, z)$ with $\tilde{r} = (x, y)$, and $\omega_{ia,q}$ is the frequency of a photon in the $i$th band with a Bloch wave vector $\tilde{q}$ in the 2D Brillouin zone $-\frac{\pi}{a} \leq q_x, q_y < \frac{\pi}{a}$. The field is normalized such that $S^{-1} \int d\tilde{r} d\epsilon(\tilde{r})|\tilde{u}_{ia,q}(\tilde{r})|^2 = 1$, where $\epsilon(\tilde{r})$ is the coordinate-dependent dielectric function. Photons in the lowest confined photonic band and electron–heavy-hole excitons in the MQWs interact to form the lower and upper polariton branches. These dispersions are depicted in Fig. 1(d) when the exciton-recombination energy coincides with the 2D photonic band edge. The dispersion of the lowest confined photonic band and that of the lower polariton branch in the 2D photonic Brillouin zone are shown in Fig. 2 for the case when the exciton-recombination energy is detuned by 30 meV above the 2D photonic band edge.

The energy levels and wave functions of the $1s$ excitonic states in QWs are obtained from diagonalizing the effective mass Hamiltonian [45]. (See the Appendix for details.) Combining the microscopic details of cavity photons and QW excitons, the Hamiltonian of the coupled exciton-photon system [46] is given by

$$
H = H_X + H_P + H_{int},
$$

(2a)

$$
H_X = \sum_{l,a,n,q} E_X^{(l)}(\tilde{q} + \tilde{G}_n) \beta_{l,a,q;\tilde{G}_n}^i \beta_{l,a,\tilde{q} + \tilde{G}_n}^i.
$$

(2b)

$$
H_P = \sum_{i,q} \hbar \omega_{ia,q} a_{ia,q}^\dagger a_{ia,q},
$$

(2c)

$$
H_{int} = \sum_{l,a,n,i,q} i \hbar \Omega_{l,a,n,i,q} \beta_{l,a,q;\tilde{G}_n}^i a_{ia,q} + \text{H.c.}
$$

(2d)

The operator $\beta_{l,a,q;\tilde{G}_n}^i$ creates a $1s$ exciton in the $l$th QW with polarization $\alpha = L, T$ (longitudinal or transverse) and center-of-mass wave vector $\tilde{q} + \tilde{G}_n$, where $\tilde{G}_n = \frac{2\pi}{a}(n_x, n_y)$ is the 2D reciprocal lattice vector for the photonic band structure with integers $n_x$ and $n_y$. The exciton dispersion $E_X^{(l)}(\tilde{q}) = E_X(\tilde{q}) + \delta E_1$ with $E_X(\tilde{q}) \equiv E_{X0} + (\hbar^2 \tilde{q}^2 / 2m_X)$ includes a fluctuation term $\delta E_1$ varying for different QWs to describe disorder effects. $E_{X0}$ is the exciton-recombination energy at zero center-of-mass wave vector. $m_X = m_e + m_h$ is the effective mass of an exciton, with $m_e$ and $m_h$ being the electron and hole effective masses, respectively. The operator $a_{ia,q}^\dagger$ creates a photon in the $i$th band with Bloch wave vector $\tilde{q}$. The coupling-matrix element is calculated [46] as

$$
\tilde{\Omega}_{l,a,n,i,q} = \frac{|\phi(0)| d \sqrt{\omega_{ia,q}}}{S_{UC} \sqrt{2\hbar \epsilon_0}} \times \int_{\text{UC}} d\tilde{r} e^{-i\tilde{G}_n \cdot \tilde{r}} \tilde{u}_{a,i,q}(\tilde{r}, z) \Theta(\tilde{r}).
$$

(3)

$|\phi(0)|$ denotes the amplitude of the $1s$ exciton wave function when the distance between electron and hole is 0. $d$ is the interband dipole-matrix element in CdTe. $z$ is the coordinate of the center of the QW in the $z$ direction. $S_{UC} = a^2$ is the area of the unit cell (UC) in the $x$-$y$ plane. $u_{a,i,q} = \tilde{e}_\alpha \cdot \tilde{u}_{a,i,q}$, where $\tilde{e}_\alpha$ is a unit vector along the polarization direction of the $\alpha$ exciton. For longitudinal ($\alpha = L$) excitons, $\tilde{e}_\alpha$ is along $\tilde{q}$, while for the transverse ($\alpha = T$) exciton, it is perpendicular to both $\tilde{q}$ and the $z$ direction. $\Theta(\tilde{r})$ equals 1 when the coordinate $\tilde{r}$ is in the semiconductor region and 0 when $\tilde{r}$ is in the air region. $\Theta(\tilde{r})$ describes the overlap between the photonic field and the excitonic wave function. The integration in Eq. (3) is over the UC of the structure in the $x$-$y$ plane.

It is sufficient to use only the spectrum close to the energy minima of the lowest confined photonic band to calculate the dispersion of the lower polariton branch [see Figs. 1(d) and 2(b)]. This branch is essential for the study of
polariton BEC. There are two energy minima for the photon: one at $\vec{Q}^{(1)} = (\frac{\pi}{a}, 0)$, the other at $\vec{Q}^{(2)} = (0, \frac{\pi}{a})$.

We consider the situation when the exciton-recombination energy $E_{X0}$ is close to the two energy minima. The photonic dispersion around the two minima is approximately parabolic:

$$\hbar \omega_{\tilde{q}} = \hbar \omega_0 + \frac{\hbar^2 (q_x - Q_x^{(1)})^2}{2m_x^{(1)}} + \frac{\hbar^2 (q_y - Q_y^{(1)})^2}{2m_y^{(1)}}, \quad (4)$$

with $\nu = x, y$. From the $D_{2d}$ symmetry, the photonic effective masses satisfy the relations $m_x^{(x)} = m_y^{(y)}$ and $m_x^{(y)} = m_y^{(x)}$. If $a = 360$ nm, the plane-wave-expansion calculation [60] yields $m_x^{(x)} = 2.9 \times 10^{-5} m_0$ and $m_x^{(y)} = 4.7 \times 10^{-5} m_0$, where $m_0$ is the electron mass in vacuum. Scale invariance of the Maxwell equations dictates that $\omega_0$, $m_x^{(x)}$, and $m_x^{(y)}$ are proportional to $1/a$. For CdTe QWs, the effective mass of the conduction-band electron is $m_e = 0.095 m_0$ [58], while the effective mass of the heavy hole is $m_h = 0.4m_0$ [48].

When the fluctuation in the exciton energy among QWs is neglected, i.e., $E_x^{(i)}(\tilde{q}) = E_x(\tilde{q})$ for all $i$, we introduce the collective excitonic operator $b_{\tilde{q}} \equiv \sum_{l,a,n} \Omega_{l,a,\tilde{q}} \phi_{l,a,n,\tilde{q}}$ to obtain the effective polariton Hamiltonian [61,62]:

$$H = H_0 + H_I. \quad (5a)$$

$$H_0 = \sum_{\tilde{q}} [E_x(\tilde{q}) b_{\tilde{q}}^\dagger b_{\tilde{q}} + \hbar \omega_{\tilde{q}} a_{\tilde{q}}^\dagger a_{\tilde{q}}]. \quad (5b)$$

$$H_I = \hbar \sum_{\tilde{q}} (b_{\tilde{q}}^\dagger a_{\tilde{q}}^\dagger - a_{\tilde{q}} b_{\tilde{q}}). \quad (5c)$$

The collective exciton-photon coupling is given by

$$\hbar \Omega_{\tilde{q}} = \hbar \sqrt{\sum_{l,a,n,\tilde{q}} |\Omega_{l,a,\tilde{q}}|^2}. \quad (6)$$

Here, $b_{\tilde{q}}$ corresponds to the mode that couples most strongly to the lowest 2D guided mode in the PBG. Other excitonic modes orthogonal to this mode (in the Hilbert space of excitonic states spanning all QWs) are much more weakly coupled to the 2D photonic bands. In the above equations, the photonic band index $i$ is omitted since only the lowest confined 2D photonic band is relevant. We also approximate the $\tilde{q}$ dependence of the collective coupling by its value at the two polariton-energy minima and define $\hbar \Omega \equiv \hbar \Omega_{\tilde{q}^{(1)}} = \hbar \Omega_{\tilde{q}^{(2)}}$. This approximation is justified since beyond the narrow range around the two energy minima, the lower polariton dispersion becomes excitonlike and its detailed form does not alter the low-energy dynamics [see Figs. 1(d) and 2(b)]. The dispersion of the lower polariton branch is given by

$$E_{LP}(\tilde{q}) = \frac{E_x(\tilde{q}) + \hbar \omega_{\tilde{q}}}{2} - \left[ \left( \frac{E_x(\tilde{q}) - \hbar \omega_{\tilde{q}}}{2} \right) + \hbar^2 \Omega^2 \right]^{1/2}. \quad (7)$$

The above dispersion can likewise be extended to the whole 2D wave-vector space since away from the energy minima $\vec{Q}^{(1)}$ and $\vec{Q}^{(2)}$, the dispersion of the lower polariton becomes excitonlike (i.e., almost flat dispersion).

III. VERY STRONG LIGHT-MATTER INTERACTION

Figure 3(a) shows the collective exciton-photon coupling $\hbar \Omega$ calculated for different QW widths when excitons are in resonance with the lowest 2D guided mode for photons, i.e., $E_{X0} = \hbar \omega_0$. The vacuum Rabi splitting $2\hbar \Omega$ exceeds 100 meV when the QW width is 3 nm (experimentally accessible, as shown by Refs. [63,64]). The width of the barrier layers between QWs is fixed at 5 nm throughout this work. Figure 3(b) depicts how the photonic crystal lattice constant $a$ must be adjusted as the QW width is varied, in order to maintain resonance between the exciton-recombination energy and the 2D guided mode. The total number of QWs that fit into the active region is correspondingly adjusted. Figure 3(c) depicts the variation of the exciton-binding energy and Bohr radius with QW width. The calculated exciton-binding energies, ranging from 17 to 23 meV, agree well with the experimental results of 17–25 meV [42–44].

Considerable enhancement of the exciton-photon coupling in our photonic crystal microcavity (compared with Fabry-Pérot microcavities) originates from the light-trapping effect of the PBG. In Fig. 3(d), we compare the photonic field-intensity $|\tilde{E}|^2$ distribution as a function of $z$ but averaged over the $x$-$y$ plane for the Cd$_{0.4}$Mg$_{0.6}$Te-Cd$_{0.8}$Mn$_{0.2}$Te Fabry-Pérot and the 3D photonic crystal microcavities with the same photon energy. The photonic crystal microcavity clearly focuses the electric field much more strongly than the Fabry-Pérot. Moreover, the averaged electric field intensity at $z = 0$ is significantly larger. This large field intensity is because in photonic crystal, a large volume fraction ($\approx 75\%$) is air, which reduces the overall dielectric constant of the structure. The reduced screening enhances the averaged electric field intensity $|\tilde{E}|^2$ at $z = 0$ by 16 times. Another important advantage of the PBG heterostructure is the strong spatial variations of the field intensity in the $x$-$y$ plane. The higher-intensity regions act as an attractive “optical potential” for the exciton, and the wave function of the lower polariton is peaked in these “hot spots” which offers a way to “pattern” the polariton condensates in the $x$-$y$ plane [see Fig. 3(e)]. The peak intensity in the $x$-$y$ plane is greater than the average intensity depicted in Fig. 3(d) which provides further enhancement in exciton-photon coupling compared
to the 1D Fabry-Pérot geometry for which the field intensity is uniform in the x-y plane. From Figs. 3(d) and 3(e), the peak intensity is about 38 times (the average intensity is 16 times) as large as that in the Fabry-Pérot microcavity. Other photonic crystals that have a larger intensity (of the order of nanoseconds [4]). Clearly, very strong exciton-photon coupling, long polariton lifetime, and small polariton effective mass are possible in the photonic crystal microcavity.

IV. ROOM-TEMPERATURE POLARITON BEC

In this section, we delineate the precise conditions for room-temperature polariton BEC in our photonic crystal microcavity. The BEC transition temperature is very sensitive to the dispersion depth of the lower polariton branch and the density of polaritons, but relatively insensitive to the polariton-trapping area over a broad range of lengths $D$, from 10 $\mu$m to 1 cm, when the polariton density is high. The polariton density can be controlled by excitation of electron-hole pairs with energy above the upper 3D photonic band edge. These carriers can then relax into the lower polariton branch within the PBG. Since the polariton lifetime is enhanced beyond the thermalization time (on the order of ps at room temperature), polaritons achieve thermal equilibrium long before they decay. We consider a finite-sized trap with box (square-well potential) confinement in the x-y plane. This square quantum box has a side length of $D$. Such a box can be created by replacing our infinite central slab by a finite-sized slab [40,53,68] or by increasing the Mg fraction outside the prescribed box region [69] to create a barrier for excitons. Trapping by these means enables a higher BEC transition temperature than harmonic trapping potentials induced by strain [18]. The trapping box induces quantization of the polariton wave vector in the x and y directions, discretizing the polariton spectra and enabling the BEC phase transition that would otherwise be forbidden in an infinite 2D system.
To simplify the calculation, we approximate the polariton effective mass with the isotropic “density-of-states mass” \( m_{\text{DOS}} = \sqrt{m_x(x) m_y(y)} \).

In Figs. 4(a) and 4(b), we plot the ground-state occupation \( N_0 \) as a function of the polariton density. The polariton distribution is calculated assuming a noninteracting, equilibrium polariton gas. There is a rapid increase of \( N_0 \) around a threshold density, above which \( N_0 \) becomes comparable with the total polariton number \( N_{\text{tot}} \). We define the polariton BEC transition according to the criterion \( N_0/N_{\text{tot}} = 0.1 [70] \). This criterion gives a lower estimate of the BEC transition temperature than the criterion employed by Ketterle and van Druten [71]. At low temperatures, polaritons are mainly distributed in the low-energy, photonlike states around the bottom of the lower polariton branch with very small effective mass [see Fig. 4(c)]. The small effective mass enhances condensation and reduces the threshold density for polariton BEC. The dispersion depth of these photonlike states is

\[
V = (E_X - E_{LP})|\vec{q}| = \frac{\Delta}{2} + \sqrt{\left(\frac{\Delta}{2}\right)^2 + \hbar^2 \Omega^2},
\]

where \( \Delta = E_{X0} - \hbar \omega_0 \) is the detuning between the exciton and the photon. On the other hand, if the temperature is comparable to or higher than \( V/k_B \), the occupation of high-energy, excitonlike states is significant. The effective mass of the bare exciton is around 4 orders of magnitude larger than the 2D guided photon effective mass. Likewise, the density of excitonlike states is about 4 orders of magnitude larger than the low-energy, photonlike states. The consequences are indicated in Figs. 4(a) (the low-temperature case) and 4(b) (the high-temperature case). Polariton BEC at temperatures comparable with \( V/k_B \) require very high polariton density. Since the polariton is a quantum superposition of a photon and an exciton, the polariton density cannot exceed a specific “saturation density,” beyond which exciton-exciton interaction causes considerable exciton ionization. Therefore, the polariton BEC transition temperature is essentially limited by the dispersion depth \( V \).

The dispersion depth is increased by a positive detuning \( \Delta \) [see Fig. 4(d)]. However, the excitonic fraction of the polariton is reduced with increasing \( \Delta \), which reduces the phonon-polariton and polariton-polariton interactions, and consequently, it takes a longer time for polaritons to reach their thermal equilibrium. From experimental measurements [55], the phonon-exciton-scattering time at room temperature is estimated to be about 0.1 ps (see the Appendix). A thermalization time on the order of 1 ps is possible if the exciton fraction is higher than 10%. In the range of detuning considered in this article \( 0 \text{ meV} < \Delta < 40 \text{ meV} \), the excitonic fraction is greater than 19% for exciton-photon coupling as low as \( \hbar \Omega = 25 \text{ meV} \). Both the excitonic fraction and the

FIG. 4. Polariton population on the ground state and other low-energy states for the exciton-box trap with \( D = 10 \mu \text{m} \), an exciton-photon coupling of \( \hbar \Omega = 48 \text{ meV} \), and an exciton-recombination energy of \( E_{X0} = 1.59 \text{ eV} \). The QW width is 4 nm, and the barrier-layer width is 5 nm. The detuning is \( \Delta = 30 \text{ meV} \) and \( \Delta = 40 \text{ meV} \). (a) Population of the ground state (GS) vs polariton density (solid curve). The rapid, nonlinear increase of the GS population indicates the BEC transition. The GS population fraction (dashed curve), i.e., the GS population divided by the total population, is of order unity for densities beyond the BEC transition. (b) GS population fraction (dashed curves) and the population fraction on the low-energy discrete states (solid curves) below the continuum exciton-recombination energy \( E_{X0} \). (There are more than 1000 such states.) These low-energy states are photonlike states with very small effective mass, whereas states higher than \( E_{X0} \) are excitonlike. When a large population fraction resides in the photonlike states, the BEC threshold density is reduced. For \( T = 100 \text{ K} \) (blue curves), populated polariton states are mostly photonlike. The threshold density is much lower than for \( T = 300 \text{ K} \) (brown curves), where the population fraction on low-energy states is negligible. (c) The dispersion of polaritons (solid red curves), bare excitons (dashed green curve), and pure photons (dash-dotted blue curve) for detuning \( \Delta = 40 \text{ meV} \) with \( q_x = \pi/a = 8.6 \mu \text{m}^{-1} \) for \( a = 370 \text{ nm} \). The dispersion depth of the lower polariton branch \( V \) is also depicted. (The dotted black line denotes the lower polariton band edge.) Inset: Excitonic fraction of the lower polariton branch as a function of detuning \( \Delta \).

(d) The dispersion depth \( V \) (solid red curve) and polariton effective mass \( m_{\text{eff}} \) (dashed green curve) of the lower polariton branch vs the detuning \( \Delta \).
effective mass of the lower-polariton dispersion minimum decrease with detuning \( \Delta \), as shown in the inset of Fig. 4(c) and in Fig. 4(d), respectively.

We calculate the polariton BEC transition temperature \( T_c \) for various QW widths, exciton-trap sizes, detunings, and exciton-photon couplings for a fixed polariton density. The results are plotted in Fig. 5. Clearly, room-temperature polariton BEC is attainable at overall polariton density \( \gtrsim 3 \times 10^3 \mu m^{-2} \) which is well below the saturation density in each QW of \( (5a_B)^{-2} \), where \( a_B \) is the exciton Bohr radius. The transition temperature is higher for smaller QW width since a larger number of QWs can be used. It is likewise higher for larger exciton-photon coupling and positive detuning which is consistent with the picture that \( T_c \) is limited by the dispersion depth \( V \). For large trap sizes \( D \gg 10 \mu m \), \( T_c \) decreases as expected from the Mermin-Wagner theorem [72] that forbids finite-temperature BEC in an infinite 2D system. However, this decrease is very slow and little degradation in \( T_c \) is seen over the range of \( 10 \mu m < D < 1 \) cm. Interestingly, the exciton-trap-size dependence of \( T_c \) for smaller \( D \) is nonmonotonic: \( T_c \) has a peak value around a box size \( D = 5 \mu m \). When the exciton-trap size is sufficiently small, the quantization energy of the cavity (e.g., the energy difference between the first excited state and the ground state) can be comparable to or larger than the dispersion depth \( V \). The condensation then crosses over from polaritonlike to excitonlike. Since the exciton effective mass is much larger than that of the polariton, the transition temperature is rapidly reduced.

The polariton density used in our calculation is experimentally accessible. For MQWs, the total exciton density is distributed among the QWs and the excitonic fraction in each QW of a polariton may be much less than unity. For example, using \( N = 100 \) QWs, each of width 4 nm and barrier width 5 nm (i.e., \( \hbar \omega_0 = 1.56 \) eV and \( E_{X0} = 1.59 \) eV with \( a = 365 \) nm and \( a_B = 3.8 \) nm), the collective exciton-photon coupling is 48 meV. For a detuning of \( \Delta = 30 \) meV, the largest excitonic fraction in any single QW is 5.5%. [The exciton fraction varies among QWs since the exciton-photon coupling for each QW is different; see Eq. (3)] For total polariton density \( 1.5 \times 10^4 \mu m^{-2} \), the exciton density in each QW is no larger than \((9a_B)^{-2}\), where \( a_B \) is the exciton Bohr radius. This single QW exciton density is less than the saturation density \([28,44] = (5a_B)^{-2}\).

![FIG. 5. Polariton BEC transition temperature \( T_c \) at fixed densities. (a) Transition temperature \( T_c \) with detuning \( \Delta = 30 \) meV for different QW widths (with QWs filling an entire active region) at fixed polariton densities: \( 1.5 \times 10^4 \mu m^{-2} \) (curve with solid circles) and \( 1.9 \times 10^3 \mu m^{-2} \) (curve with solid squares). For the higher total density, the exciton density in each QW is below \( (9a_B)^{-2}\). For the lower total density, the exciton density in each QW is below \( (26a_B)^{-2}\). (b) Dependence of the transition temperature \( T_c \) on the detuning \( \Delta \) and the exciton-trap size \( D \) when the exciton-photon coupling is \( h\Omega = 48 \) meV (QW width 4 nm and barrier width 5 nm) and the polariton density is \( 3 \times 10^3 \mu m^{-2} \). (c) Dependence of the transition temperature \( T_c \) on the detuning \( \Delta \) and the exciton-photon coupling \( h\Omega \) when the exciton-trap size is \( D = 10 \mu m \) and the polariton density is \( 3 \times 10^3 \mu m^{-2} \).](image1)

![FIG. 6. BEC transition temperature \( T_c \) as a function of total polariton density and (a) box-trap size, (b) exciton-photon detuning, and (c) exciton-photon-coupling strength. (d) Root-mean-square deviation of the vacuum Rabi splitting (diamonds) and lower-polariton dispersion depth (circles) as a function of exciton inhomogeneous broadening \( \delta E_{X0} \). In (a) and (b), the exciton-photon coupling is \( h\Omega = 48 \) meV (QW width 4 nm and barrier width 5 nm). For (a) and (c), the detuning is 30 meV. For (b) and (c), the exciton-box-trap size is 10 \mu m. The exciton-recombination energy is \( E_{X0} = 1.59 \) eV. For (d), the detuning is \( \Delta = 0 \). The dashed curve in (d) depicts the value of \( \delta E_{X0} \) itself for reference.](image2)
Systematic dependence of the BEC transition temperature on the total polariton density is shown in Fig. 6. Figure 6(a) reveals that the exciton-trap-size dependence of $T_c$ is much more pronounced at low polariton density, where the transition temperature is much smaller than $V/k_B$. Here, most polaritons are low-energy photonlike states with very small effective mass. The transition temperature at fixed density is limited mainly by the level spacing between the ground and first excited states [18,71], which depends sensitively on the exciton-trap size. In contrast, at high polariton density, the transition temperature is close to $V/k_B$. When the dispersion depth $V$ is the main factor limiting $T_c$, the exciton-trap size has marginal influence. Figures 6(b) and 6(c) reveal that large detuning and/or exciton-photon coupling is favorable for room-temperature polariton BEC because both of them enhance the dispersion depth $V$ [see Fig. 4(d)].

Finally, we discuss the effect of fabrication disorder which can randomize sensitive parameters such as the detuning $\Delta$ and the collective exciton-photon coupling $\hbar \Omega$. We show that the former effect is more significant. Photonic disorder arises from fluctuation of the shape and size of the rods and slabs constituting the photonic crystal. Electronic disorder arises from impurities, dislocations, (local) QW width fluctuation, random strains, etc. In addition to these forms of inhomogeneous broadening, dynamic fluctuations (homogeneous broadening) arise from phonon-polariton and polariton-polariton interactions which are particularly important at high temperatures.

Plane-wave-expansion calculation indicates that the 2D photonic band edge varies by less than 2% of its value if the fabrication error is smaller than 20 nm for woodpile rods outside the active region, less than 12 nm for rods in the active woodpile region, and less than 6 nm for the central slab thickness. The effect of electronic disorder has been studied earlier [62] for the single QW case, where it was found that polaritons remain robust due to their small effective mass and highly mobile half-photon nature. Electronic scale disorder is largely averaged out in a scenario similar to motional narrowing [62].

For the MQW structures studied here, there are also fluctuations of exciton energy among QWs due to variations in QW width or lateral confinement of the rods. This broadening is modeled by adding a random energy $\delta E_i$ to the exciton dispersion in the $l$th QW $E_X^{(l)}(\Omega) = E_{X_0} + \hbar^2 q^2/(2 m^*_X) + \delta E_i$. $\delta E_i$ is modeled as a Gaussian random variable with variance $(\delta E_{X_0})^2$. The effects of this disorder on vacuum Rabi splitting $2\hbar \Omega$ and polariton-dispersion depth $V$ are presented in Fig. 6(d). The calculation is performed by averaging over $10^5$ random configurations. The standard deviation of the vacuum Rabi splitting is very small due to the collective nature of the polariton. The fluctuation in polariton energy consists of the sum of random exciton-energy variations from each of the $N$ QWs. The total effect is an average effect that has a much smaller variance, according to the central limit theorem [46] $\frac{\sigma^{\prime}}{\sqrt{N}} \sim \mathcal{O}(1/\sqrt{N})$.

The fluctuation of the polariton-dispersion depth $V$ is approximately the same as the inhomogeneous broadening of the exciton $\delta E_{X_0}$. The randomization of the detuning $\Delta$ directly affects this dispersion depth [see Eq. (8)]. This effect is much more significant than the fluctuation of the vacuum Rabi splitting $2\hbar \Omega$. Experimental measurements in a single CdTe-CdMgTe QW give a typical inhomogeneous broadening of 1 meV [33]. Hence, intra-QW inhomogeneous broadening can be rendered small with present-day fabrication capabilities. Inter-QW inhomogeneous broadening estimated from the lateral confinement difference for QWs in rods and in the central slab is less than 1 meV as well.

Finally, dynamic fluctuations (such as polariton-phonon and polariton-polariton scattering) cause both homogeneous broadening and the relaxation of polaritons. The latter is crucial for polaritons to reach the ground state and achieve thermal equilibrium BEC. However, homogeneous broadening reduces the polariton-dispersion depth $V$, and consequently, $T_c$. In CdTe QWs, at room temperature, experiments [55] suggest a homogeneous linewidth of $\Gamma = 22$ meV (see the Appendix). The broadening of the cavity photon is negligible for high-quality-factor ($2 \times 10^6$ as shown in Ref. [53]) photonic crystal microcavities. If we estimate the effect of homogeneous broadening by adding an imaginary part $i \Gamma$ to the exciton energy, the vacuum Rabi splitting at zero detuning ($\Delta = 0$) is reduced to $2\sqrt{\hbar^2 \Omega^2 - \Gamma^2}/4$ [73]. More importantly, the dispersion depth of the lower polariton for nonzero detuning becomes

$$V = \frac{\Delta}{2} + \text{Re} \sqrt{\left(\frac{\Delta - i \Gamma}{2}\right)^2 + \hbar^2 \Omega^2}.$$ 

In general, exciton-phonon interaction reduces the dispersion depth $V$. However, for $\Delta = 30$ meV, $\hbar \Omega = 48$ meV, and $\Gamma = 22$ meV, the lower-polariton dispersion depth is reduced by only 1.1 meV which is equivalent to a reduction of detuning by 2 meV and has negligible effects on the transition temperature, according to Fig. 6(b). These results suggest that our very strongly coupled exciton-photon system can withstand considerable homogeneous and inhomogeneous broadening and still deliver equilibrium room-temperature polariton BEC.

V. CONCLUSION

In summary, we have identified a CdTe-based photonic band-gap architecture with a range of different quantum-well embeddings that are predicted to support room-temperature (or higher) equilibrium Bose-Einstein condensation of exciton polaritons. The most crucial factors in enabling high-temperature BEC are the dispersion depth of the lower polariton branch and the...
total areal density of long-lived excitons within the trapping region. The dispersion depth is determined by the collective exciton-photon-coupling strength and is enhanced by detuning the bare exciton-recombination energy above the lower edge of a slow-light, 2D guided photonic band within the larger 3D photonic band gap. The 3D PBG enables considerably stronger light trapping than conventional 1D Fabry-Pérot microcavities, leading to stronger exciton-photon coupling. The collective exciton-phonon-coupling strength is further enhanced by embedding up to about 100 quantum wells in the photonic crystal regions adjacent to a central slab region containing two principal quantum wells. Positive detuning of the exciton-recombination energy relative to the strongly coupled photon mode is made possible by the 3D PBG. The positively detuned exciton remains within the 3D PBG and it cannot decay radiatively into extraneous optical modes that leave the system.

The total areal density of excitons is enhanced by distributing them over a large number of quantum wells that are all strongly coupled to the 2D guided mode within the 3D PBG. The use of CdTe-based architectures offers a suitable balance between photonic and electronic properties. The relatively low dielectric constant of CdTe compared to other popular materials (such as GaAs) enables a small exciton Bohr radius and higher saturation exciton density. Nevertheless, the dielectric constant is sufficiently large enough to facilitate a 3D PBG that encompasses the lower-polariton dispersion depth and provides strong 3D light confinement.

Our calculations of the BEC transition temperature are based on a noninteracting polariton gas confined in a 2D box trap. Previous studies [18] have shown that a slight reduction in the BEC transition, together with polariton antibunching effects, are expected when exciton-exciton interactions are included in the microscopic Hamiltonian. While a box trap of 5-μm side length is predicted to yield the highest BEC transition temperature, very little degradation of $T_c$ is seen for box dimensions up to 1 cm when polariton density is high. This result suggests that BEC may be observable in a finite-size photonic crystal up to centimeter-scale lateral dimension, without recourse to a separately engineered 2D trap.

It is significant that for total polariton densities approaching $10^4$ μm$^{-2}$, the exciton density per quantum well remains below $(10 a_B)^{-2}$, where $a_B$ is the exciton Bohr radius. At these densities, our PBG architecture provides sufficiently strong exciton-photon coupling and polariton-dispersion depth to provide a predicted BEC transition as high as 500 K, in the absence of additional homogeneous and inhomogeneous broadening effects. This architecture offers a safe margin for the realization of room-temperature BEC in realistic systems with both foreseen and unforeseen fabrication imperfections, exciton-phonon-scattering processes, and other damping effects. In this way, the photonic band-gap architecture provides a realistic prospect of bringing the magic of macroscopic quantum mechanics to the realm of everyday experience.

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APPENDIX: CALCULATION METHODS AND DETAILS

The spectrum and wave function of the photonic bands are calculated by solving the Maxwell equations using the plane-wave-expansion method [60]. In calculating the photonic bands in the Cd$_{0.4}$ Mg$_{0.6}$Te-Cd$_{0.4}$Mn$_{0.6}$Te Fabry-Pérot cavity, the dielectric constant for Cd$_{0.4}$ Mg$_{0.6}$Te is 7.0 (linear interpolation between the dielectric constant of CdTe is 8.5 [49], and that of MgTe is 6.0 [50]), while the dielectric constant of Cd$_{0.8}$Mn$_{0.2}$Te is 7.8 [74]. The electronic structures are calculated using the effective mass approximation [45]. The effective mass of the electron is $m_e = 0.095 m_0$, with $m_0$ being the bare electron mass in vacuum [58]. For the [001]-grown QWs concerned in this work, the heavy-hole effective mass along the growth direction is 0.6$m_0$ [75], while the effective mass in the QW plane is $m_h = 0.4 m_0$ [48]. The energy and wave functions of the electron and hole subbands are calculated using a finite-depth well model [45]. The electronic band gap of CdTe is $E_g = 1.475$ eV [58,76], while the electronic band gap for MgTe is 3.49 eV [77]. Linear interpolation yields the band gap of Cd$_{0.6}$ Mg$_{0.4}$Te as 2.28 eV. The band-gap difference between Cd$_{0.6}$ Mg$_{0.4}$Te and CdTe is 0.8 eV. The offset for the conduction band between those two materials is 70% of their band-gap difference [78]. The interband dipole-matrix element is given by

$$d = \frac{\epsilon \hbar \sqrt{E_{CV}}}{E_g / 2 m_0},$$

(A1)

where $E_{CV} = 2P_{CV}^2 / m_0$ is the energy related to the momentum-matrix element $P_{CV}$ between the conduction and valence bands. From Ref. [78], we take $E_{CV} = 21$ eV. Material parameters in the above are taken for room temperature.

The exciton spectrum and wave functions are calculated by diagonalizing the exciton Hamiltonian. For our narrow QWs, we consider only the excitons formed by electrons and holes in their lowest subband [43]. We ignore the mixing with higher subbands and numerically diagonalize the exciton Hamiltonian within the lowest subband. This calculation yields an exciton-binding energy comparable to the experimentally observed one. The exciton wave amplitude $|\phi(0)|$ and exciton Bohr radius are also obtained, using the same considerations.
The Auger recombination time $\tau_A$ is estimated using the method presented in Ref. [66]. For a volume exciton density of $10^{17} \text{ cm}^{-3}$ (volume density of excitons corresponding to an areal polariton density of $10^4 \text{ cm}^{-2}$, estimated by dividing the areal polariton density by the thickness of the active region) in CdTe, $\tau_A = 10^{-3} \text{ s}$. This very small Auger recombination rate is due to the large band gap and small carrier density. Another nonradiative decay mechanism is the Shockley-Read-Hall mechanism due to electronic trapping centers within the semiconductor band gap. However, experiments in high-quality CdTe QWs have shown a photoluminescence-decay time of 150 ps at room temperature [54] which places a lower bound on the nonradiative decay time.

The polariton-thermalization time is estimated as follows. Experiments [55] have found that exciton homogeneous broadening at high temperature is dominated by interactions with longitudinal-optical (LO) phonons. The exciton linewidth is given by $\Delta E_{\text{LO}}/[\exp(E_{\text{LO}}/k_B T) - 1]$, where $E_{\text{LO}} = 21.3 \text{ meV}$ is the LO phonon energy [58] and the parameter $A_{\text{LO}} = 15 \text{ meV}$ is fitted from the measured temperature dependence of the exciton linewidth in Ref. [55]. Using this result, we estimate that the exciton linewidth due to LO phonon scattering at $T = 300 \text{ K}$ is 22 meV. This result suggests a polariton linewidth at zero detuning ($\Delta = 0$) of 11 meV (the exciton fraction of the polariton is 50%) and corresponds to a subpicosecond thermalization time. For positive detuning, if the exciton fraction in the polariton remains larger than 10%, then the thermalization time is below or around 1 ps. This timescale is considerably smaller than the nonradiative decay time of the polariton and suggests that the polariton gas has sufficient time to reach thermal equilibrium.


PHOTONIC CRYSTAL ARCHITECTURE FOR ROOM-