

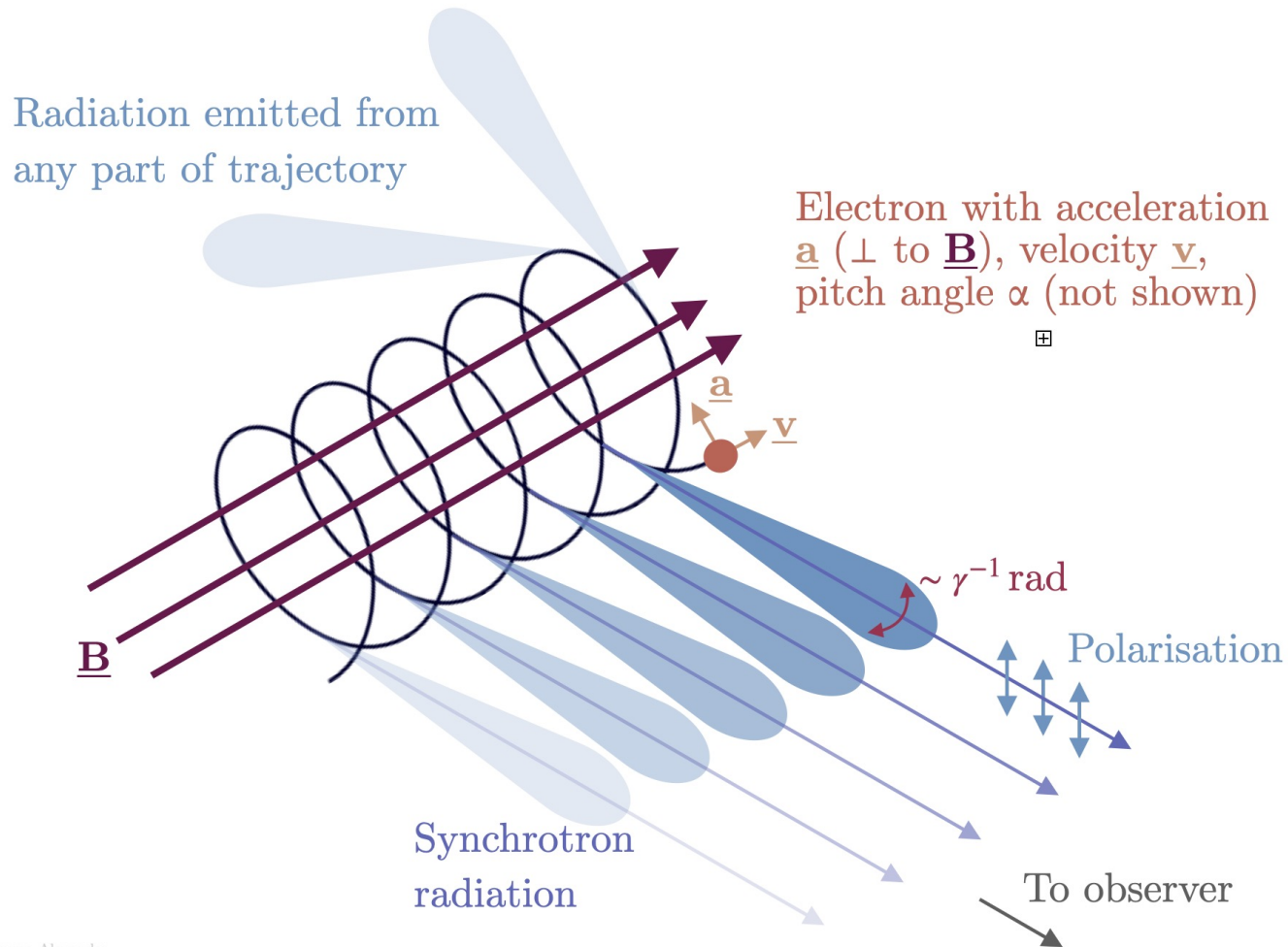
Future Colliders

W. Trischuk

~~January 23, 2019~~

January 18, 2024

Synchrotron Radiation



A direct consequence of [Maxwell's equations](#) is that accelerated charged particles always emit electromagnetic radiation. Synchrotron radiation is the special case of charged particles moving at relativistic speed undergoing acceleration perpendicular to their direction of motion, typically in a magnetic field. In such a field, the force due to the field is always perpendicular to both the direction of motion and to the direction of field, as shown by the [Lorentz force law](#).

The power carried by the radiation is found (in [SI units](#)) by the [relativistic Larmor formula](#).^{[9][10]}

$$P_{\gamma} = \frac{q^2}{6\pi\epsilon_0 c^3} a^2 \gamma^4 = \frac{q^2 c}{6\pi\epsilon_0} \frac{\beta^4 \gamma^4}{\rho^2},$$

where

- ϵ_0 is the [vacuum permittivity](#),
- q is the particle charge,
- a is the magnitude of the acceleration,
- c is the speed of light,
- γ is the [Lorentz factor](#),
- $\beta = v/c$,
- ρ is the [radius of curvature](#) of the particle trajectory.

Jackson E&M
(Chapter 14)

The force on the emitting electron is given by the [Abraham–Lorentz–Dirac force](#).

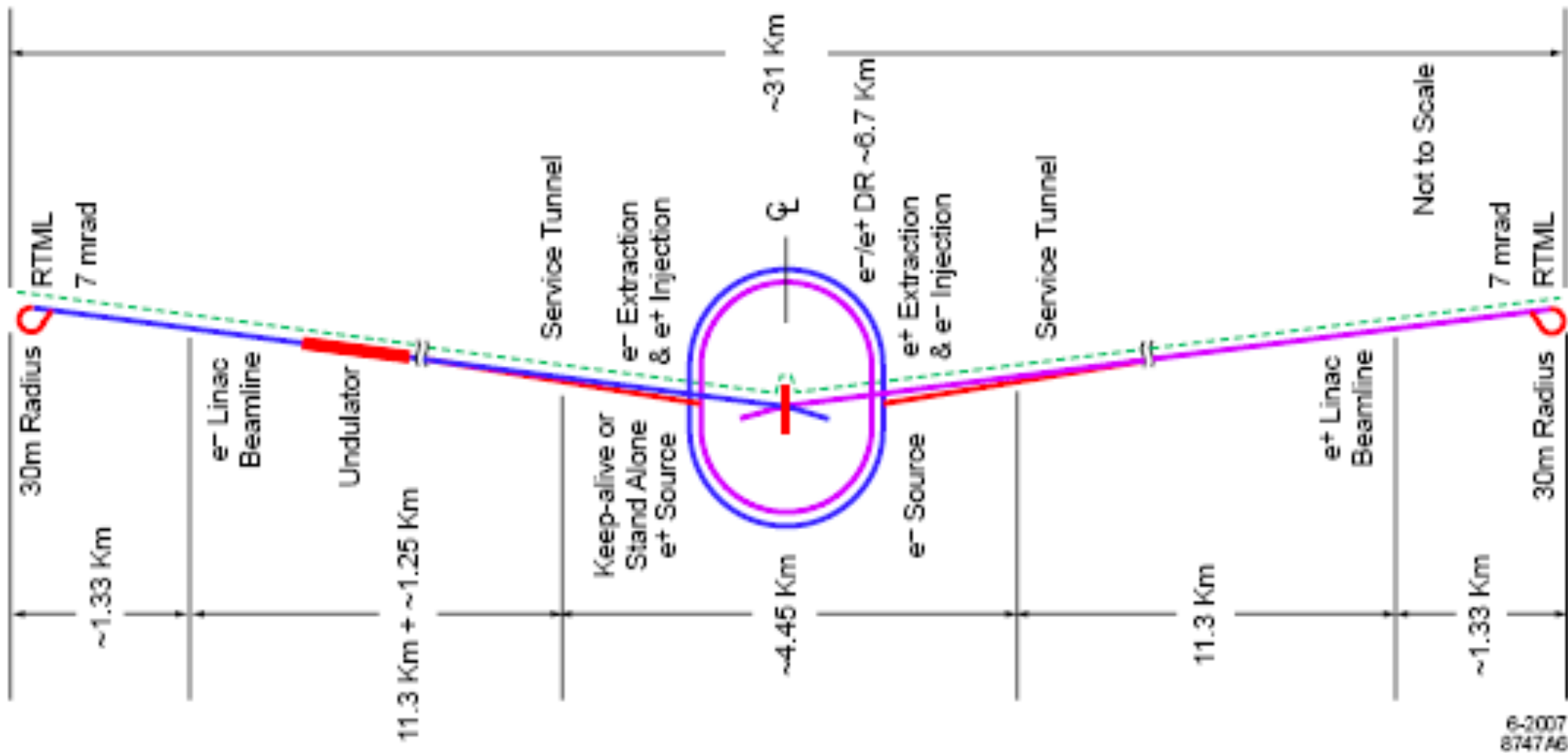
Lepton vs. Proton Colliders

- Colliding electrons
 - Puts all the beam energy in to the collision
 - Limited by energies you can reach
 - Circular electron colliders limited by synchrotron radiation
 - **Linear colliders** limited by only colliding each accelerated bunch once
- Colliding protons
 - Quarks/gluons on carry a fraction of beam energy
 - Synchrotron losses are much lower (go like γ^4)
 - Still non-negligible energy/power at LHC – ends up in superC magnets
- Colliding muons
 - Might be best of both worlds
 - Point like projectiles, 200x higher mass (10^9 less synchrotron rad)
 - But muons only have a 2us lifetime...

Summary of Future Colliders

- ILC/CLIC comparison (Zimmerman: CERN-ATS-2010-056)
 - Linear colliders don't have synchrotron radiation limits
 - But can only use each accelerated bunch “once”.
- Circular colliders
 - Hadron machines (HE-LHC CDR: CERN-ACC-2018-0059)
 - Electron machines (Chinese Circular Collider)
- Muon collider
 - <https://cerncourier.com/a/sketching-out-a-muon-collider/>

ILC Layout



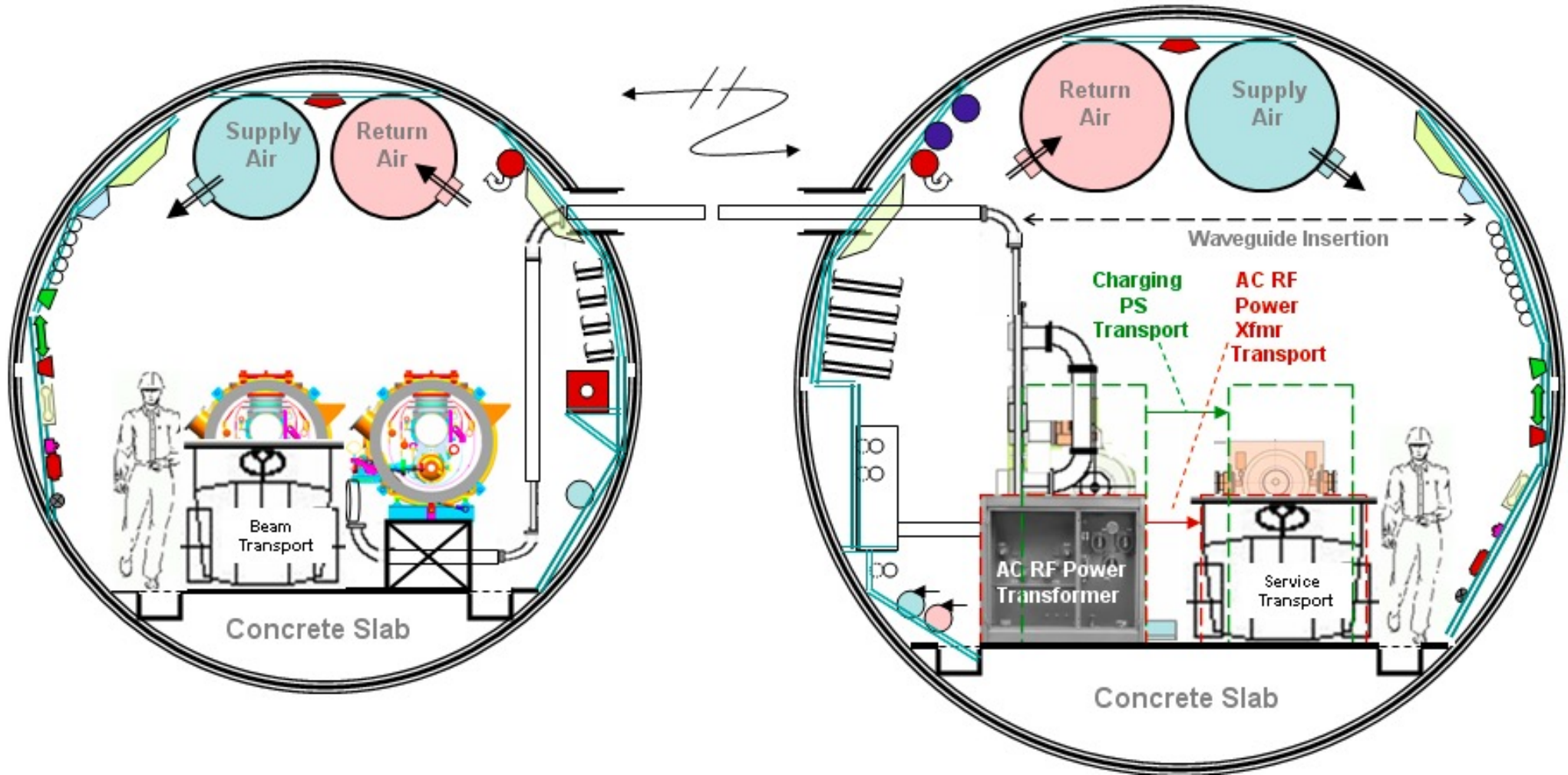
ILC/CLIC Comparison

Table 14: CLIC and ILC parameters [61,65].

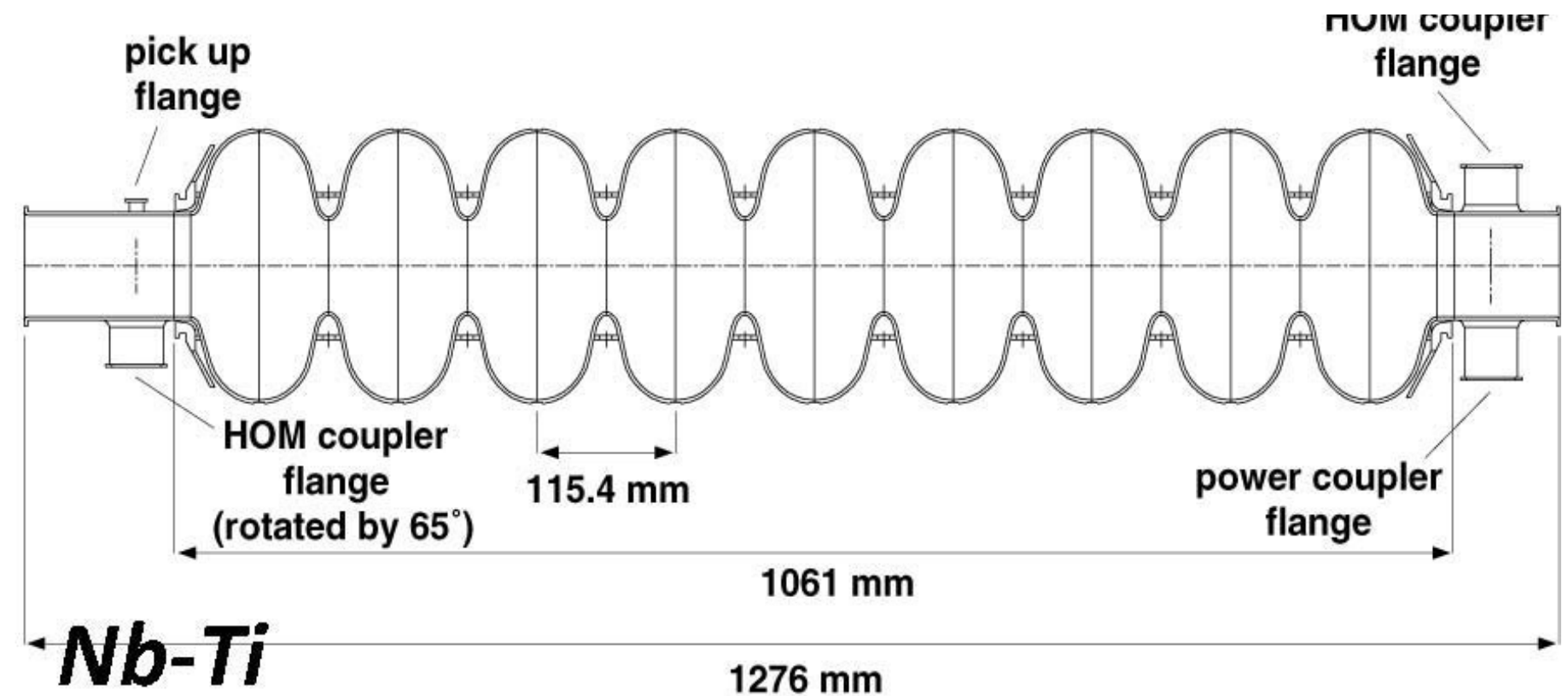
centre-of-mass energy	ILC 500 GeV	CLIC 500 GeV	CLIC 3 TeV
total (peak 1%) luminosity [$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$]	2(1.5)	2.3 (1.4)	5.9 (2.0)
repetition rate [Hz]	5	50	
loaded accelerating gradient [MV/m]	32	80	100
main linac RF frequency [GHz]	1.3	12	
particles per bunch [10^9]	20	6.8	3.7
bunch separation [ns]	370	0.5	
beam pulse duration [ns]	950,000	177	156
beam power / beam [MW]	10.8	4.9	14
horizontal/vertical IP beam size [nm]	639, 5.7	200, 2.3	40, 1.0
#hadronic events / crossing at IP	0.12	0.2	2.7
incoherent pairs at IP [10^3]	1.0	1.7	3.0
crossing angle [mrad]	14	18.6	20
beam delivery system length / beam [km]	2.23	1.87	2.75
total site length [km]	31	13	48
total electrical power consumption [MW]	230	130	415

Parameters		units	ILC(RDR)	CLIC(3 TeV)
Injection / final linac energy	E_{Linac}	GeV	25 / 250	9/ 1500
Acceleration gradient	E_a	MV/m	31.5	100
Average beam current	I_b	μA	42	9
Peak RF power	$P_{\text{in peak}}$	MW/m	0.37	275
Average RF power	$\langle P_{\text{in}} \rangle$	kW/m	2.9	3.7
Initial / final horizontal emittance	ε_x	μm	8.4 / 9.4	0.38/0.66
Initial / final vertical emittance	ε_y	nm	24 / 34	4/20
RF pulse width	T_p	μs	1565	0.24
Repetition rate	F_{rep}	Hz	5	50
Number of particles in a bunch	N	10^9	20	3.7
Number of bunches / train	N_b		2625	312
Bunch spacing	T_b	ns	360	0.5
Bunch spacing per RF cycle	T_b / T_{RF}		468	6

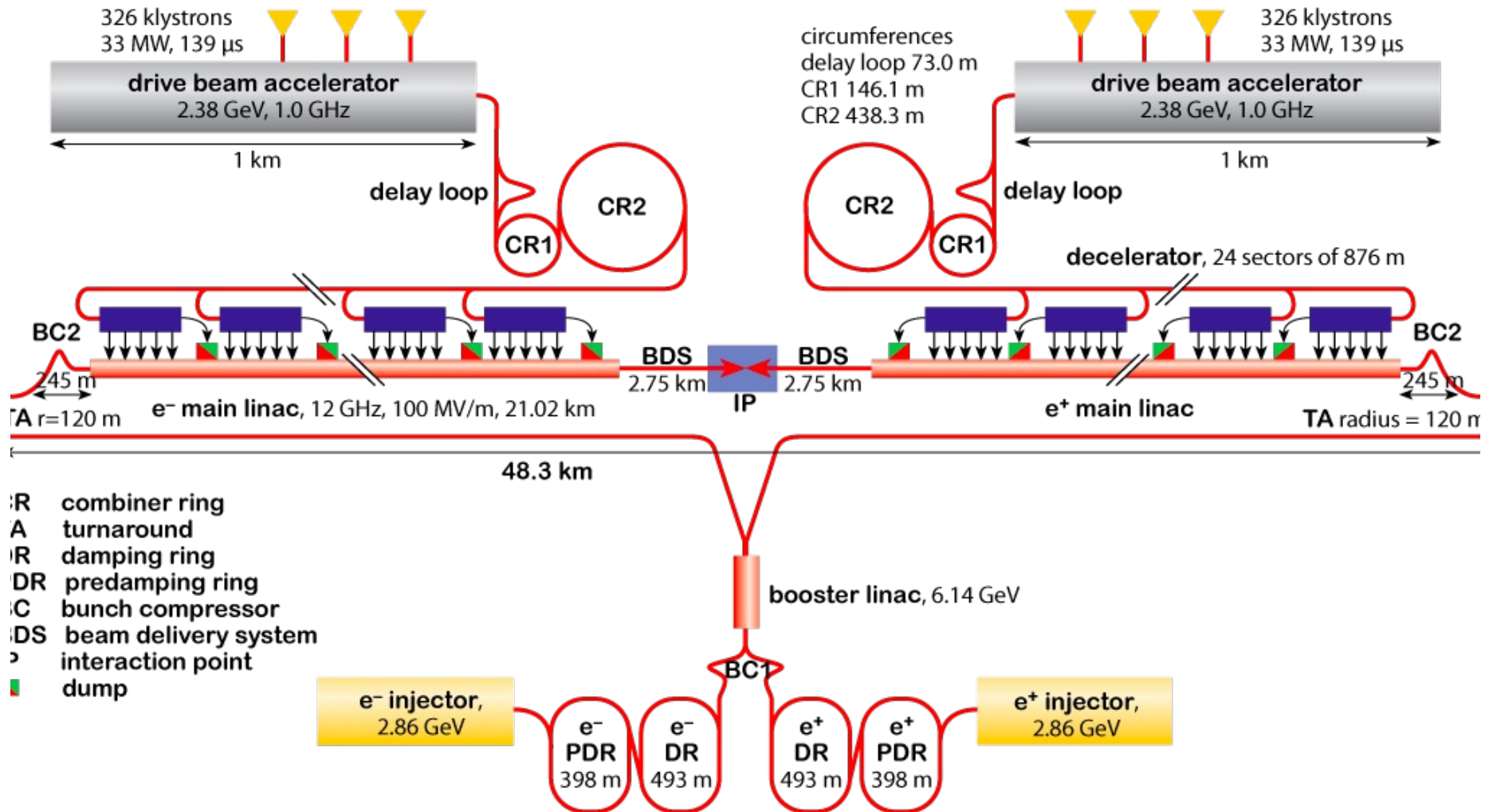
ILC tunnels



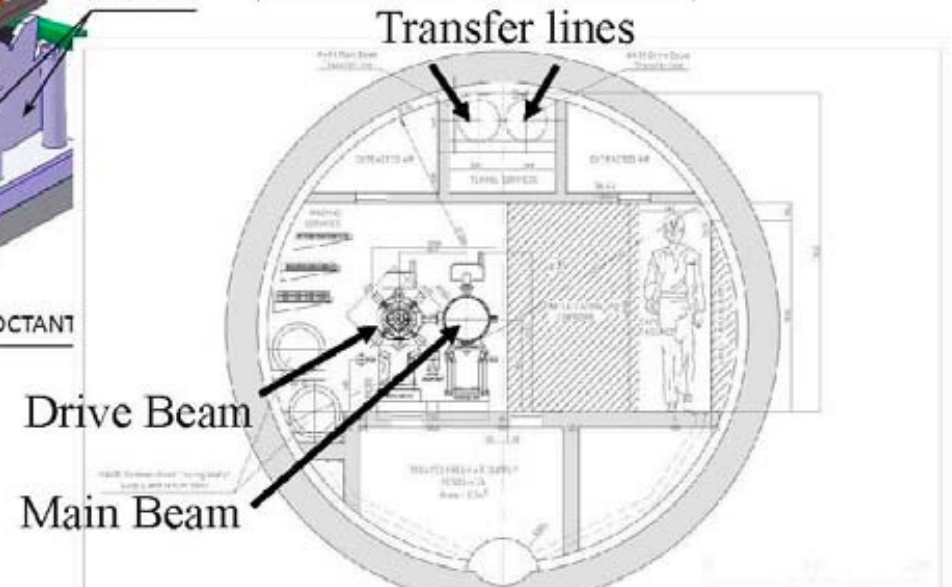
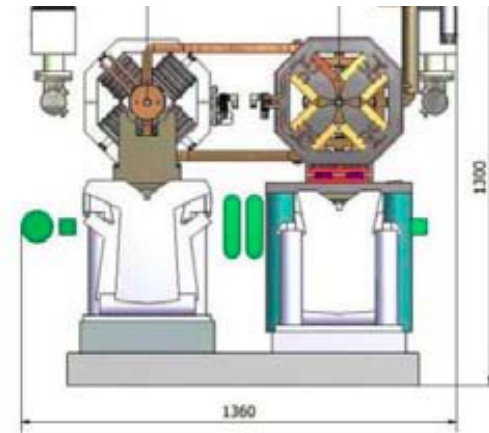
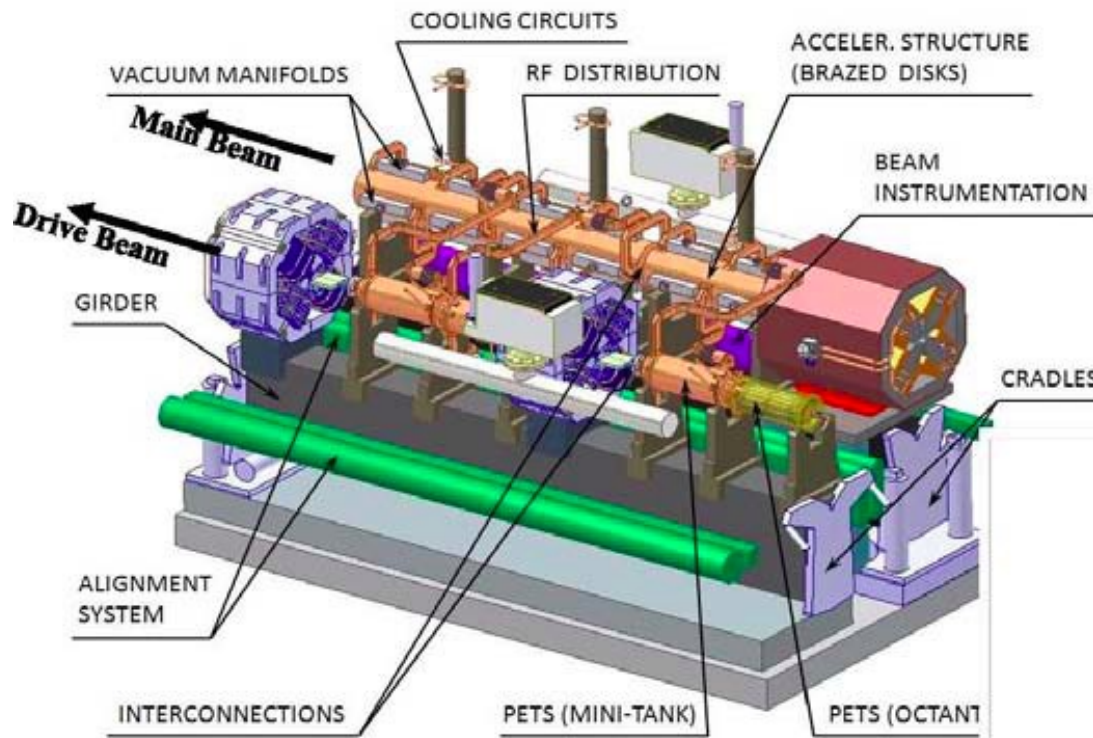
ILC Cavity



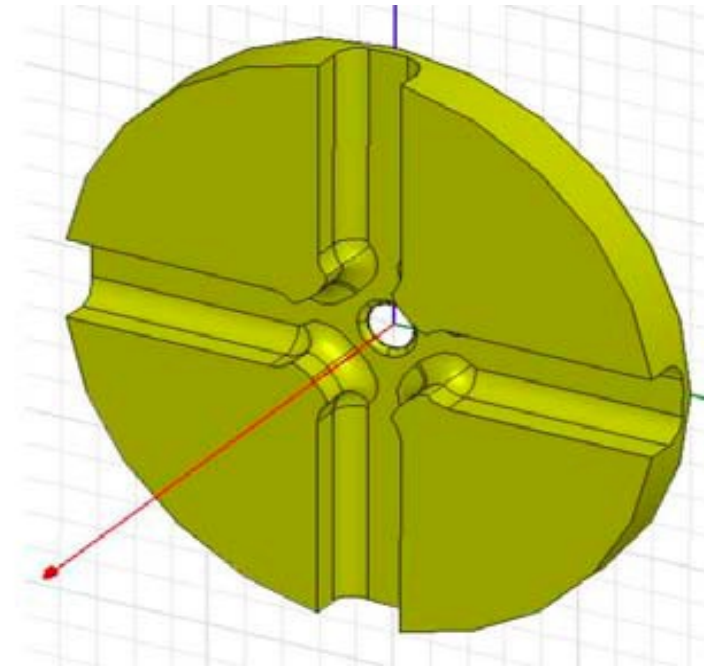
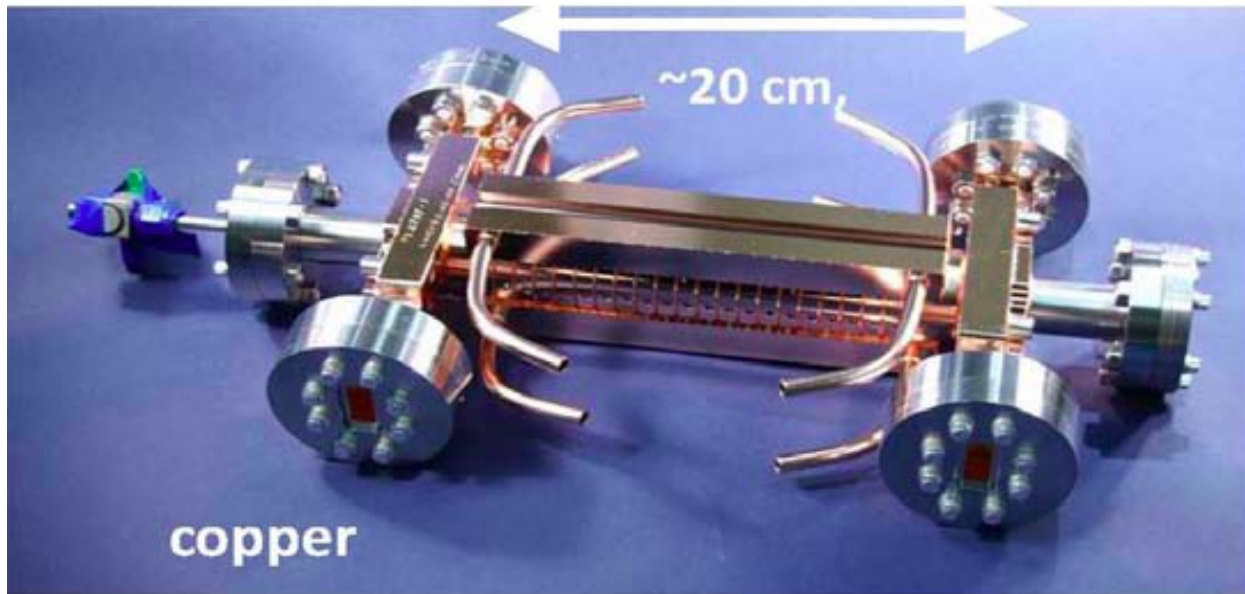
CLIC Layout



CLIC Layout

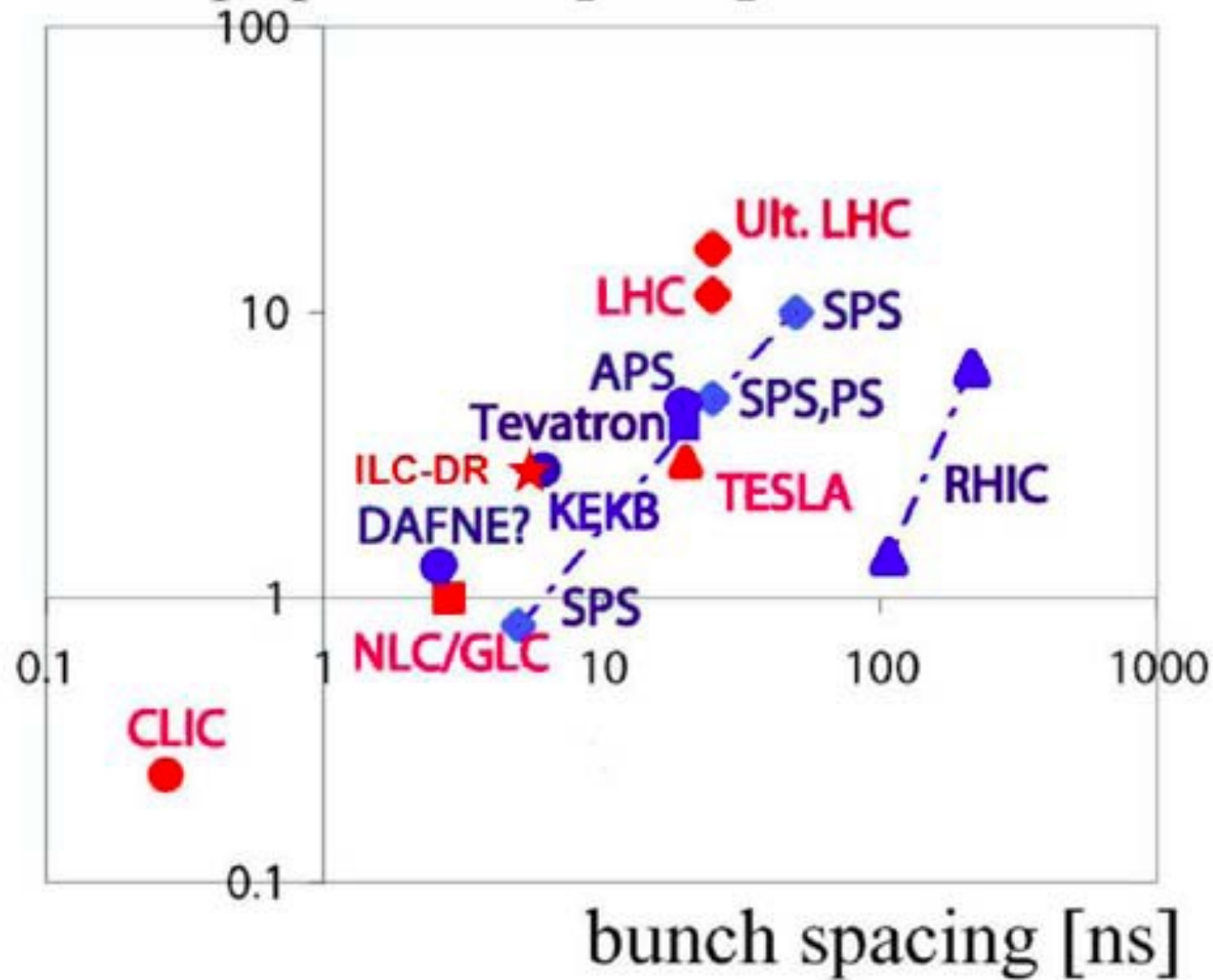


CLIC RF structure

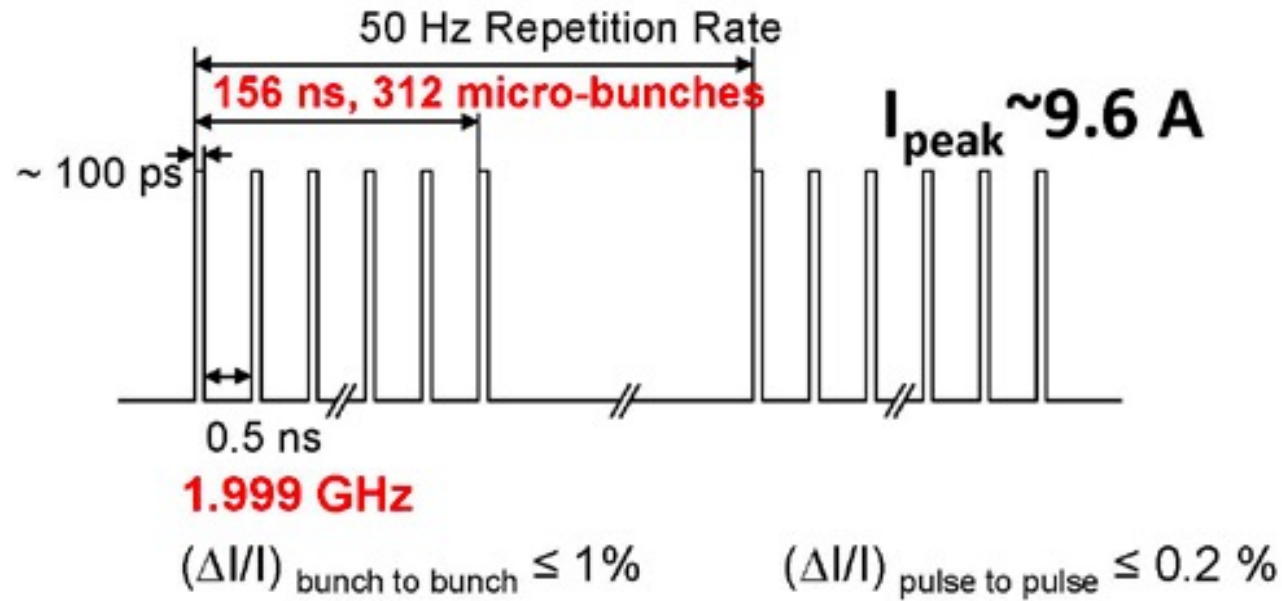


bunch population [10^{10}]

blue: e-cloud effect observed
red: planned accelerators



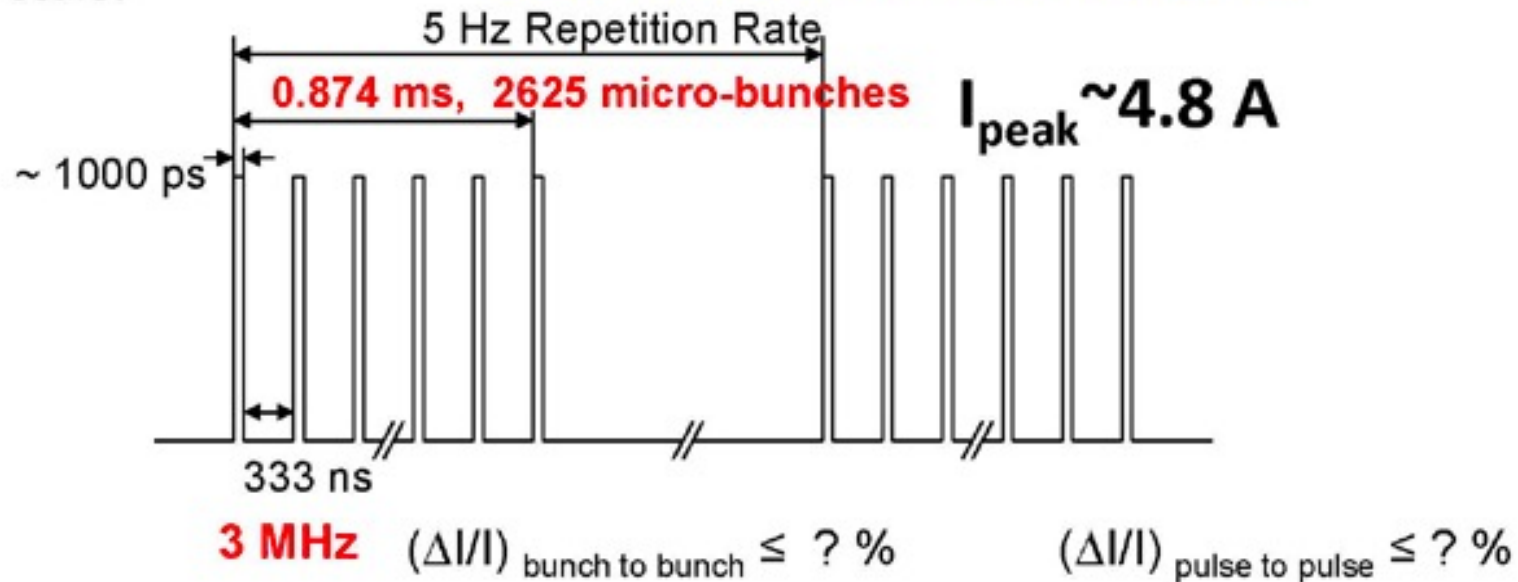
CLIC e⁻ beam time structure



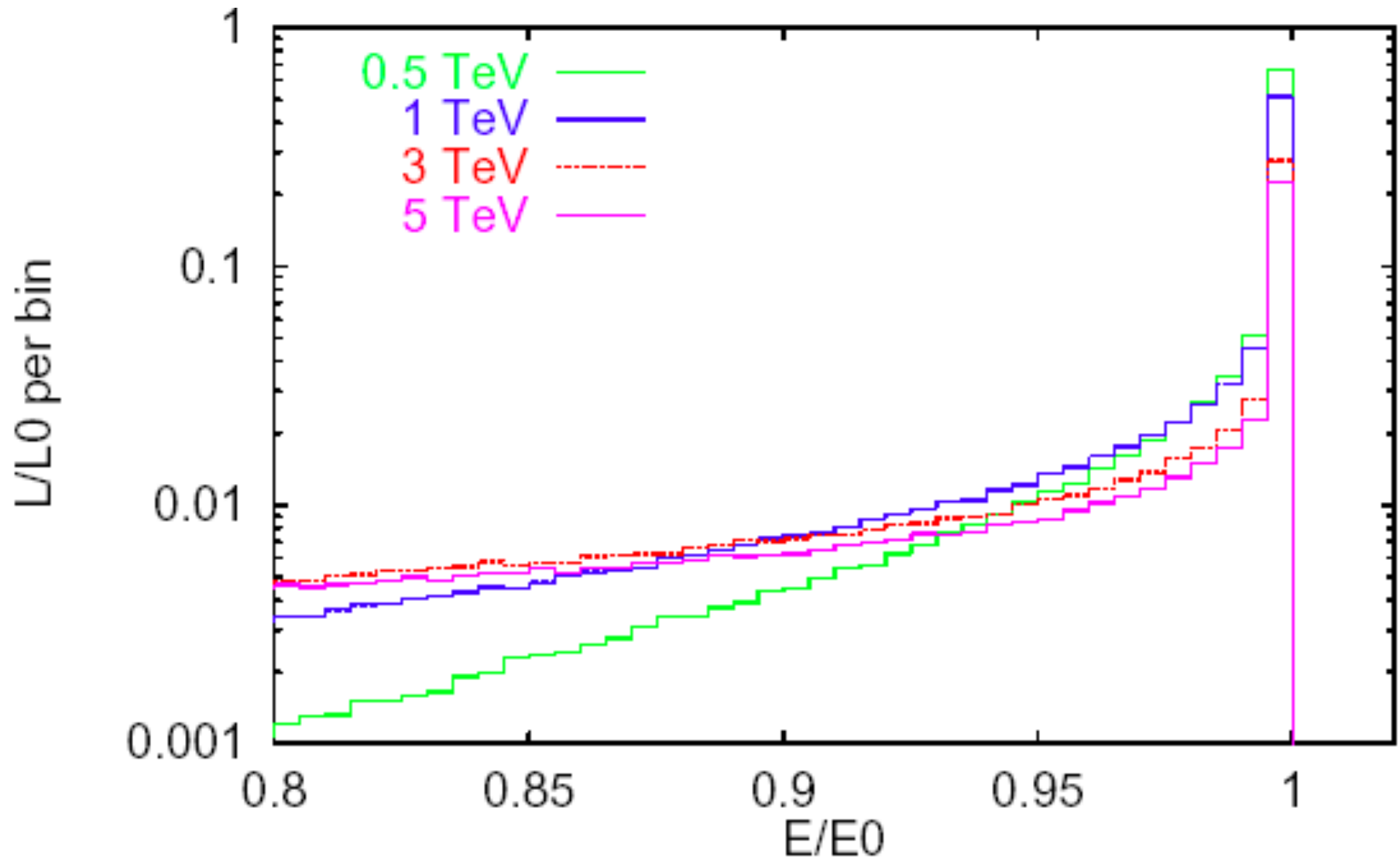
L. Rinolfi

not to scale!

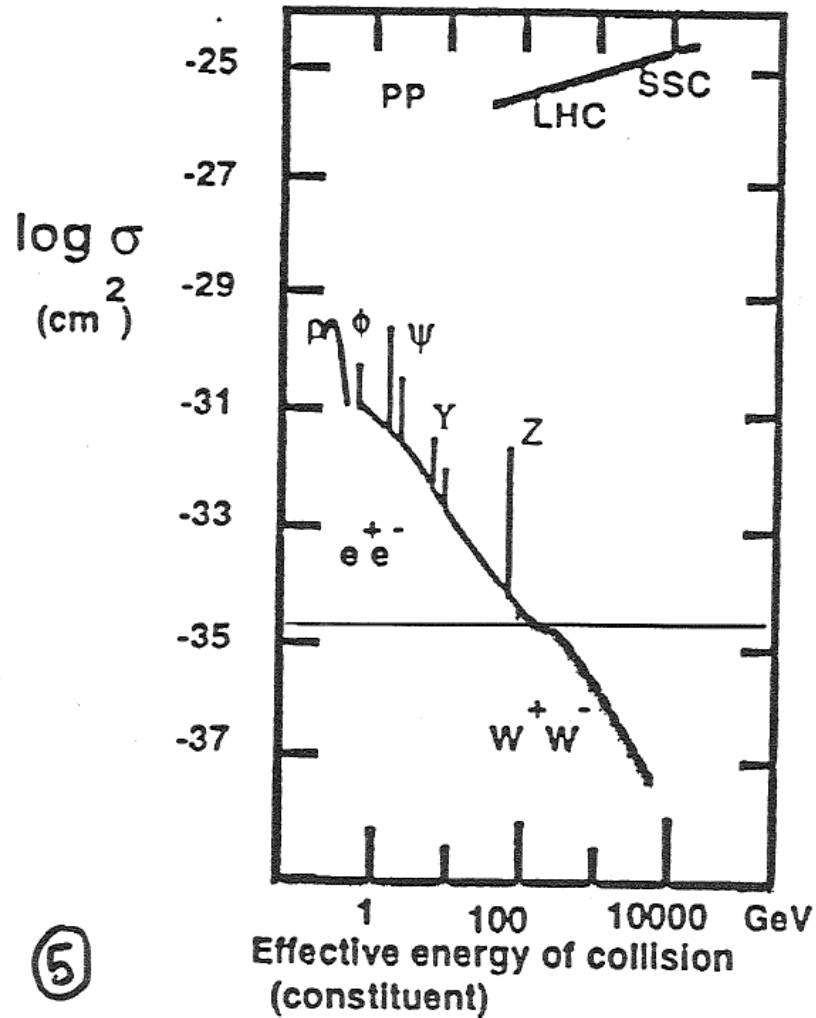
ILC e⁻ beam time structure



Collision Energy Dispersion (CLIC)



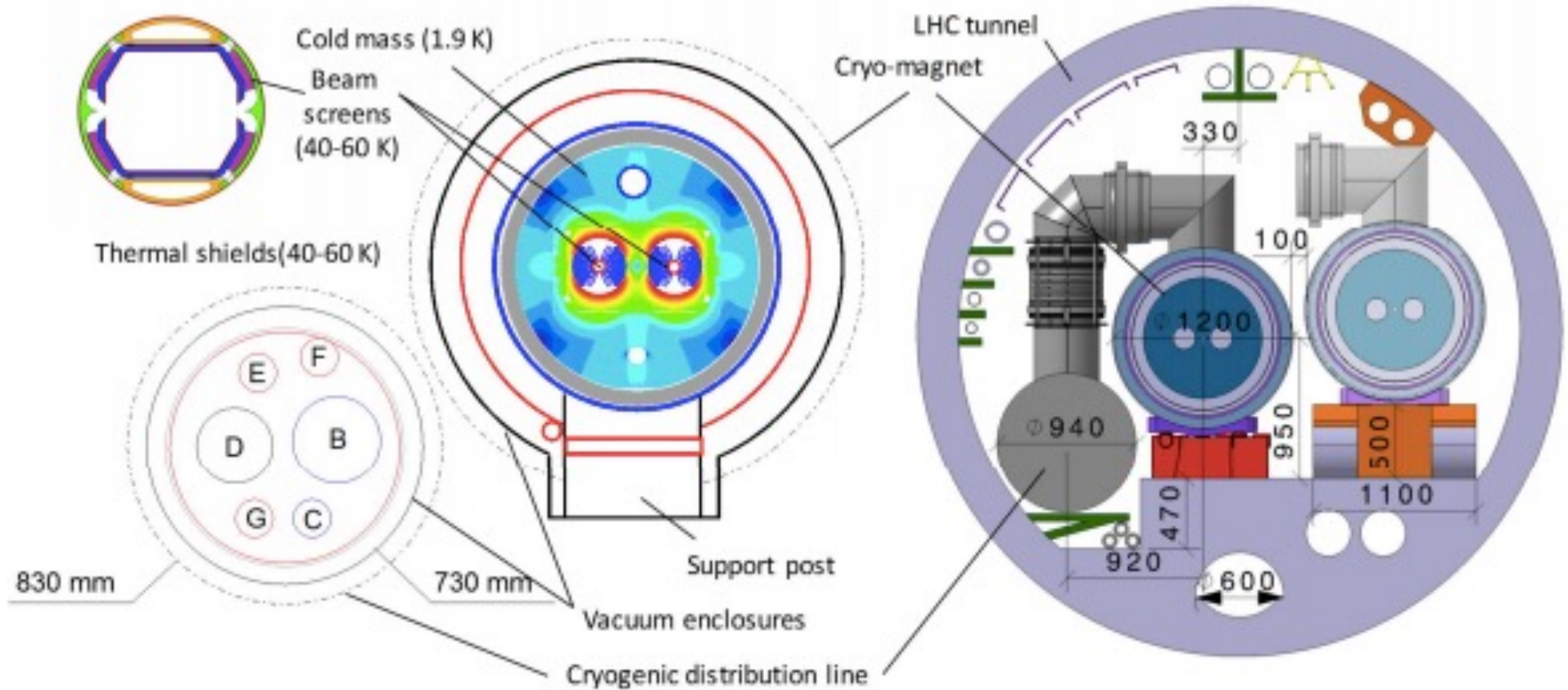
Future Hadron Colliders



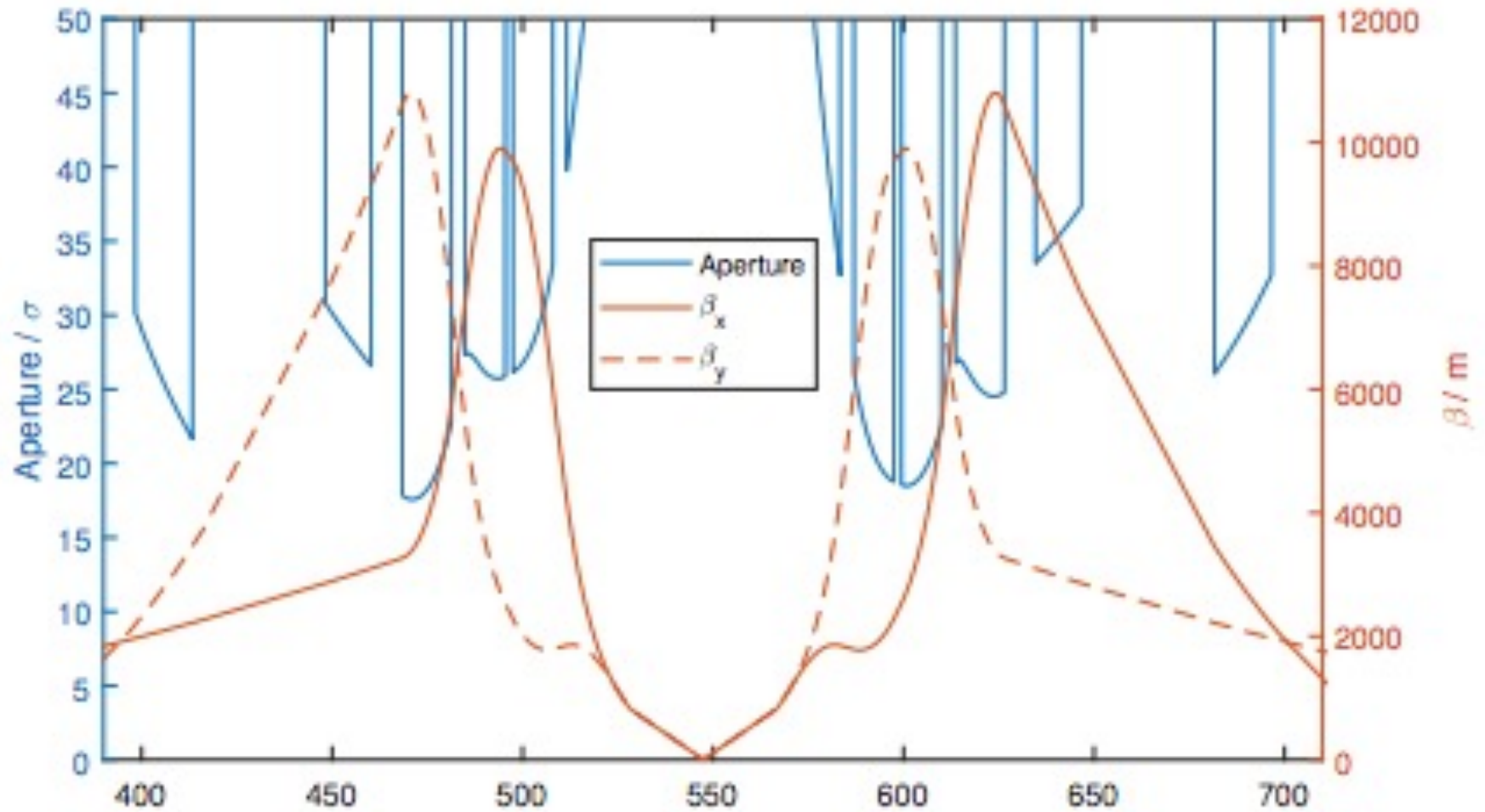
⑤

Parameter	Unit	FCC-hh		HE-LHC	(HL-)LHC
Centre-of-mass energy	TeV	100		27	14
Injection energy	TeV	3.3		1.3 (0.9, 0.45)	0.45
Peak arc dipole field	T	16		16	8.33
Circumference	km	97.8		26.7	26.7
Straight-section length	m	1400		528	528
Beam current	A	0.5		1.12	(1.12) 0.58
Bunch population	10^{11}	1.0		2.2	(2.2) 1.15
Number of bunches / beam	—	10400		2808	(2760) 2808
RF voltage	MV	32		16	(16) 16
RMS bunch length	mm	~ 80		90	(90) 75.5
Longitudinal emittance ($4\pi\sigma_x\sigma_E$)	eVs	~8		4.2	2.5
Bunch spacing	ns	25		25	25
Norm. transv. rms emittance	μm	2.2		2.5	(2.5) 3.75
IP beta function $\beta_{x,y}^*$	m	1.1	0.3	0.45	(0.15) 0.55
Initial rms IP beam size $\sigma_{x,y}^*$	μm	6.7	3.5	9.0	(7.1 min.) 16.7
Half crossing angle	μrad	37	100	165	(250) 142.5
Peak luminosity per IP	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	5	30	16	(5, levelled) 1
Peak no. of events / crossing	—	170	1000	460	(135) 27
RMS luminous region	mm	53	49	57	(68) 45
Stored energy / beam	GJ	8.4		1.4	(0.7) 0.36
SR power / beam	kW	2400		100	(7.3) 3.6
Transv. emittance damping time	h	1.1		3.6	25.8
No. of high-luminosity IPs	—	2	2	2	(2) 2
Initial proton burn-off time	h	17	3.4	2.5	(15) 40
Allocated physics time / year	days	160	160	160	160 (160)
Average turnaround time	h	5	4	5	4 (5)
Optimum run time	h	11.6	3.7	5.3	(18–13) ~10
Accelerator availability	—	70%	70%	75%	(80%) 71%
Nominal luminosity per day	fb^{-1}	2.0	8.0	4.5	(1.9) 0.4
Luminosity per year (160 days)	fb^{-1}	≥ 250	≥ 1000	500	(350) 55

Dipole magnets



Beam envelope near IP



Synchrotron radiation screens

Table 2.2: Synchrotron radiation (SR) characteristics in the arcs of LHC, HE-LHC and FCC-hh.

Parameter	LHC	HE-LHC	FCC-hh
Linear SR power [W/m]	0.25	5.5	35
Linear photon flux [10^{16} photons/m/s]	5	27	15
Critical photon energy [eV]	44	320	4300

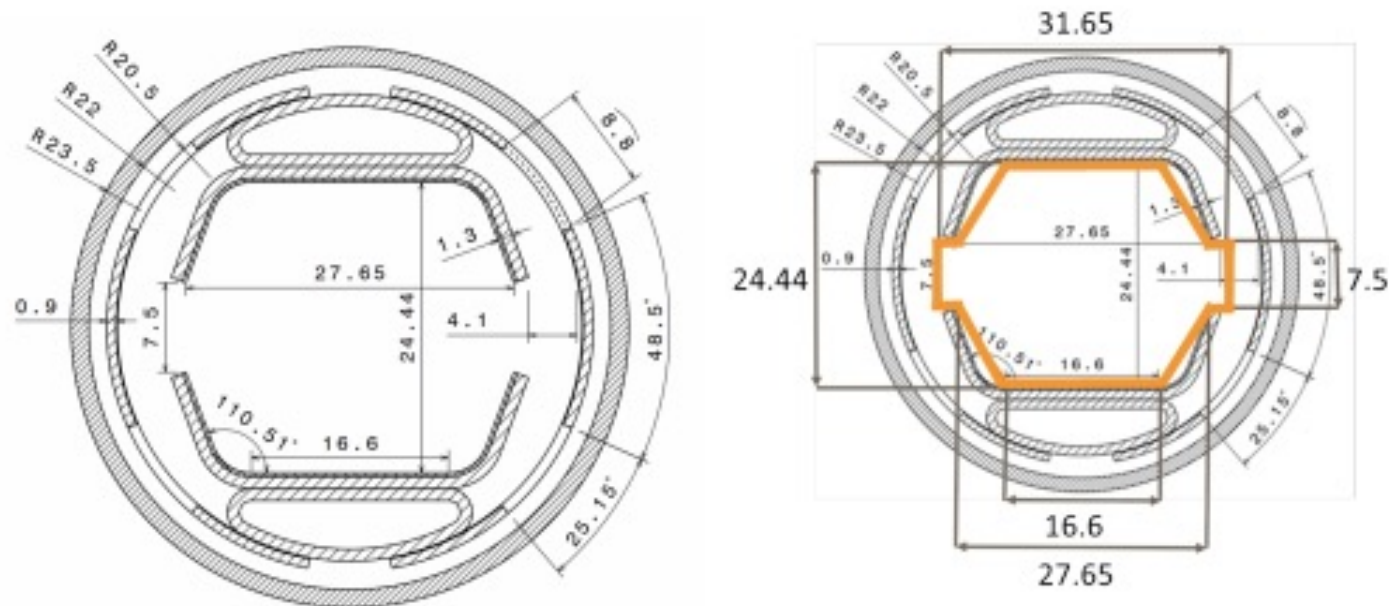


Figure 2.1: Beamscreen proposed for FCC-hh and HE-LHC [31] (left); and the approximation used for aperture calculation [32] (orange line, right).

e-p Collider ?

Table 2.13: Baseline parameters and estimated peak luminosities of future ep collider configurations based on an electron ERL, esp. HE-LHeC, when used in concurrent ep and pp operation mode [110].

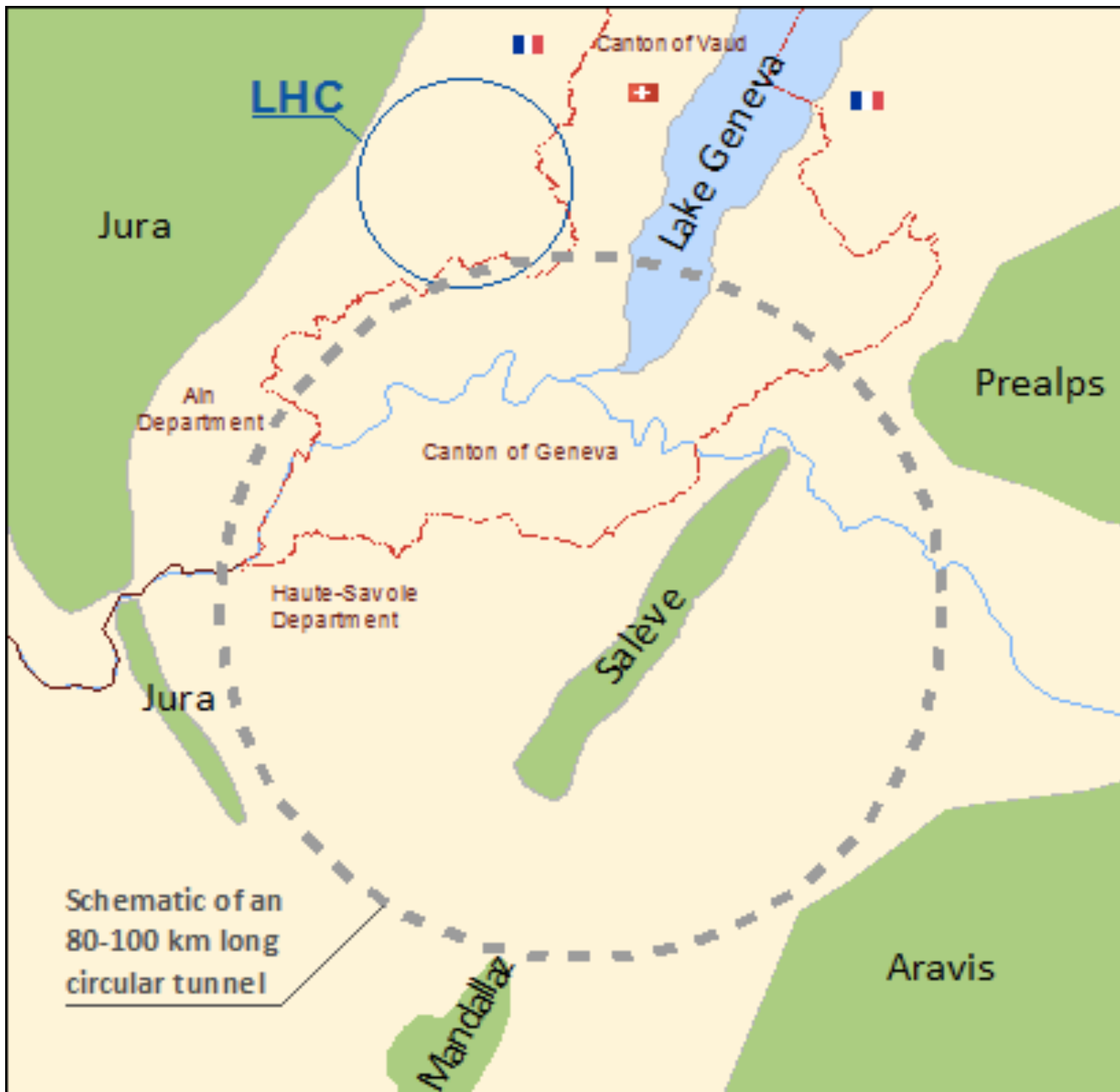
Parameter [unit]	LHeC CDR	ep at HL-LHC	ep at HE-LHC	FCC-he
E_p [TeV]	7	7	13.5	50
E_e [GeV]	60	60	60	60
\sqrt{s} [TeV]	1.3	1.3	1.7	3.5
Bunch spacing [ns]	25	25	25	25
Protons per bunch [10^{11}]	1.7	2.2	2.5	1
$\gamma\epsilon_p$ [μm]	3.7	2	2.5	2.2
Electrons per bunch [10^9]	1	2.3	3.0	3.0
Electron current [mA]	6.4	15	20	20
IP beta function β_p^* [cm]	10	7	10	15
Hourglass factor H_{geom}	0.9	0.9	0.9	0.9
Pinch factor H_{b-b}	1.3	1.3	1.3	1.3
Proton filling H_{coll}	0.8	0.8	0.8	0.8
Luminosity [$10^{33} \text{cm}^{-2} \text{s}^{-1}$]	1	8	12	15

Table 7.1: Key values relating the [detector challenges](#) at the different accelerators.

Parameter	Unit	LHC	HL-LHC	HE-LHC	FCC-hh
E_{cm}	TeV	14	14	27	100
Circumference	km	26.7	26.7	26.7	97.8
Peak \mathcal{L} , nominal (ultimate)	$10^{34} \text{cm}^{-2} \text{s}^{-1}$	1 (2)	5 (7.5)	16	30
Bunch spacing	ns	25	25	25	25
Number of bunches		2,808	2,760	2,808	10,600
Goal $\int \mathcal{L}$	ab^{-1}	0.3	3	10	30
σ_{inel} [244]	mb	80	80	86	103
σ_{tot} [244]	mb	108	108	120	150
BC rate	MHz	31.6	31.0	31.6	32.5
Peak pp collision rate	GHz	0.8	4	14	31
Peak av. PU events/BC, nominal (ultimate)		25 (50)	130 (200)	435	950
RMS luminous region σ_z	mm	45	57	57	49
Line PU density	mm^{-1}	0.2	1.0	3.2	8.1
Time PU density	ps^{-1}	0.1	0.29	0.97	2.43
$dN_{ch}/d\eta _{\eta=0}$ [244]		6.0	6.0	7.2	10.2
Charged tracks per collision N_{ch} [244]		70	70	85	122
Rate of charged tracks	GHz	59	297	1,234	3,942
$\langle p_T \rangle$ [244]	GeV/c	0.56	0.56	0.6	0.7
Bending radius for $\langle p_T \rangle$ at B=4 T	cm	47	47	49	59
Total number of pp collisions	10^{16}	2.6	26	91	324
Charged part. flux at 2.5 cm, est.(FLUKA)	GHz cm^{-2}	0.1	0.7	2.7	8.4 (10)
1 MeV-neq fluence at 2.5 cm, est.(FLUKA)	10^{16}cm^{-2}	0.4	3.9	16.8	84.3 (60)
Total ionising dose at 2.5 cm, est.(FLUKA)	MGy	1.3	13	54	270 (300)
$dE/d\eta _{\eta=5}$ [244]	GeV	316	316	427	765
$dP/d\eta _{\eta=5}$	kW	0.04	0.2	1.0	4.0

LHC HL-LHC HE-LHC FHC

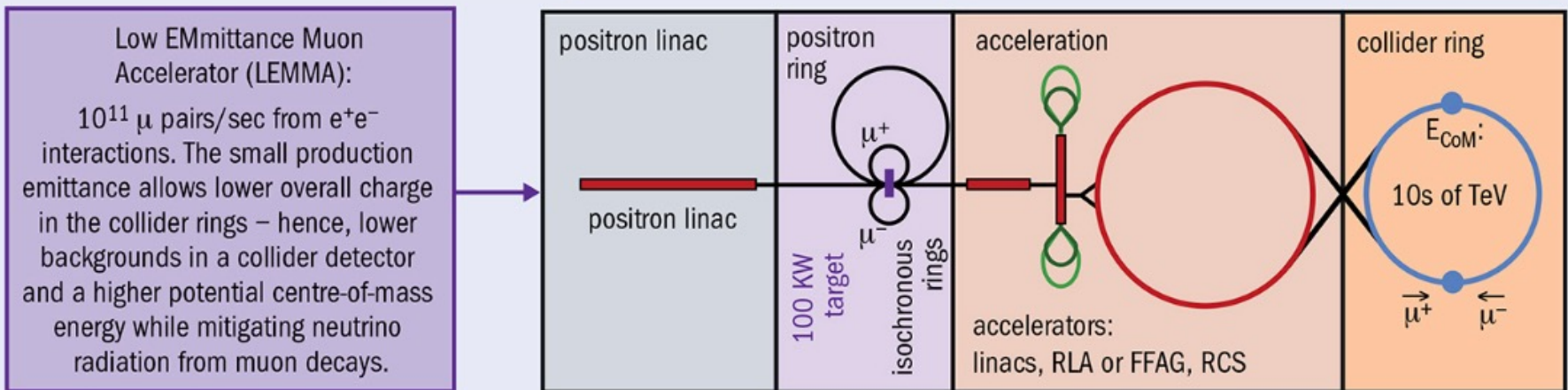
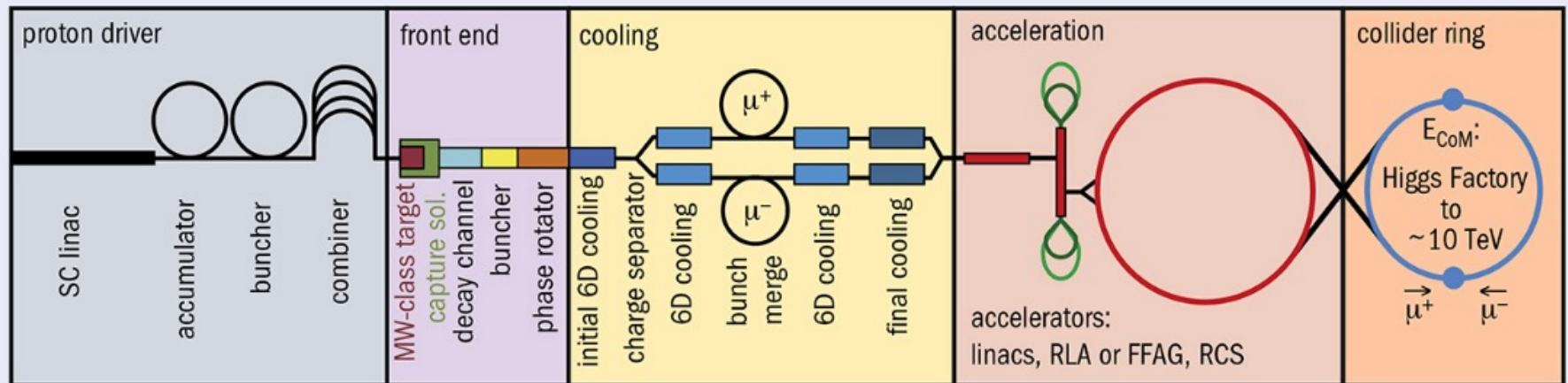
90% $b\bar{b} p_T^b > 30 \text{ GeV}/c$ [245]	$ \eta <$	3	3	3.3	4.5
VBF jet peak [245]	$ \eta $	3.4	3.4	3.7	4.4
90% VBF jets [245]	$ \eta <$	4.5	4.5	5.0	6.0
90% $H \rightarrow 4l$ [245]	$ \eta <$	3.8	3.8	4.1	4.8
$b\bar{b}$ cross-section	mb	0.5	0.5	1	2.5
$b\bar{b}$ rate	MHz	5	25	250	750
$b\bar{b} p_T^b > 30 \text{ GeV}/c$ cross-section	μb	1.6	1.6	4.3	28
$b\bar{b} p_T^b > 30 \text{ GeV}/c$ rate	MHz	0.02	0.08	1	8
Jets $p_T^{\text{jet}} > 50 \text{ GeV}/c$ cross-section [244]	μb	21	21	56	300
Jets $p_T^{\text{jet}} > 50 \text{ GeV}/c$ rate	MHz	0.2	1.1	14	90
$W^+ + W^-$ cross-section [246]	μb	0.2	0.2	0.4	1.3
$W^+ + W^-$ rate	kHz	2	10	100	390
$W^+ \rightarrow l + \nu$ cross-section [246]	nb	12	12	23	77
$W^+ \rightarrow l + \nu$ rate	kHz	0.12	0.6	5.8	23
$W^- \rightarrow l + \nu$ cross-section [246]	nb	9	9	18	63
$W^- \rightarrow l + \nu$ rate	kHz	0.1	0.5	4.5	19
Z cross-section [246]	nb	60	60	100	400
Z rate	kHz	0.6	3	25	120
$Z \rightarrow ll$ cross-section [246]	nb	2	2	4	14
$Z \rightarrow ll$ rate	kHz	0.02	0.1	1	4.2
$t\bar{t}$ cross-section [246]	nb	1	1	4	35
$t\bar{t}$ rate	kHz	0.01	0.05	1	11



Muon Collider

- Muons (like electrons) are point-like projectiles
 - All energy available in collisions \rightarrow new particles
 - Bending radiation $\gamma^4 \sim 200^4$ smaller than electrons
- Their rest lifetime is only 2 μ s
 - Accelerate them to near $v \sim c$ they survive for $\gamma\tau$
 - Long enough to make collisions
- Muon beam halo difficult for detectors

Schematic of a Muon Collider



Muon Beam halo backgrounds

